

ELECTROSTATICS



THE COULOMB

- Standard unit of charge
- The charge on a single electron = $-1.6 \times 10^{-19} \text{ C}$
- a proton... $1.6 \times 10^{-19} \text{ C}$
- or... 1 coulomb is 6.2×10^{18} electrons



ELECTRIC CHARGE



- Robert A. Millikan
- Oil Drop experiment published in 1913
- found the quantum value of electric charge

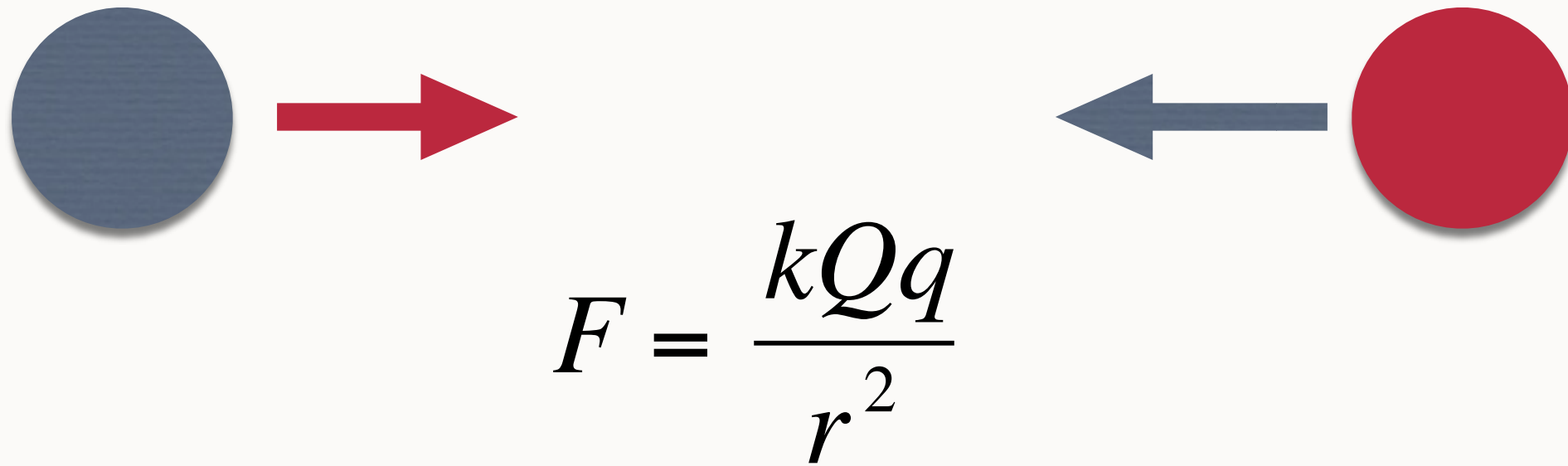
ELECTRIC FORCE



- Coulomb's Law
- Force
- Q -"Source" charge
- q -test charge
- r -distance (radius)
- $k = 9 \times 10^9 \text{ Nm}^2/\text{C}^2$

$$F = \frac{kQq}{r^2}$$

TWO CHARGES - LINEAR

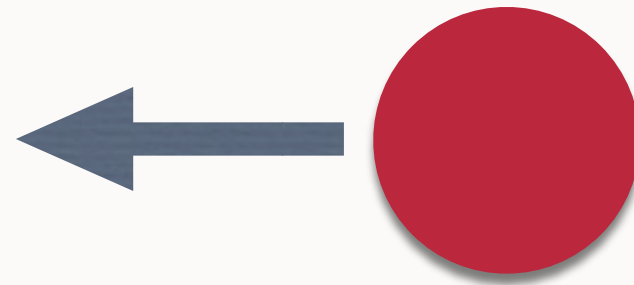


TWO CHARGES - LINEAR

$$Q = -8.6 \mu\text{C}$$



$$Q = +5.9 \mu\text{C}$$



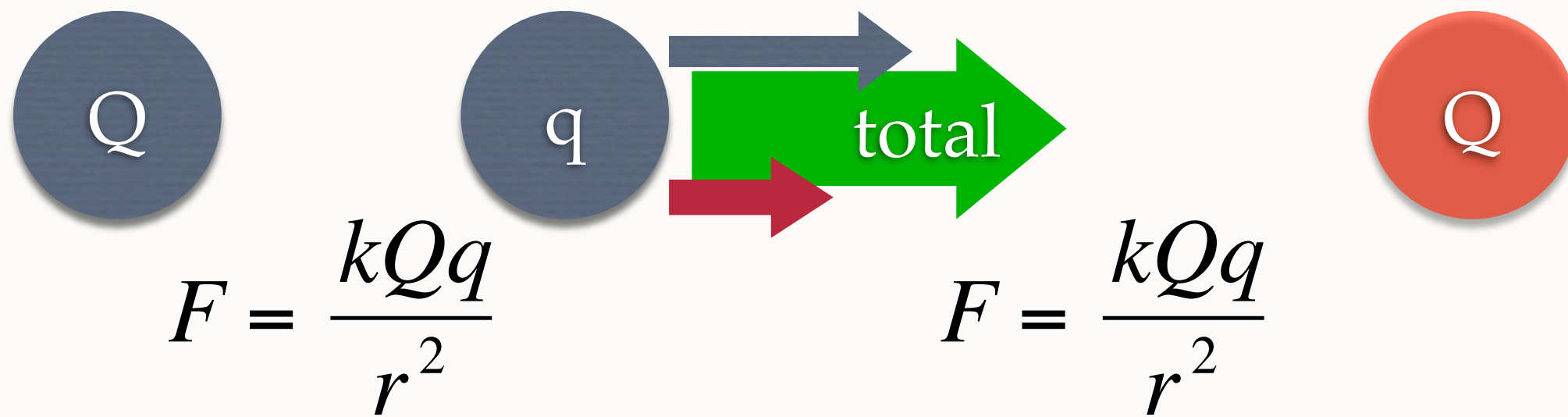
$$\text{-----} r = 0.40 \text{ m} \text{-----}$$

$$F = \frac{kQq}{r^2}$$

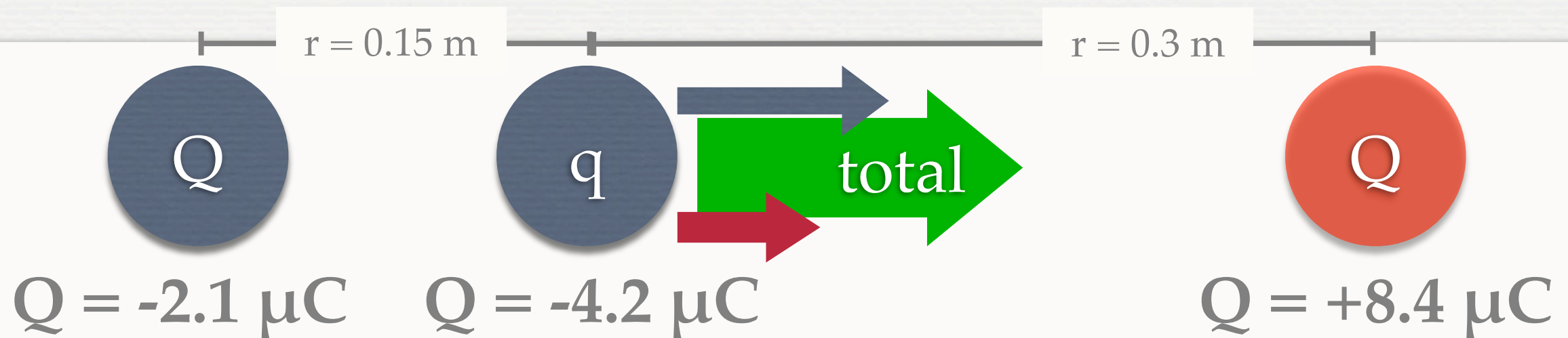
$$F = \frac{[(9 \times 10^9)(-8.6 \times 10^{-6})(5.9 \times 10^{-6})]}{(0.4^2)}$$

$$\text{-----} F = -2.85 \text{ N} \text{-----}$$

MULTIPLE CHARGES -LINEAR



MULTIPLE CHARGES -LINEAR



$$F = \frac{kQq}{r^2}$$

$$F = \frac{[(9 \times 10^9)(-2.1 \times 10^{-6})(-4.2 \times 10^{-6})]}{(0.15^2)}$$

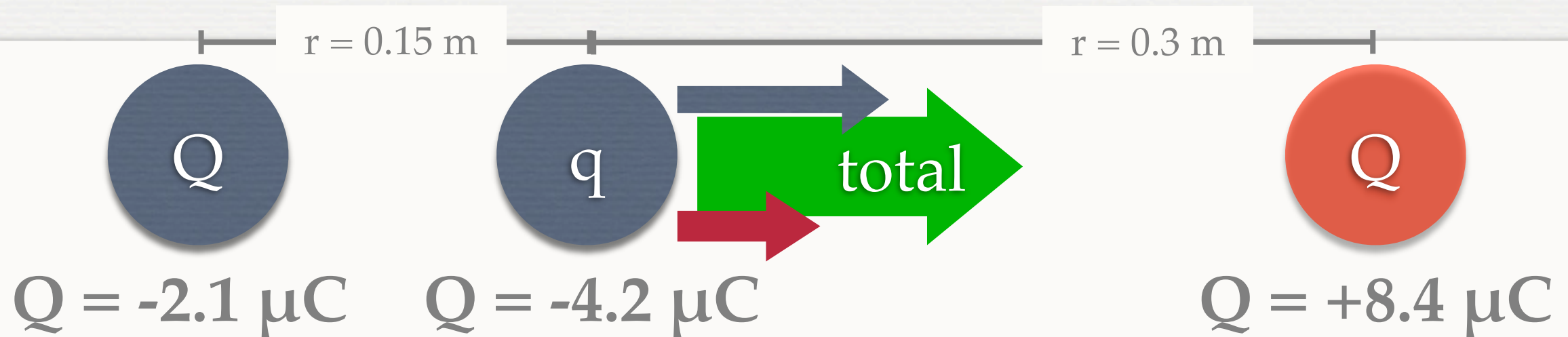
$$3.53$$

$$F = \frac{kQq}{r^2}$$

$$F = \frac{[(9 \times 10^9)(8.4 \times 10^{-6})(-4.2 \times 10^{-6})]}{(0.3^2)}$$

