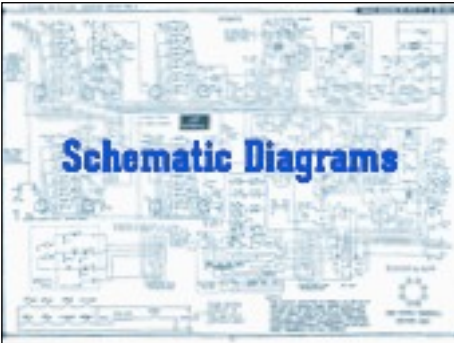


Electric Circuits



1

Schematic Diagrams



2

Schematic Icons



3

Resistance

$$R = \frac{\rho L}{A}$$

- ⊗ Resistance (Ω)
- ⊗ resistivity (Ω·m)
- ⊗ length (m)
- ⊗ area (m²)

Material	Resistivity (Ω·m)	Symbol	Resistivity (Ω·m)
Aluminum	2.82 × 10 ⁻⁸	Aluminum	2.82 × 10 ⁻⁸
Copper	1.72 × 10 ⁻⁸	Copper	1.72 × 10 ⁻⁸
Gold	2.2 × 10 ⁻⁸	Gold	2.2 × 10 ⁻⁸
Iron	9.71 × 10 ⁻⁸	Iron	9.71 × 10 ⁻⁸
Steel	1.43 × 10 ⁻⁷	Steel	1.43 × 10 ⁻⁷
Carbon	3.5 × 10 ⁻⁵	Carbon	3.5 × 10 ⁻⁵
Graphite	1.2 × 10 ⁻⁵	Graphite	1.2 × 10 ⁻⁵
Platinum	1.06 × 10 ⁻⁷	Platinum	1.06 × 10 ⁻⁷
Mercury	9.8 × 10 ⁻⁸	Mercury	9.8 × 10 ⁻⁸
Constantan	4.9 × 10 ⁻⁸	Constantan	4.9 × 10 ⁻⁸
NiCr	1.1 × 10 ⁻⁷	NiCr	1.1 × 10 ⁻⁷
Vanadium	1.9 × 10 ⁻⁸	Vanadium	1.9 × 10 ⁻⁸
Lead	2.2 × 10 ⁻⁸	Lead	2.2 × 10 ⁻⁸
Brass	7.0 × 10 ⁻⁸	Brass	7.0 × 10 ⁻⁸
Stainless Steel	7.2 × 10 ⁻⁸	Stainless Steel	7.2 × 10 ⁻⁸
Aluminum Oxide	3.44 × 10 ¹¹	Aluminum Oxide	3.44 × 10 ¹¹
Carbon	3.5 × 10 ⁵	Carbon	3.5 × 10 ⁵
Graphite	1.2 × 10 ⁵	Graphite	1.2 × 10 ⁵
Platinum	1.06 × 10 ⁸	Platinum	1.06 × 10 ⁸
Mercury	9.8 × 10 ⁷	Mercury	9.8 × 10 ⁷
Constantan	4.9 × 10 ⁷	Constantan	4.9 × 10 ⁷
NiCr	1.1 × 10 ⁸	NiCr	1.1 × 10 ⁸
Vanadium	1.9 × 10 ⁸	Vanadium	1.9 × 10 ⁸
Lead	2.2 × 10 ⁸	Lead	2.2 × 10 ⁸
Brass	7.0 × 10 ⁸	Brass	7.0 × 10 ⁸
Stainless Steel	7.2 × 10 ⁸	Stainless Steel	7.2 × 10 ⁸



4

Ohm's Law

$$V = IR$$

$$\mathcal{E} = IR$$

- Potential or Voltage (V) = Volts (V)
- Current (I) = Amperes (A)
- Resistance (R) = Ohms (Ω)



George Simon Ohm (1789-1854)




André-Marie Ampère (1775-1836)



Alessandro Giuseppe Antonio Anastasio Galvani (1737-1820)

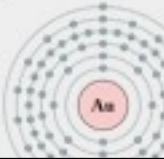
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Charles-Augustin de Coulomb (1733-1806)

- The charge of a single electron is 1.602×10^{-19} Coulombs
- or... it would take 6.241×10^{18} electrons to have a Coulomb of charge
- 1 Ampere is a current of that many electrons every second.

