

MECHANICAL ENERGY

NEW MEANINGS

2 Volunteers

- ▶ Place a chair on the table
- ▶ Hold a chair at the same height
- ▶ the big question:
 - ▶ who did more work?




Work

$$W = F d$$

Work = Force x distance

- ▶ Joules (J) = N m
- ▶ Force and Distance must be collinear

col·lin·ear  *adj* \kə-'li-nē-ər, kă-\

Definition of COLLINEAR

1 : lying on or passing through the same straight line

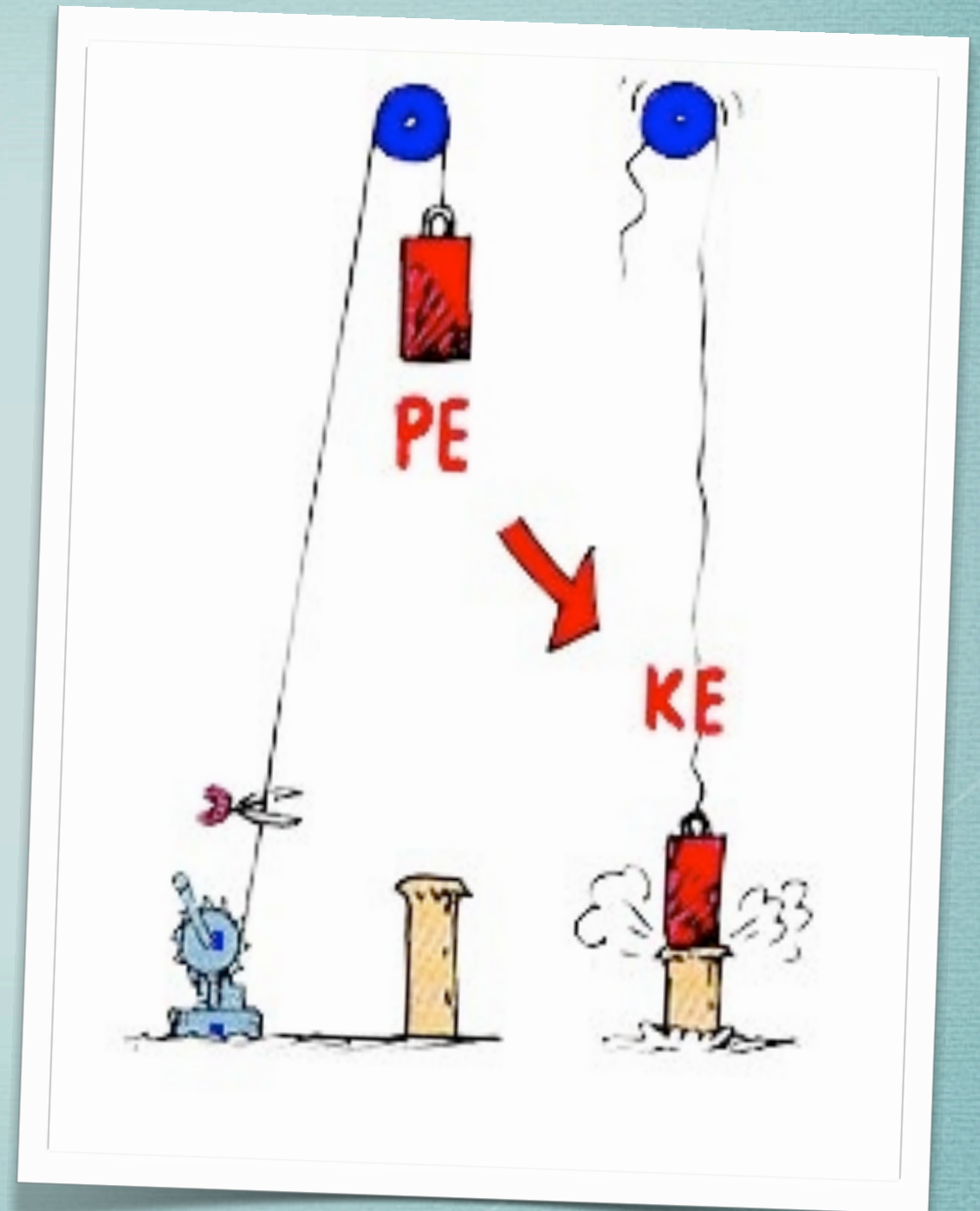
2 : having axes lying end to end in a straight line <*collinear*
antenna elements>

— col·lin·ear·i·ty  *noun*

Kinetic & Potential

Kinetic - Energy of a mass in motion

Potential - Energy stored for later



Potential Energy

$$PE = mgh$$

- ▶ mass (kg)
- ▶ gravity (9.8 m/s²)
 - ▶ height (m)
- ▶ the height must be relative to some “ground” level

Kinetic Energy

$$KE = \frac{1}{2}mv^2$$

- ▶ mass (kg)
- ▶ velocity (m/s)
- ▶ KE is often relative to an original velocity of 0 m/s (0 Joules)

Conservation of Energy

- ▶ Find the total Energy at any one point
- ▶ The total can not change in a closed system
- ▶ KE is often used to find final velocities

Another Volunteer

Another Volunteer

- ▶ A race to put the chair on the desktop

Another Volunteer

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Another Volunteer

- ▶ A race to put the chair on the desktop
- ▶ Who was stronger?