$$-3.53$$

MULTIPLE CHARGES -LINEAR



$$F = \frac{kQq}{r^2}$$

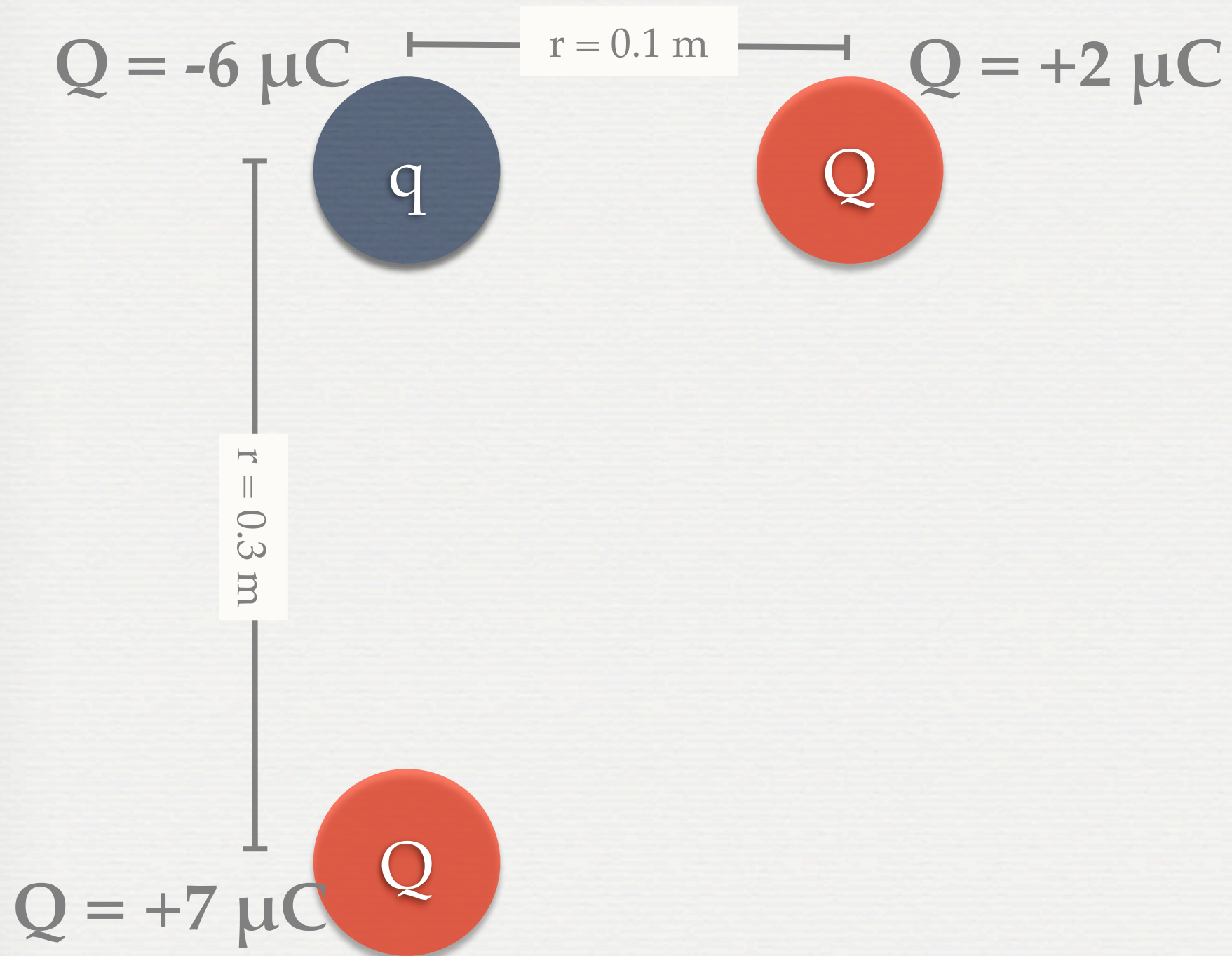
$$F = \frac{[(9 \times 10^9)(-2.1 \times 10^{-6})(-4.2 \times 10^{-6})]}{(0.15^2)}$$

$$F = \frac{kQq}{r^2}$$

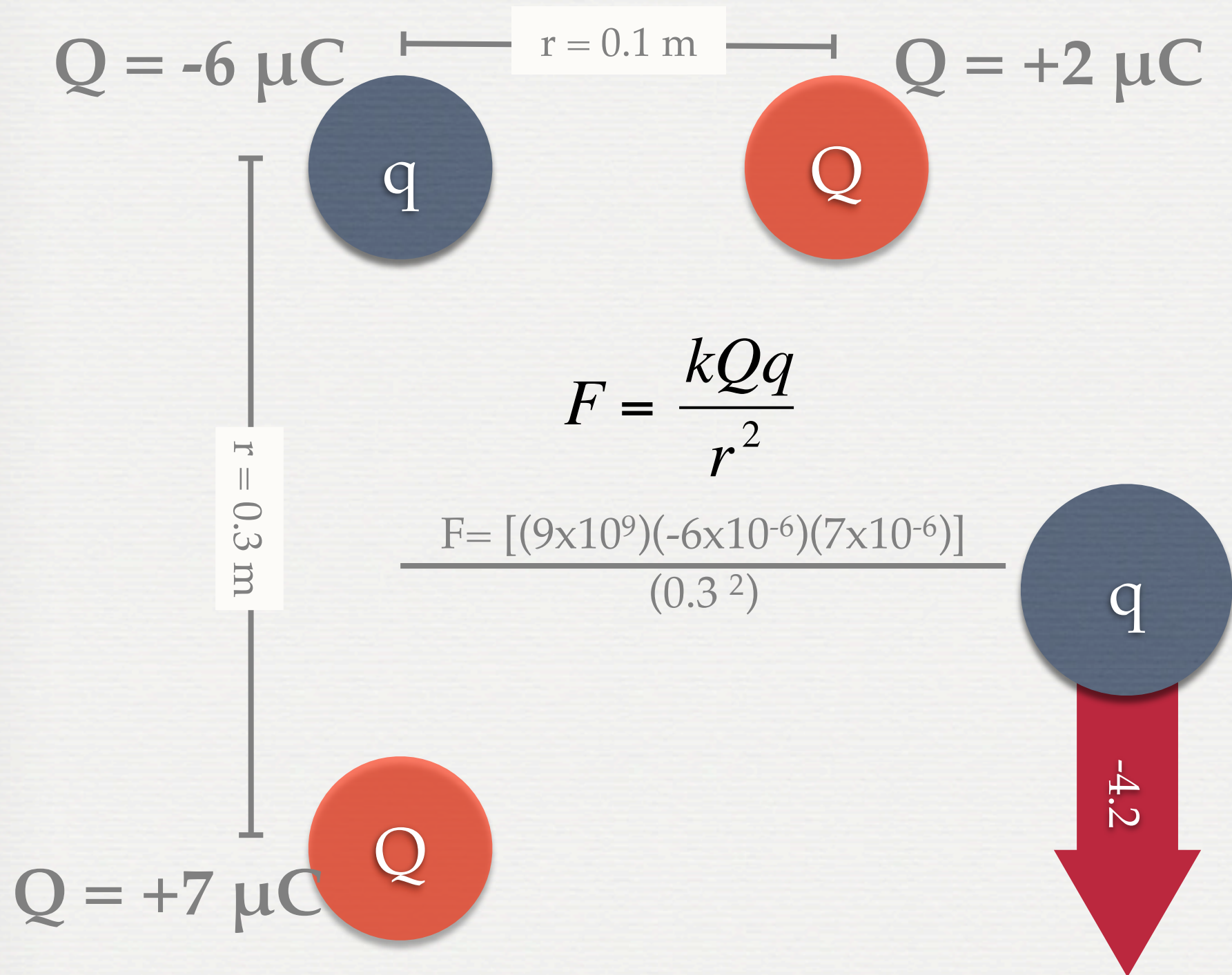
$$F = \frac{[(9 \times 10^9)(8.4 \times 10^{-6})(-4.2 \times 10^{-6})]}{(0.3^2)}$$