Electric Charge



6



Power


$P = IV$

$P = V^2/R$

$P = I^2R$

7

Resistors in Series



- The Charge has to "fight" through every resistor. This decreases the total current.

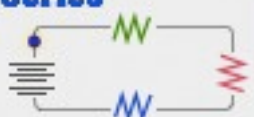
Voltage: $V = V_1 + V_2 + V_3$

Current: $I_1 = I_2 = I_3 = I_t$

Resistance: $R_t = R_1 + R_2 + R_3$

8

Series




The current starts at the top of the battery and follows a single path, clockwise, around the circuit.

	V (V)	I (A)	R (Ω)	P (W)
R_1			2	
R_2			4	
R_3			6	
TOTAL	24			

9

Series



Start with the total resistance, a simple sum of the individual values.

	V (V)	I (A)	R (Ω)	P (W)
R_1			2	
R_2			4	
R_3			6	
TOTAL	24		12	

10

Series

Use the total resistance to find the total current.
 $I = V / R$
 $= 24 / 12$
 $= 2 \text{ Amperes}$

	V (V)	I (A)	R (Ω)	P (W)
R_1			8	
R_2			4	
R_3			0	
TOTAL	24	2	12	

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Series

In a series circuit, there is only one current, so that value can be applied to each resistor.

	V (V)	I (A)	R (Ω)	P (W)
R_1		2	8	
R_2		2	4	
R_3		2	0	
TOTAL	24	2	12	

12

Series

When you have two values for a resistor, equations will get you the other numbers.
 $V = IR$
 $V = 2 \times 2 = 4 \text{ Volts}$

	V (V)	I (A)	R (Ω)	P (W)
R_1	4	2	8	
R_2	8	2	4	
R_3	12	2	0	
TOTAL	24	2	12	

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Series

Save Power for last. The sum should always equal the product.
 $P = I^2 R$
 $P_{\text{total}} = 2^2 \times 12 = 48 \text{ Watts}$

	V (V)	I (A)	R (Ω)	P (W)
R_1	4	2	8	8
R_2	8	2	4	16
R_3	12	2	0	24
TOTAL	24	2	12	48

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Resistors in Parallel

- The Charges have a choice of paths to follow.
- This decreases the total resistance

Voltage: $V = V_1 = V_2 = V_3$
 Current: $I = I_1 + I_2 + I_3$
 Resistance: $1/R_T = 1/R_1 + 1/R_2 + 1/R_3$

15

Parallel

	V (V)	I (A)	R (Ω)	P (W)
R_1			180	
R_2			60	
R_3			10	
TOTAL	12			

16

Parallel

Add the resistors
inversely
 $1/R_T = 1/R_1 + 1/R_2 + 1/R_3$
 $1/R_T = 1/180 + 1/60 + 1/10$
 $R_T = 8 \Omega$

	V (V)	I (A)	R (Ω)	P (W)
R_1			180	
R_2			60	
R_3			10	
TOTAL	12		8	

17

Parallel

If you are given the total
Voltage [EMF] resistors
in parallel all have the
same Voltage.