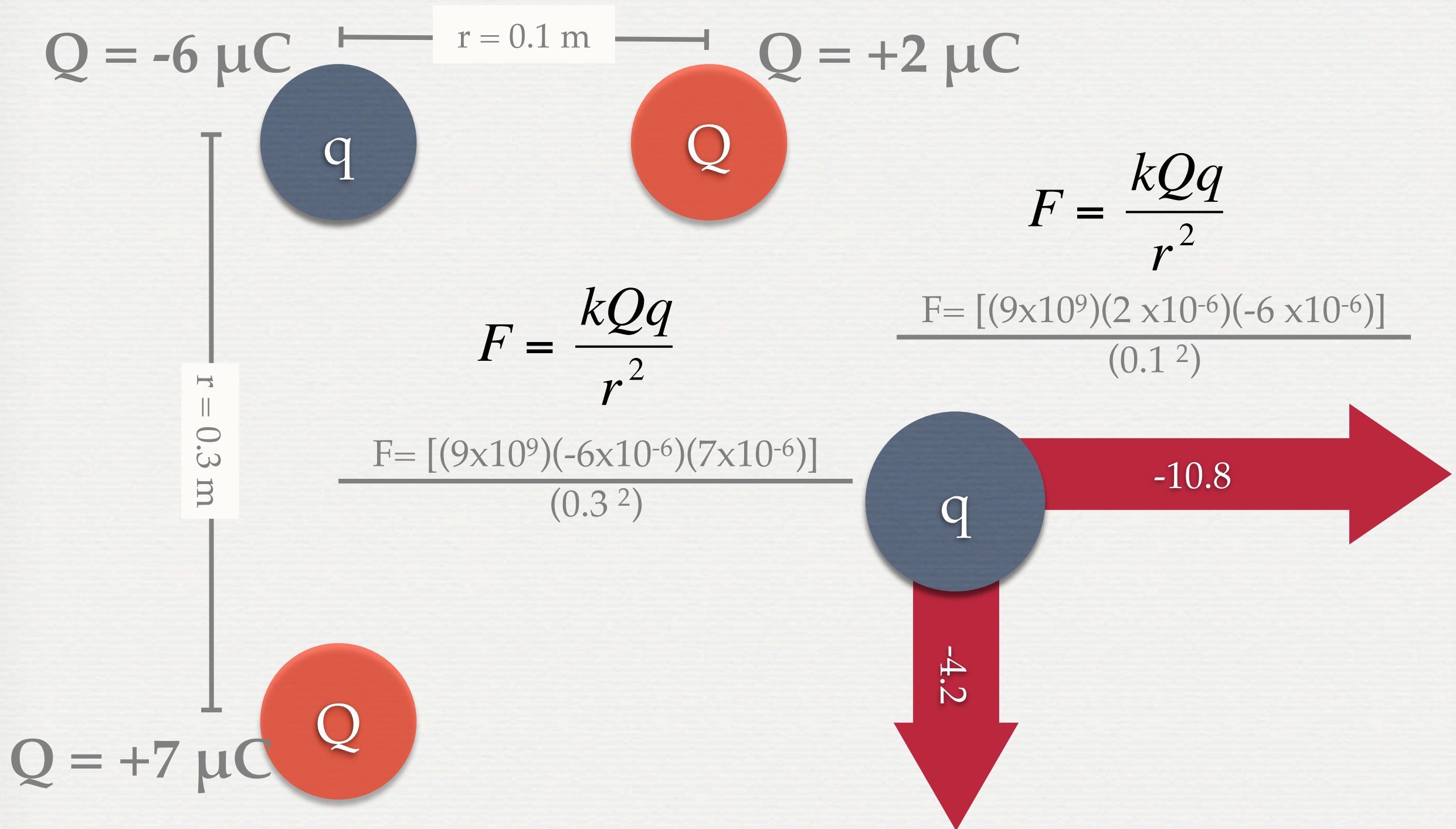
2 FORCES - NON LINEAR



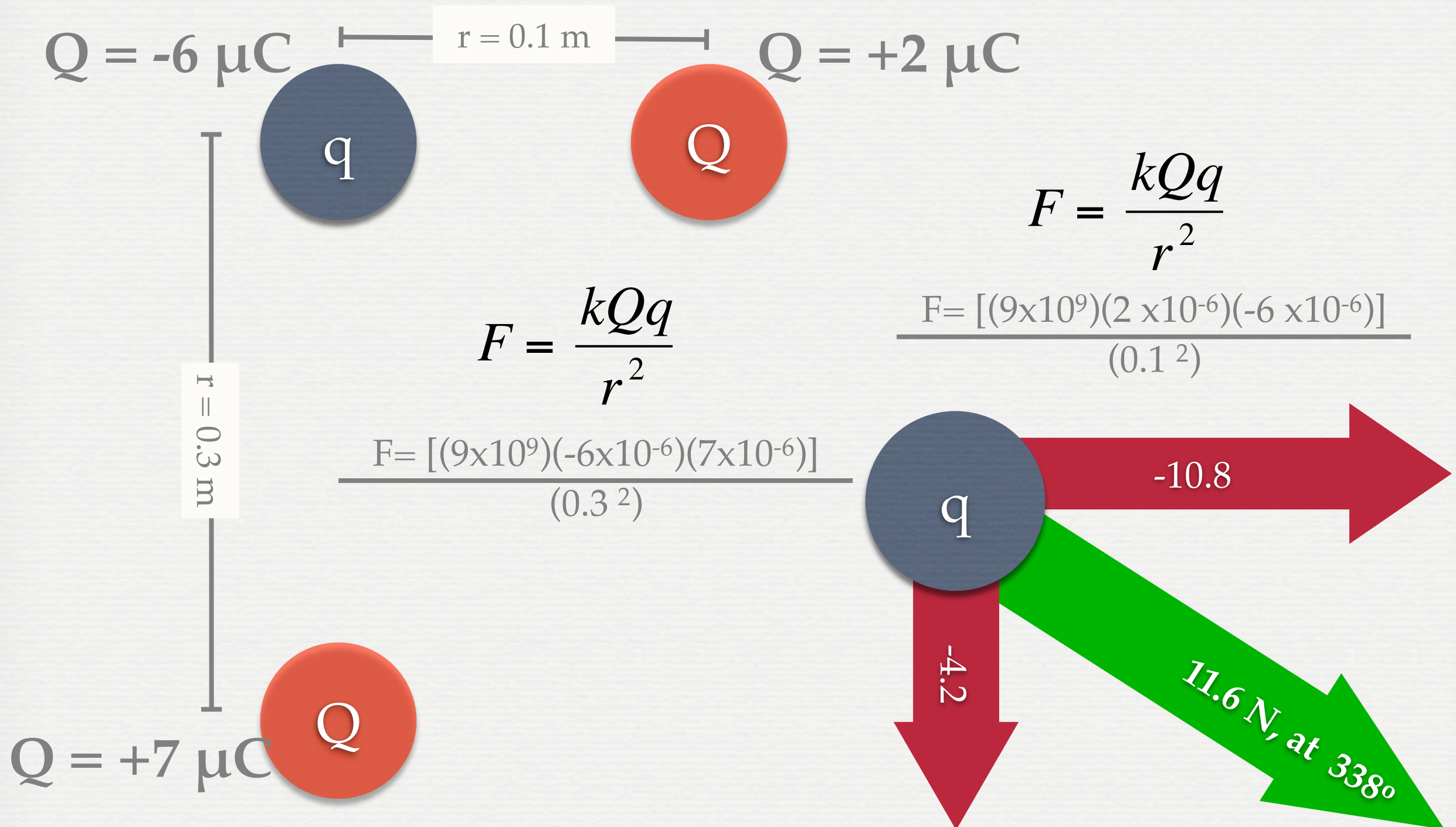
2 FORCES - NON LINEAR



2 FORCES - NON LINEAR



2 FORCES - NON LINEAR



LOOK FAMILIAR?

The relationship between charges is very similar to the force of gravity between masses, although many times stronger.

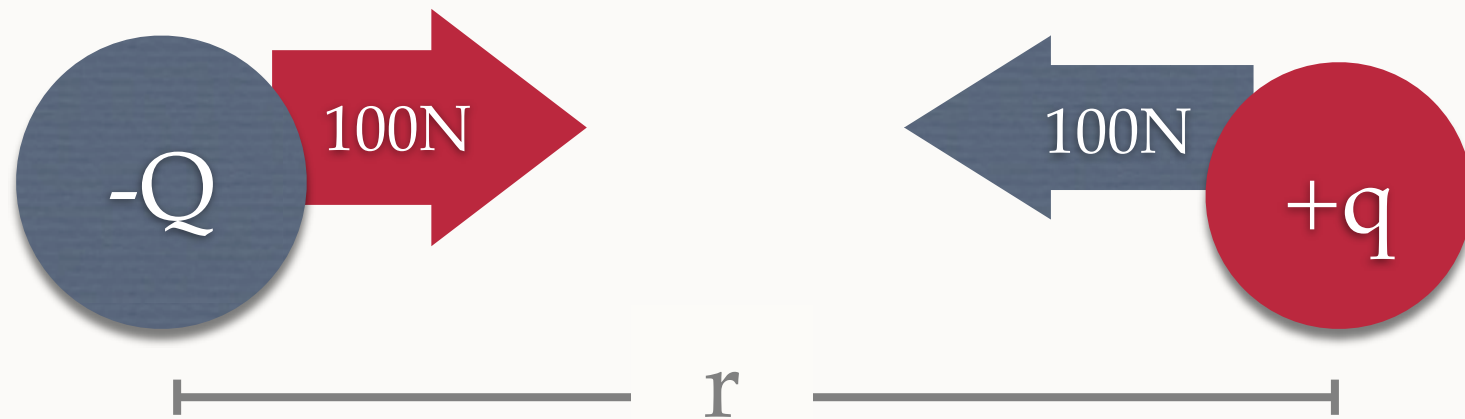
Between Planets

$$F_g = \frac{GMm}{r^2}$$



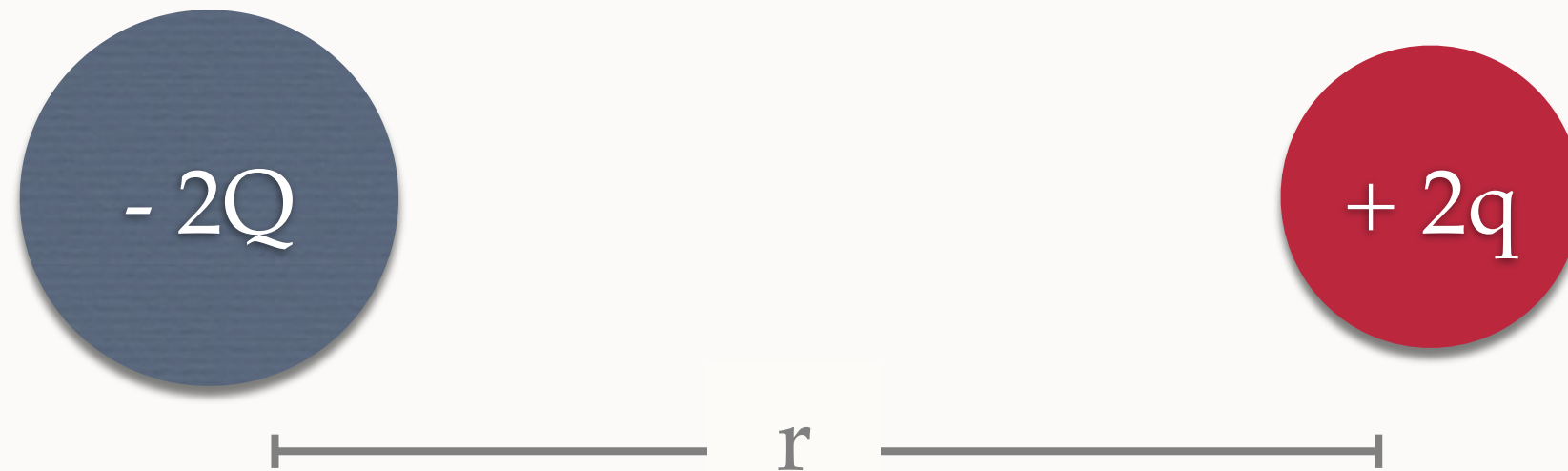
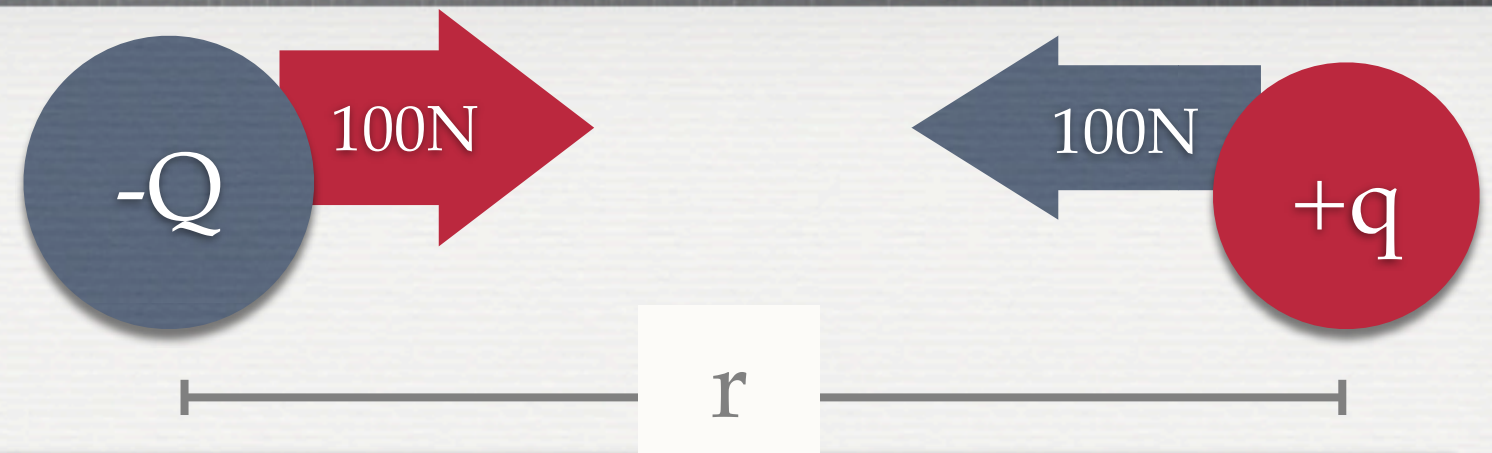
- * What is the force of attraction between the **$5.97 \times 10^{24} \text{ kg}$ Earth** and the **$7.24 \times 10^{22} \text{ kg}$ moon** that is **$3.84 \times 10^8 \text{ m}$** away?
- * **$1.955 \times 10^{20} \text{ N}$**
- * What is the result of this force?