	V (V)	I (A)	R (Ω)	P (W)
R_1	12		180	
R_2	12		60	
R_3	12		10	
TOTAL	12		8	

18

Parallel

Use Ohm's Law to
find the currents
 $V = IR$
 $I_2 = V \div R_2$
 $I_2 = 0.2 \text{ Amperes}$

	V (V)	I (A)	R (Ω)	P (W)
R_1	12	0.1	180	
R_2	12	0.2	60	
R_3	12	1.2	10	
TOTAL	12	1.5	8	

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Parallel

Multiply V and I to
find Power.
 $P = IV$
 $P_1 = 0.1 \times 12$
 $P_1 = 1.2 \text{ Watts}$

	V (V)	I (A)	R (Ω)	P (W)
R_1	12	0.1	180	1.2
R_2	12	0.2	60	2.4
R_3	12	1.2	10	14.4
TOTAL	12	1.5	8	18

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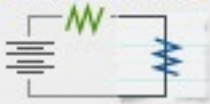
Combinations



- Some in Series, some in Parallel
- Look for parts that are only one or the other
- Find an Equivalent Resistance

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Combinations

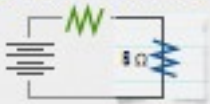


This one starts with the parallel component. Rip a piece of paper large enough to cover R_2 and R_3 .

	V (V)	I (A)	R (Ω)	P (W)
R_1			4	
R_2			18	
R_3			9	
TOTAL	80			

22

Combinations



A parallel combination of 18 and 9 can be replaced by a 6 ohm resistor

	V (V)	I (A)	R (Ω)	P (W)
R_1			4	
R_2			18	
R_3			9	
TOTAL	80			

23

Combinations



the now series of 6 and 4 creates a total resistance of 10 ohms.

	V (V)	I (A)	R (Ω)	P (W)
R_1			4	
R_2			18	
R_3			9	
TOTAL	80		10	

24

Combinations



Use Ohm's Law to find a total current of 6 amperes. This is the current throughout the SERIES.

	V (V)	I (A)	R (Ω)	P (W)
R_1		6	4	
R_2			18	
R_3			9	
TOTAL	80	6	10	

25

Combinations

Now find the voltage for R_1 and for the power.

	V (V)	I (A)	R (Ω)	P (W)
R_1	24	0	4	
R_2			18	
R_3			9	
TOTAL	80	8	10	

26

Combinations

Uncover the original circuit, keep the voltage for parallel components. [If the original is a series, keep the current.]

	V (V)	I (A)	R (Ω)	P (W)
R_1	24	0	4	
R_2	36		18	
R_3	36		9	
TOTAL	80	8	10	

27

Combinations

Finish the table with Ohm's Law and Power equations.

	V (V)	I (A)	R (Ω)	P (W)
R_1	24	0	4	144
R_2	36	2	18	72
R_3	36	4	9	144
TOTAL	80	8	10	360

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Practice

	V	I	R	P
1		4A	10	
2		4A	5	
3	60V		30	
4	48V		40	
5	48V		10	
6	72V	6A	12	
T	180	6	30	

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Practice

	V	I	R	P
1	40	4	30	100
2	20	4	5	80
3	60	2	30	180
4	48	1.2	40	97.6
5	48	4.8	30	230.4
6	72	6	12	632
T	180	6	30	1080

30

Black	0
Brown	1
Red	2
Orange	3
Yellow	4
Green	5
Blue	6
Violet	7
Gray	8
White	9

Resistor Codes

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Black	0
Brown	1
Red	2
Orange	3
Yellow	4
Green	5
Blue	6
Violet	7
Gray	8
White	9

Orange, Orange, Green, Gold

orange	3
orange	3
green	00,000

3,300,000 Ω \pm 5%
3.3 M Ω

32

Black	0
Brown	1
Red	2
Orange	3
Yellow	4
Green	5
Blue	6
Violet	7
Gray	8
White	9

Gold, Yellow, Brown, Green ?

green	5
brown	1
yellow	0,000

510,000 Ω \pm 5%
510 k Ω

33

Black	0
Brown	1
Red	2
Orange	3
Yellow	4
Green	5
Blue	6
Violet	7
Gray	8
White	9

34

5 resistors

60 12 Ω 12 Ω 36 Ω 36 Ω

35

Biggest Possible Total?

102 Ω

6 Ω 12 Ω 12 Ω 36 Ω 36 Ω

36

Smallest Possible Total?