RELATIVE CHANGES



- These two charges have a force between them of 100N

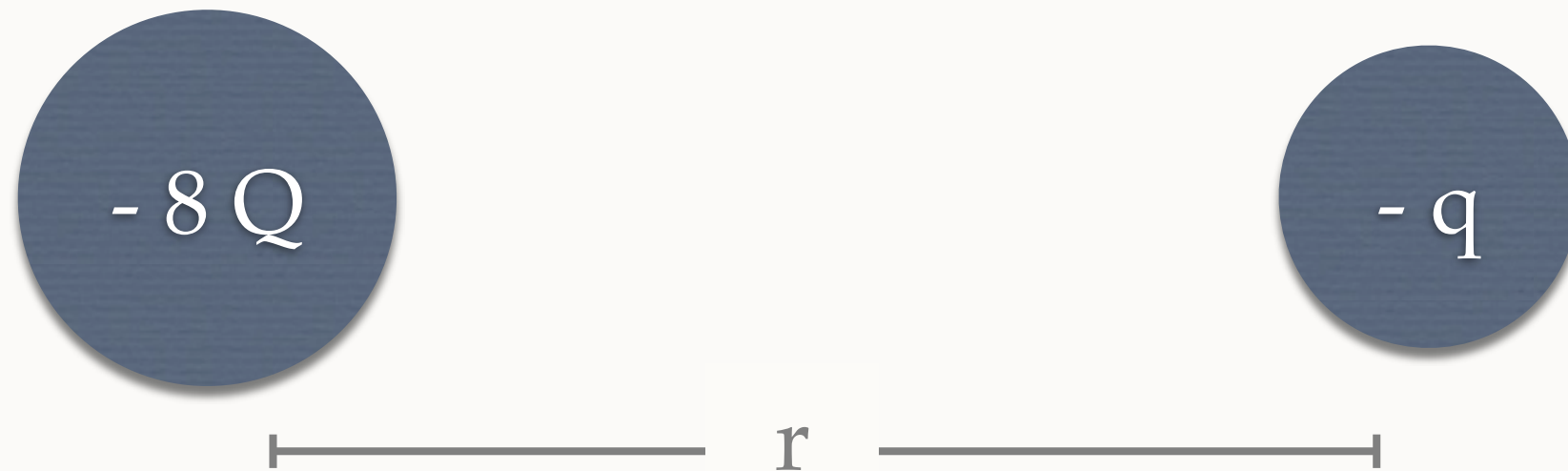
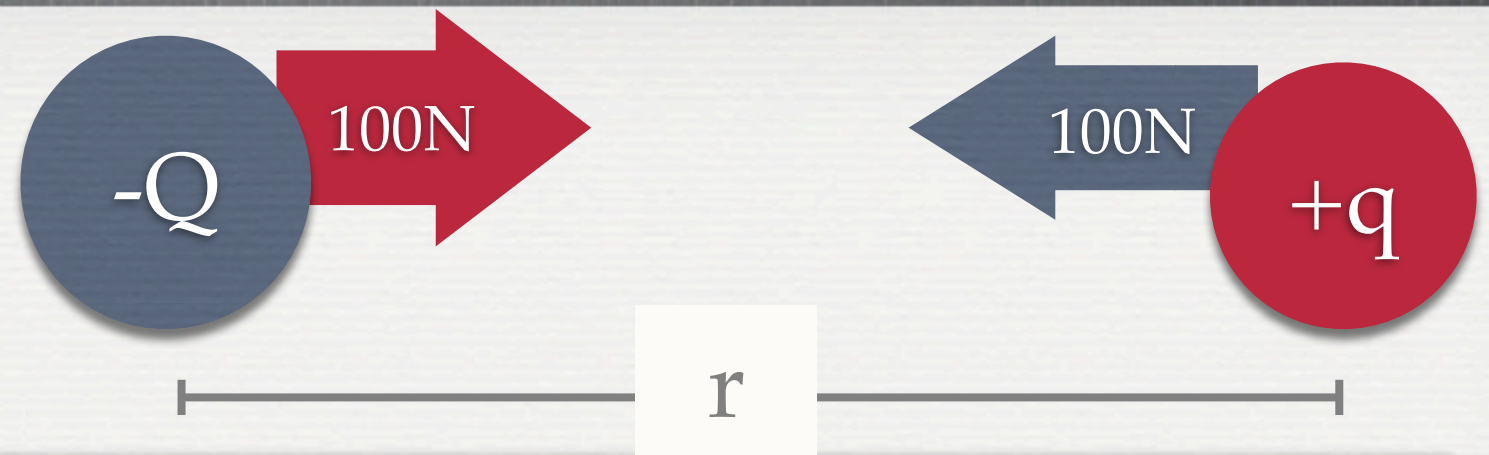
RELATIVE CHANGES



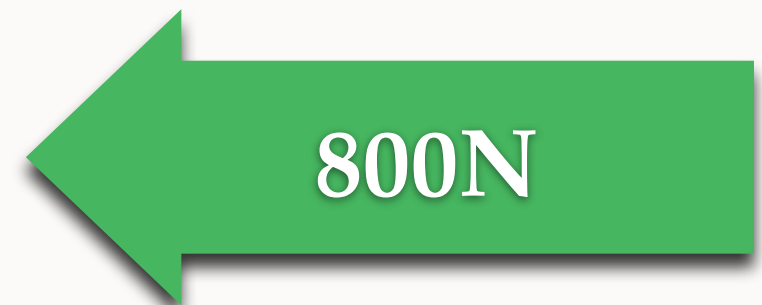
- What is the force on the left charge?



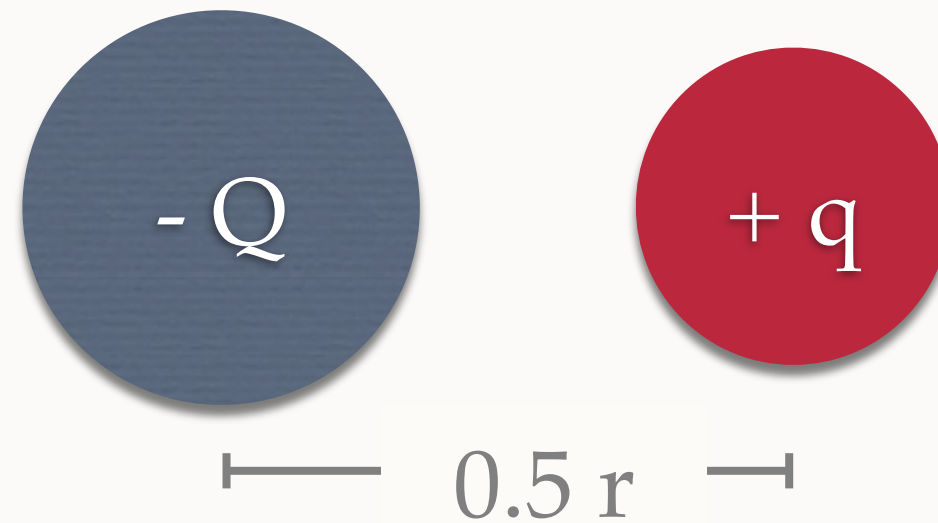
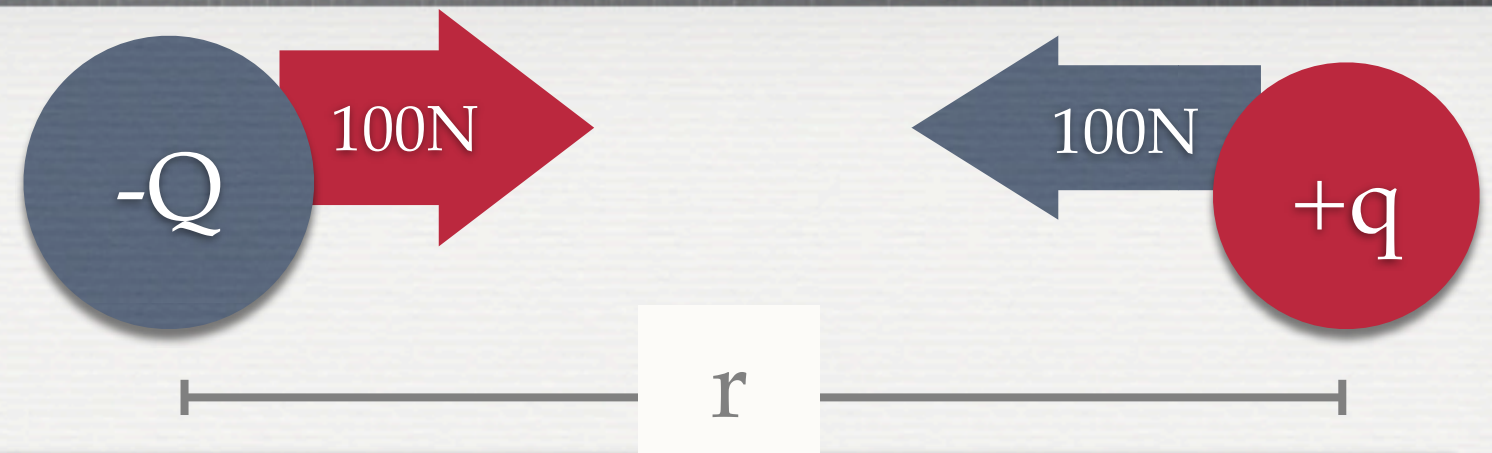
RELATIVE CHANGES



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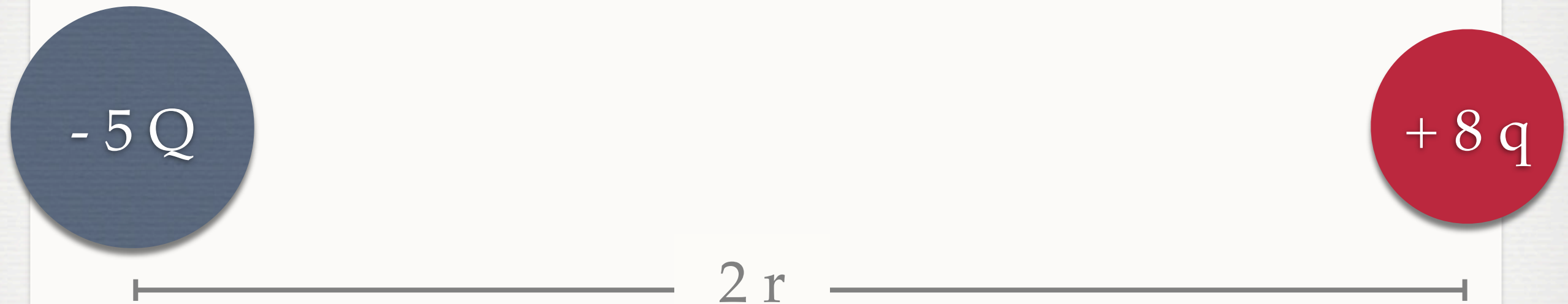
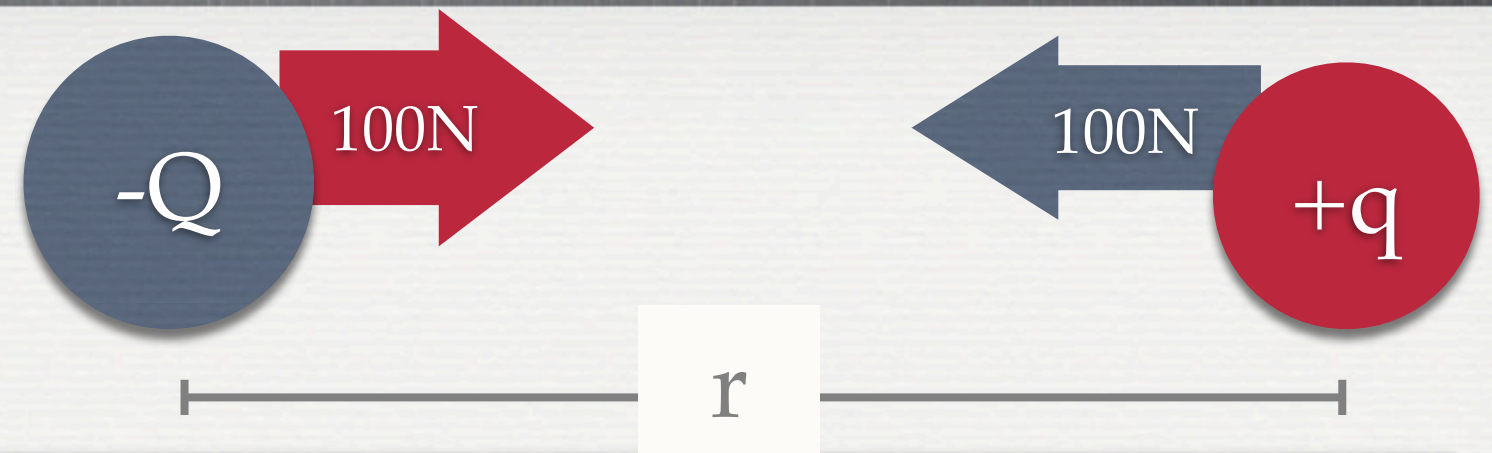
RELATIVE CHANGES



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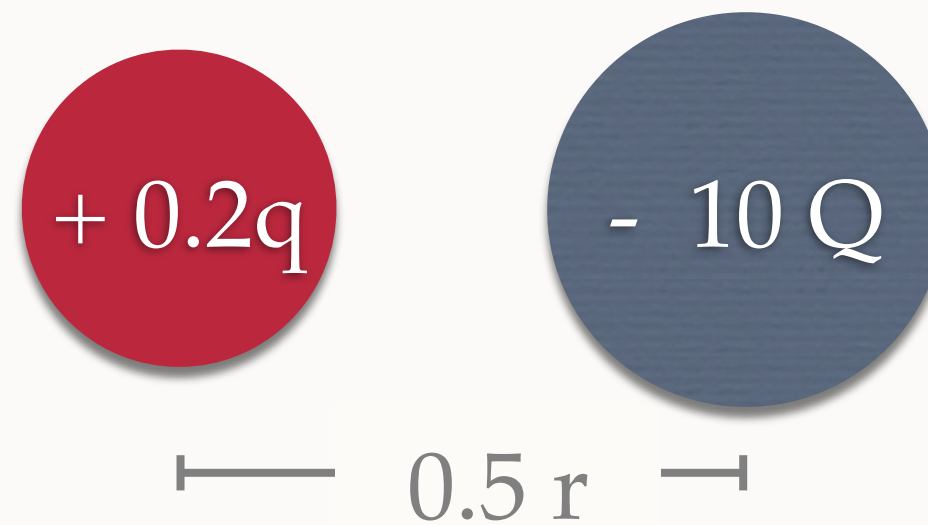
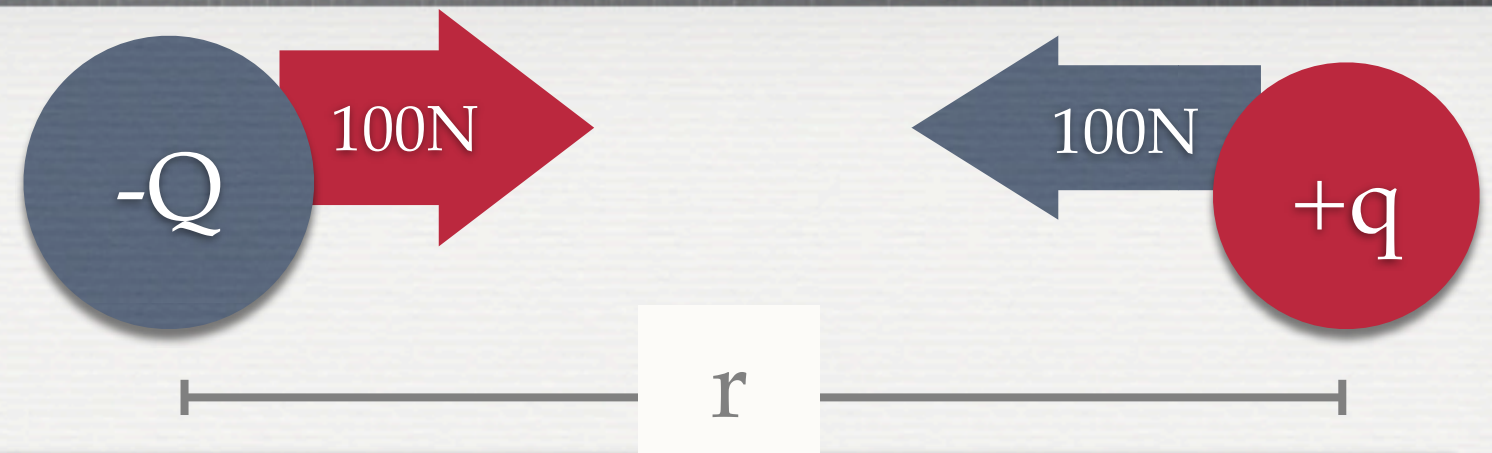
RELATIVE CHANGES



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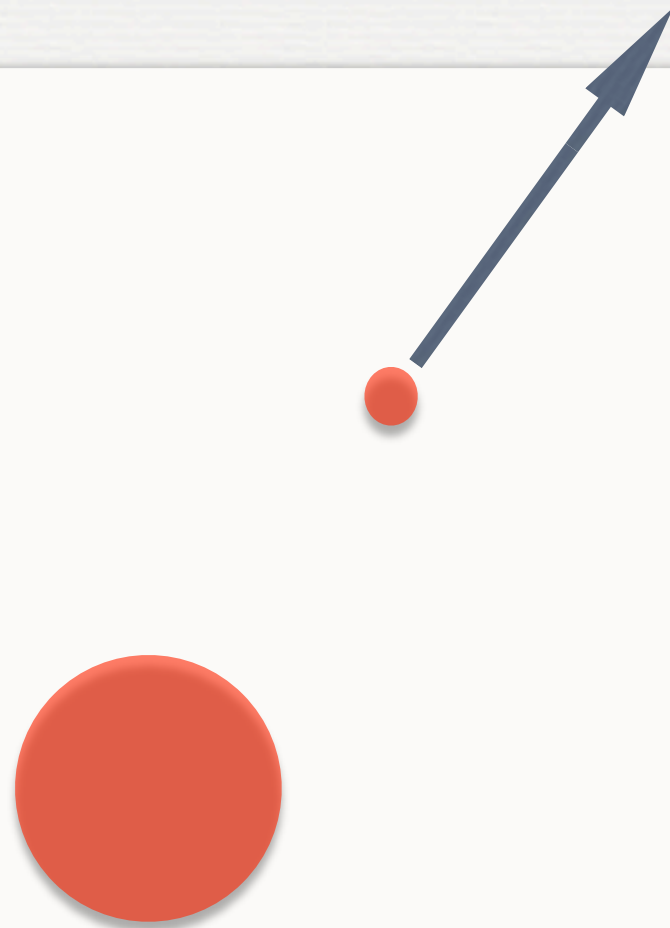
RELATIVE CHANGES



- What is the force on the left charge?