2.57 Ω

6 Ω 12 Ω 12 Ω 36 Ω 36 Ω

37

How could you get...

60 Ω

6 Ω 12 Ω 12 Ω 36 Ω 36 Ω

38

How could you get...

4 Ω

6 Ω 12 Ω 12 Ω 36 Ω 36 Ω

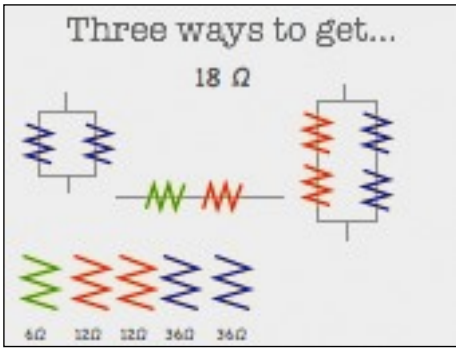
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How could you get...

7.2 Ω

6 Ω 12 Ω 12 Ω 36 Ω 36 Ω

40



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Kirchhoff's Rules

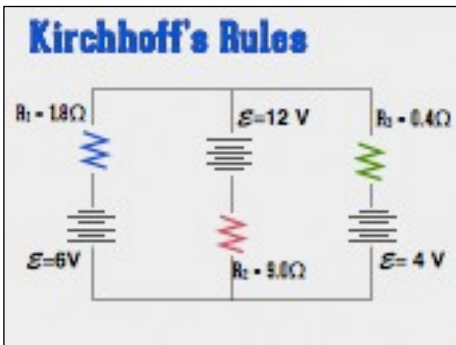
The Point Rule-
The sum of current going in to a point must equal the sum of current coming out.

$$\Sigma I_{in} = \Sigma I_{out} \quad \Sigma I = 0$$

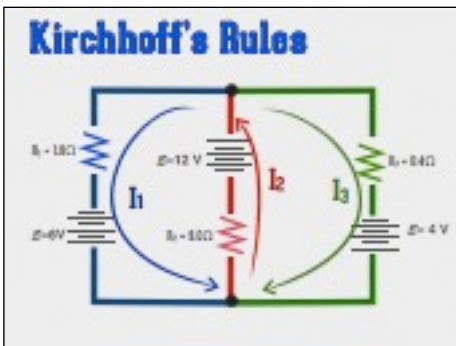
The Loop Rule-
A closed path that begins and ends at the same point will have no net change in potential.

$$\Sigma V = 0$$

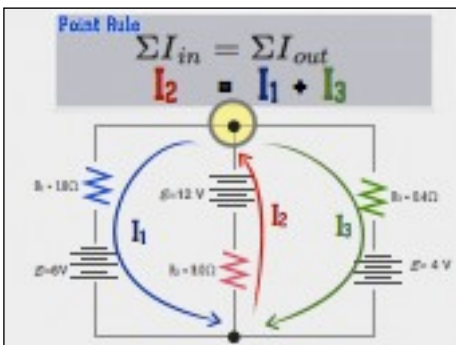
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Loop Rule $\Sigma V = 0$

$$-18I_1 + 6 - 9I_2 + 12 = 0$$

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Loop Rule $\Sigma V = 0$

$$-18I_1 + 6 - 4 + 0.4I_3 = 0$$

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Loop Rule $-18I_1 + 6 - 9I_2 + 12 = 0$ **Bring Algebra**

simplify to: $18 - 18I_1 = 9I_2$

divide by 9 to get: $2 - 0.2I_1 = I_2$ $1.23 \text{ A} = I_1$

Loop Rule $-18I_1 + 6 - 4 + 0.4I_3 = 0$

simplify to: $2 - 18I_1 = -0.4I_3$

divide by -0.4 to get: $-5 + 45I_1 = I_3$

Point Rule $I_2 = I_1 + I_3$

substitute I_2 : $2 - 0.2I_1 = I_1 - 5 + 45I_1$ substitute I_3

$$7 = 57 I_1$$

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