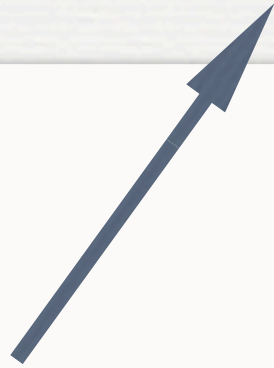
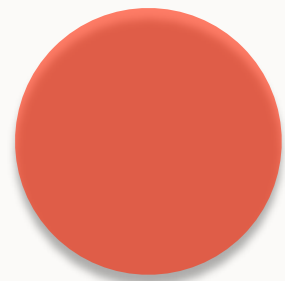


ELECTRIC FIELD



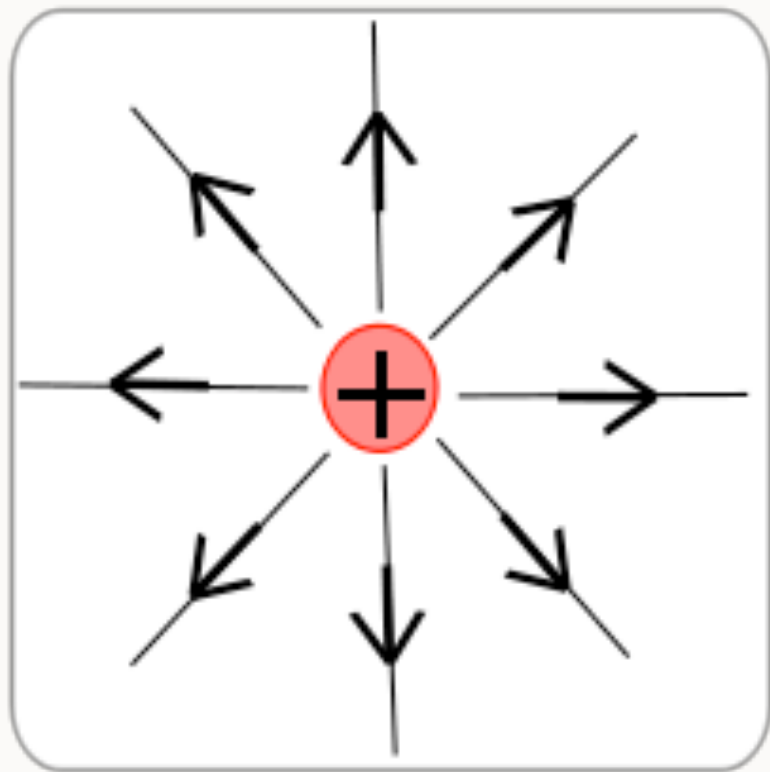
- Field Lines showing the direction of a force that **WOULD** exist on a positive charge.

ELECTRIC FIELD



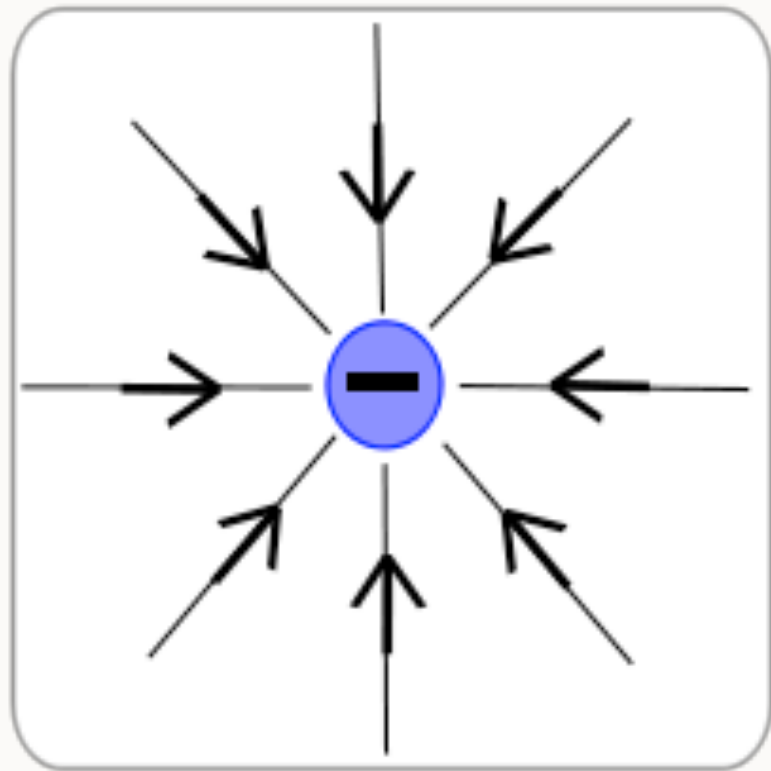
- Keep adding test charges

POSITIVE MONOPOLE



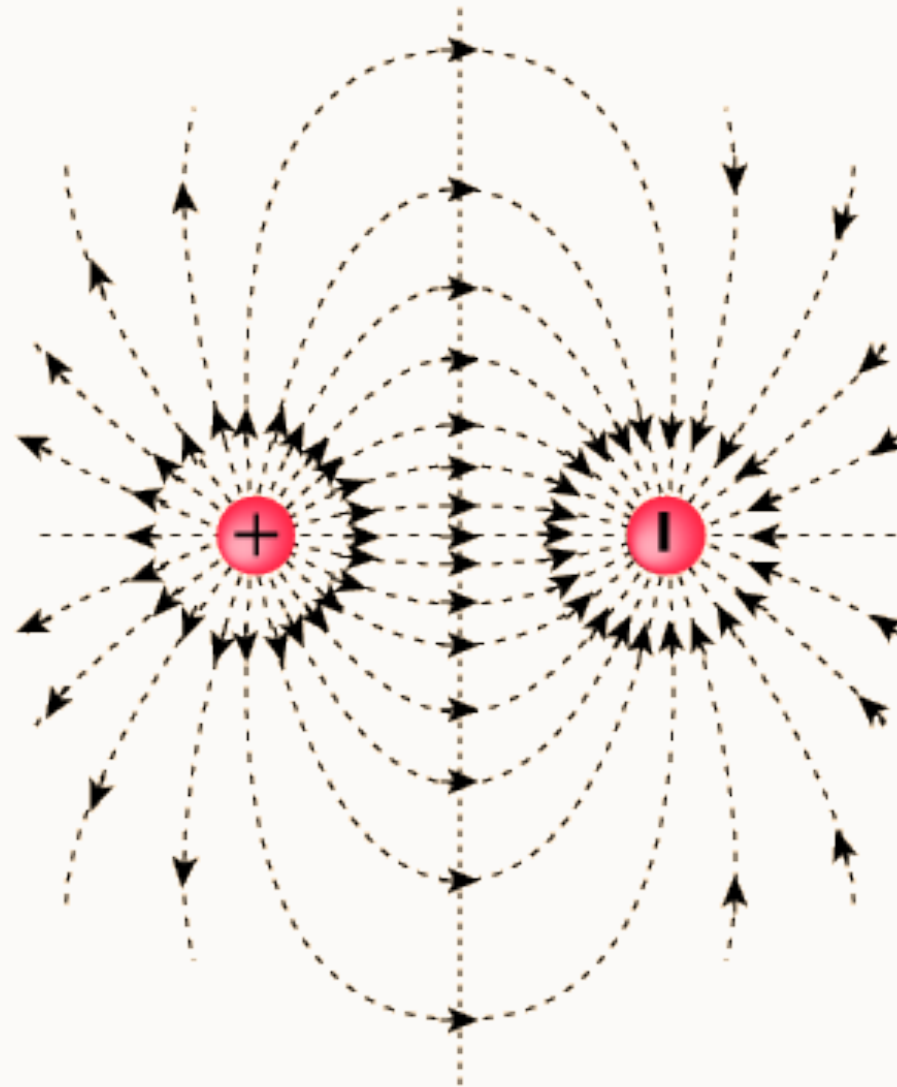
- All the lines going away from the positive charge

NEGATIVE?



- The lines would go towards the charge instead

DIPOLE



- Still, the lines go away from the positive, and towards the negative

ELECTRIC FIELD

$$E = \frac{kQ}{r^2}$$

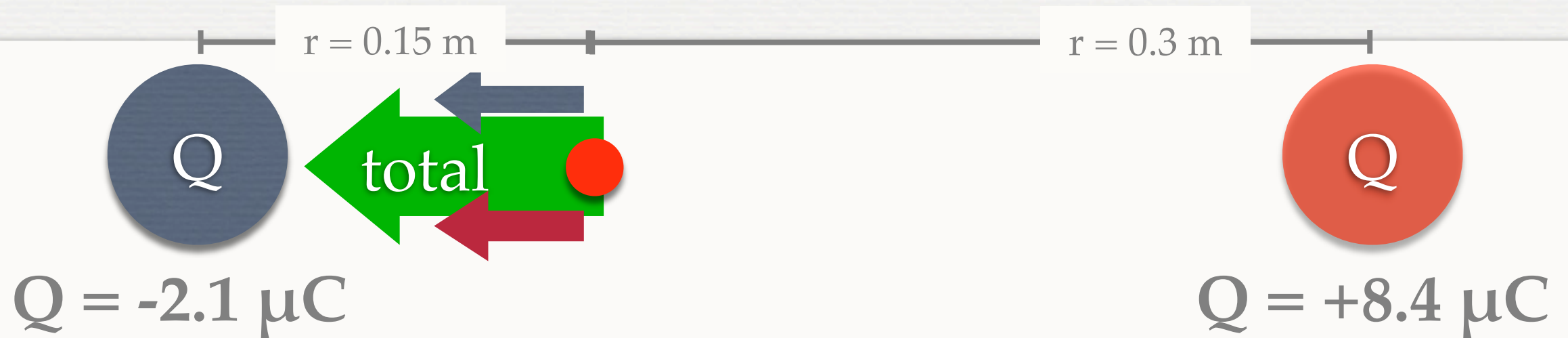
- E Electric Field
- k constant 9×10^9
- Q source charge
- r Distance from the charge

FORCE IN A FIELD

$$F = Eq$$

- The electric field shows the direction of a force that WOULD exist on a positive charge
- The actual force would be in the opposite direction for a negative charge

MULTIPLE CHARGES - E FIELD



MULTIPLE CHARGES - E FIELD

$Q = -2.1 \mu\text{C}$

$Q = +8.4 \mu\text{C}$

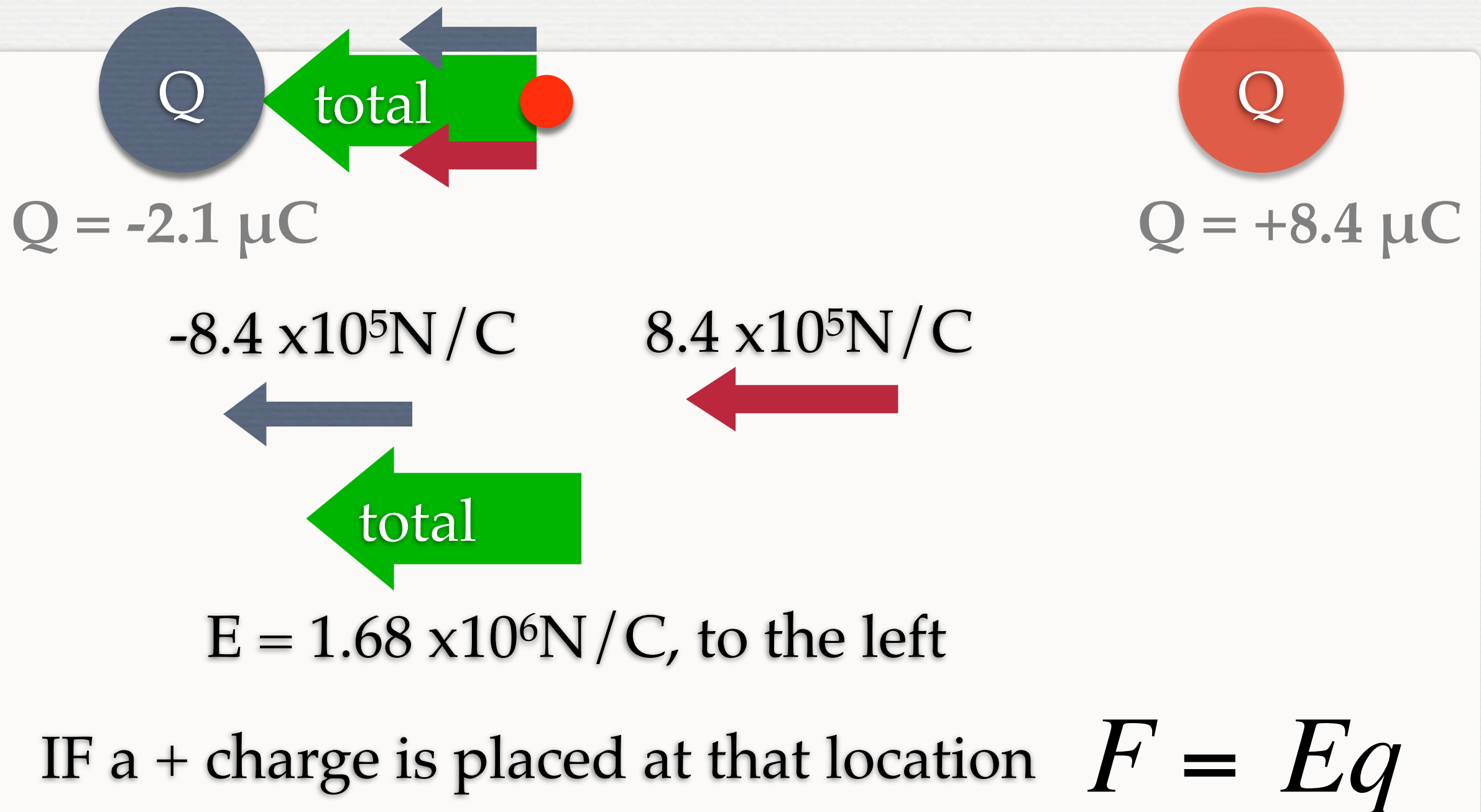
$r = 0.15 \text{ m}$

$r = 0.3 \text{ m}$

total

$$E = \frac{kQ}{r^2}$$
$$E = \frac{(9 \times 10^9)(-2.1 \times 10^{-6})}{(0.15)^2}$$
$$8.4 \times 10^5 \text{ N/C}$$
$$E = \frac{kQ}{r^2}$$
$$E = \frac{(9 \times 10^9)(8.4 \times 10^{-6})}{(0.3)^2}$$
$$8.4 \times 10^5 \text{ N/C}$$

MULTIPLE CHARGES - E FIELD



ALL THE EQUATIONS

$$F = \frac{kQq}{r^2}$$

Force (N)

Electrostatic Force

attracts or repels

ALL THE EQUATIONS

$$F = \frac{kQq}{r^2}$$

$$E = \frac{kQ}{r^2}$$

Electric Field (N/C)
similar to gravity (g) in a
gravity problem

ALL THE EQUATIONS

$$F = \frac{kQq}{r^2}$$

$$E = \frac{kQ}{r^2}$$

$$V = \frac{kQ}{r}$$

Voltage (volt)
Electric Potential
similar to the height in a
gravity problem

ALL THE EQUATIONS

$$F = \frac{kQq}{r^2}$$

$$E = \frac{kQ}{r^2}$$

$$W = \frac{kQq}{r}$$

Work or Energy (J)
similar to PE in a gravity
problem

$$V = \frac{kQ}{r}$$

ALL THE EQUATIONS

The diagram illustrates the relationships between several electrostatic equations. Green arrows indicate direct relationships, while red arrows indicate indirect or derived relationships.

$$\begin{array}{lcl} & F = \frac{kQq}{r^2} & \\ \swarrow \text{green} & & \searrow \text{red} \\ F = Eq & & W = Fr \\ \swarrow \text{green} & & \swarrow \text{red} \\ & E = \frac{kQ}{r^2} & \\ & & \searrow \text{red} \\ & & V = Er \\ \swarrow \text{green} & & \swarrow \text{red} \\ W = qV & & \\ & W = \frac{kQq}{r} & \\ & & \swarrow \text{red} \\ & V = \frac{kQ}{r} & \end{array}$$

SOLVE FOR ALL VALUES

$$Q = +8 \mu\text{C}$$

$$q = -4 \mu\text{C}$$

$$Q = +6 \mu\text{C}$$

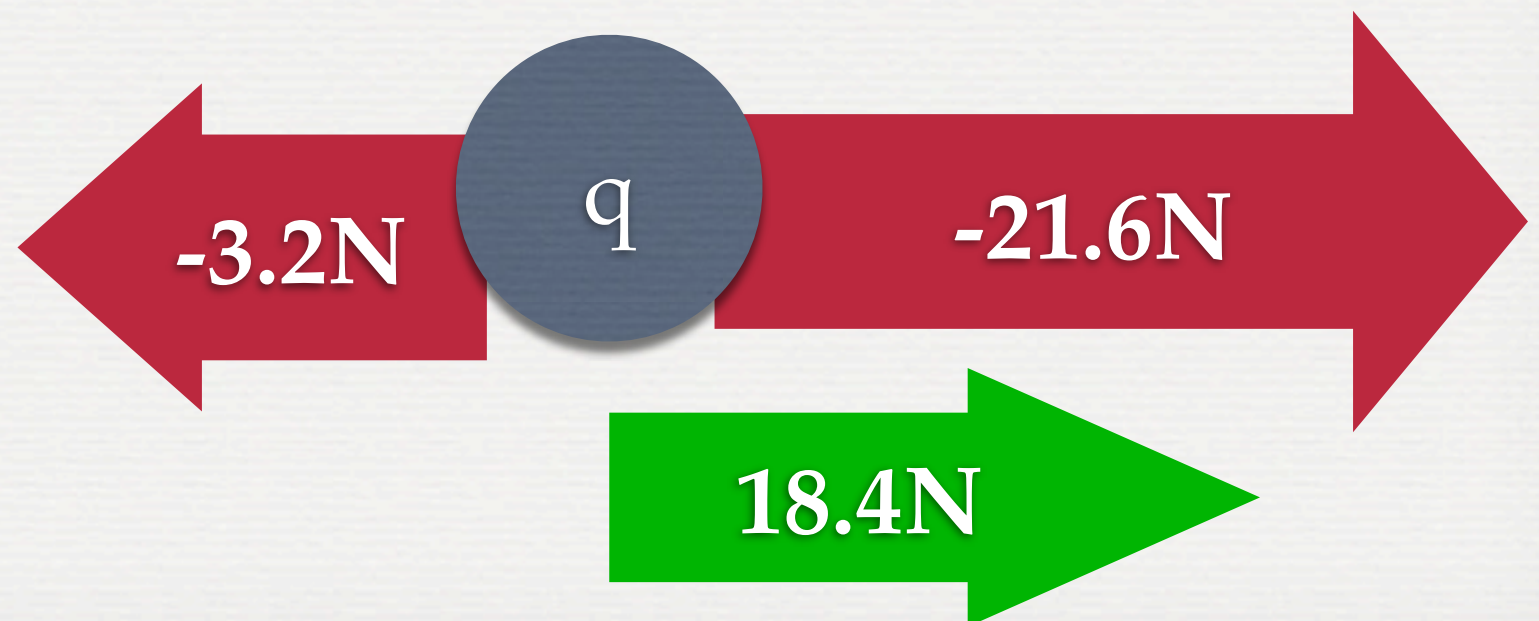


$$F = \frac{kQq}{r^2}$$

$$F = \frac{kQq}{r^2}$$

$$\frac{F = [(9 \times 10^9)(8 \times 10^{-6})(-4 \times 10^{-6})]}{(0.3^2)}$$

$$\frac{F = [(9 \times 10^9)(6 \times 10^{-6})(-4 \times 10^{-6})]}{(0.1^2)}$$



SOLVE FOR ALL VALUES

$$Q = +8 \mu\text{C}$$

$$Q = +6 \mu\text{C}$$

$$r = 0.3 \text{ m}$$

$$r = 0.1 \text{ m}$$



$$E = \frac{kQ}{r^2}$$



$$E = \frac{kQ}{r^2}$$



$$E = \frac{[(9 \times 10^9)(8 \times 10^{-6})]}{(0.3^2)}$$

$$E = \frac{[(9 \times 10^9)(6 \times 10^{-6})]}{(0.1^2)}$$

5,400,000 N/C



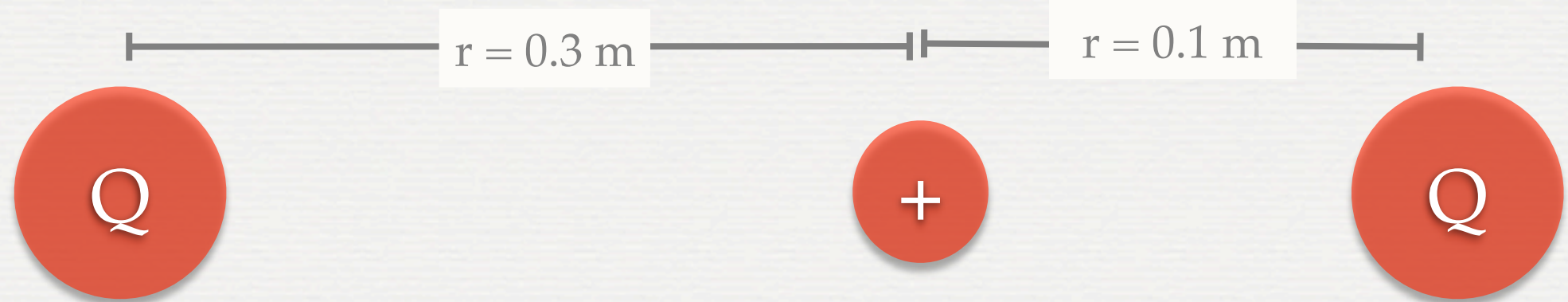
800,000 N/C

4,600,000 N/C

SOLVE FOR ALL VALUES

$$Q = +8 \mu\text{C}$$

$$Q = +6 \mu\text{C}$$



$$F = Eq$$

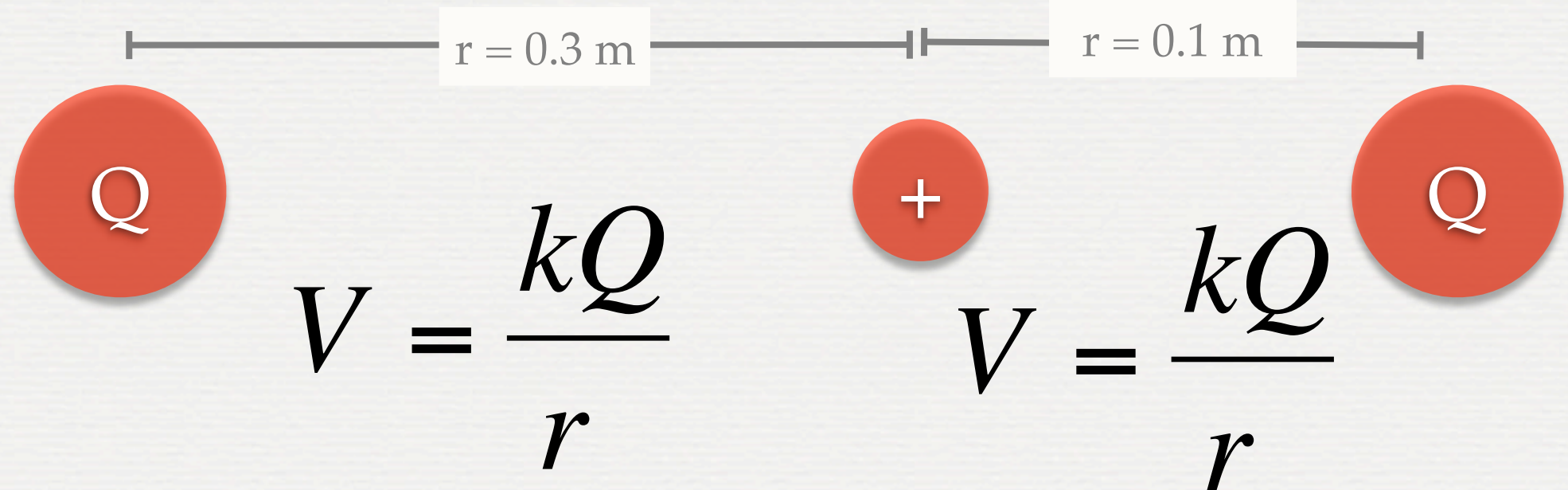
$$18.4 \text{ N} = E (-4 \times 10^{-6} \text{ C})$$



SOLVE FOR ALL VALUES

$$Q = +8 \mu\text{C}$$

$$Q = +6 \mu\text{C}$$



$$V = \frac{[(9 \times 10^9)(8 \times 10^{-6})]}{(0.3)}$$

$$V = \frac{[(9 \times 10^9)(6 \times 10^{-6})]}{(0.1)}$$

$$V = 240 \text{ kV}$$

$$V = 540 \text{ kV}$$

$$V_{\text{total}} = 780 \text{ kV}$$

SOLVE FOR ALL VALUES

$$Q = +8 \mu\text{C}$$

$$q = -4 \mu\text{C}$$

$$Q = +6 \mu\text{C}$$



$$W = \frac{kQq}{r}$$

$$W = \frac{kQq}{r}$$

$$\frac{W = [(9 \times 10^9)(8 \times 10^{-6})(-4 \times 10^{-6})]}{(0.3)}$$

$$\frac{W = [(9 \times 10^9)(6 \times 10^{-6})(-4 \times 10^{-6})]}{(0.1)}$$

$$W = -0.96 \text{ J}$$

$$W = -2.16 \text{ J}$$

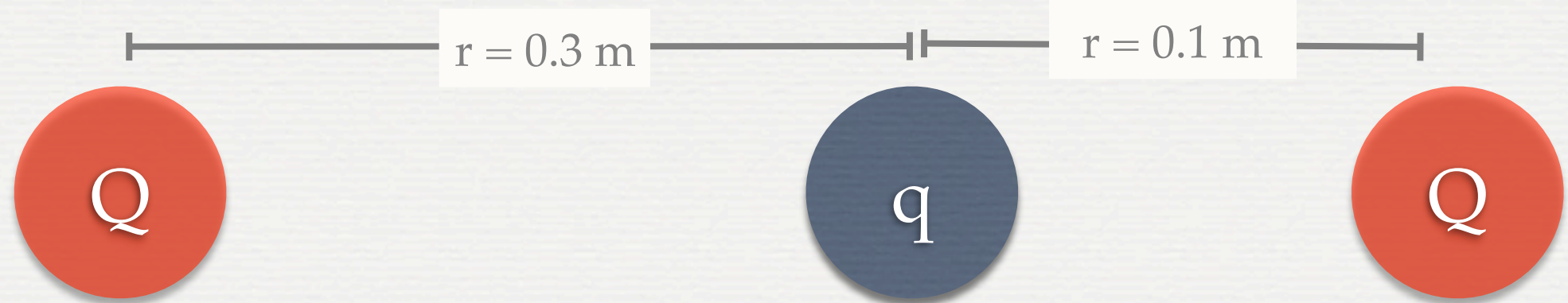
$$W_{\text{total}} = -3.12 \text{ J}$$

SOLVE FOR ALL VALUES

$$Q = +8 \mu\text{C}$$

$$q = -4 \mu\text{C}$$

$$Q = +6 \mu\text{C}$$



$$W = qV$$

$$W = (780 \times 10^3 \text{ V}) (-4 \times 10^{-6} \text{ C})$$

$$W = -3.12 \text{ J}$$

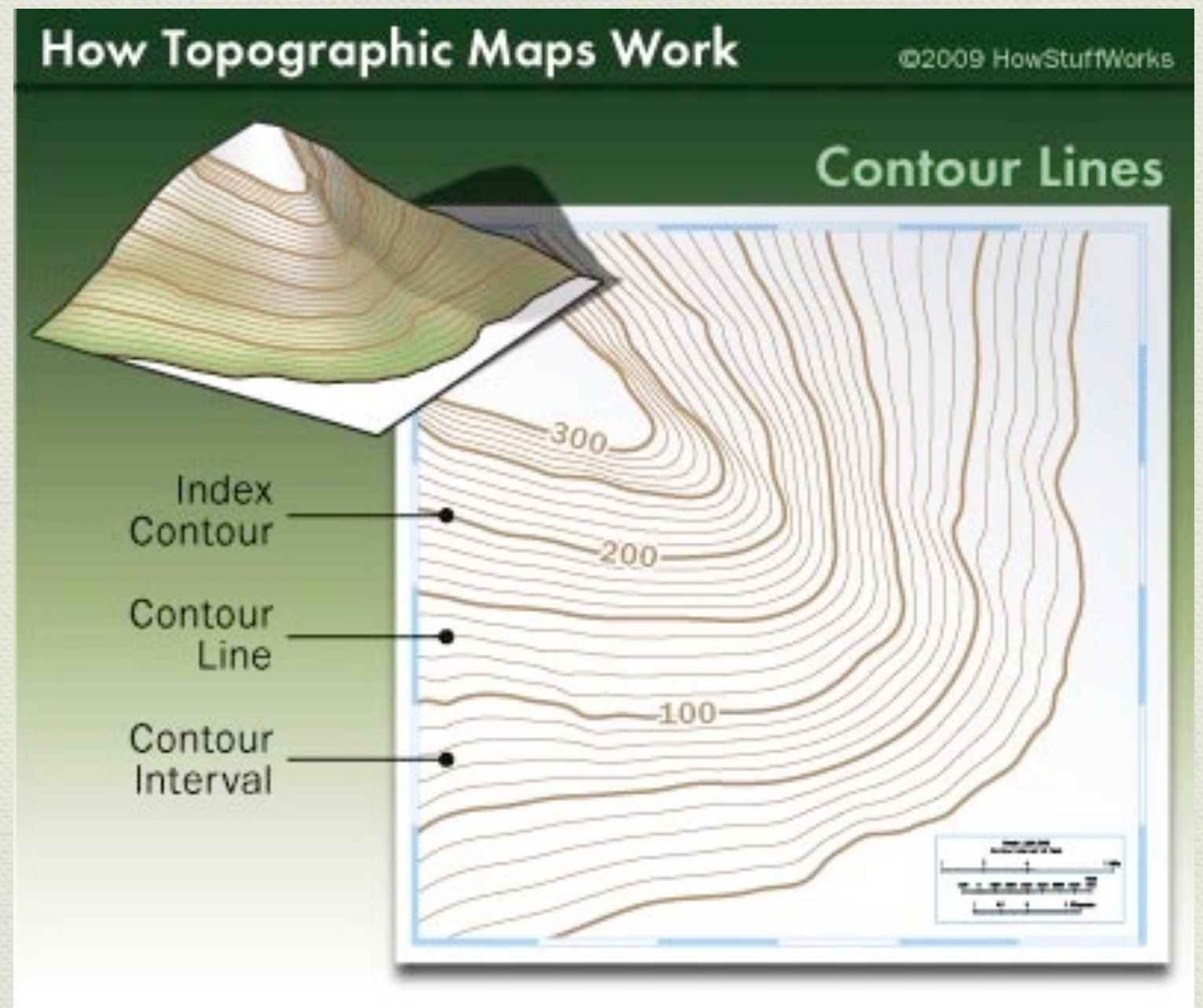


$$V_{\text{total}} = 780 \text{ kV}$$

Plotting an Electric Field

Like a Topographic Map

- ❖ Where do you start?
- ❖ What are all those curved lines for?



Potential Energy

gh (not yet mgh)



70



60



50



40



30



20



10



Force of gravity

and the path objects
would follow