Another Volunteer

- ▶ A race to put the chair on the desktop
- ▶ Who was stronger?
- ▶ Who did more Work?



Another Volunteer

- ▶ A race to put the chair on the desktop
- ▶ Who was stronger?
- ▶ Who did more Work?
- ▶ So what's the difference?



Power

How Fast Work is Done

$$P = \text{Work} / \text{time}$$

▶ Watts (W) = J/s

▶ 1 hp = 550 ft lb / s = 746 W



Sled Pull

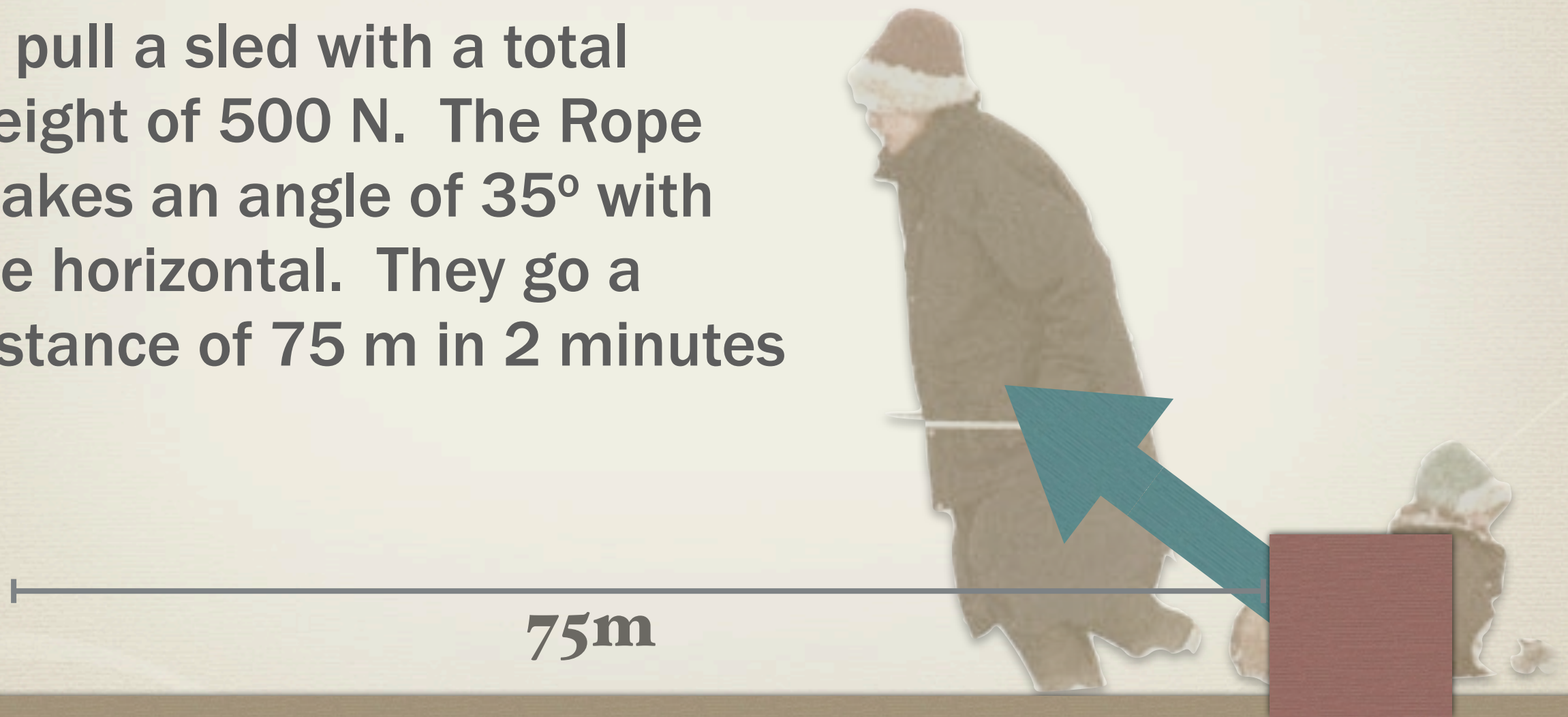
Work and Power

- ▶ A Father uses a force of 150N to pull a sled with a total weight of 500 N . The Rope makes an angle of 35° with the horizontal. They go a distance of 75 m in 2 minutes



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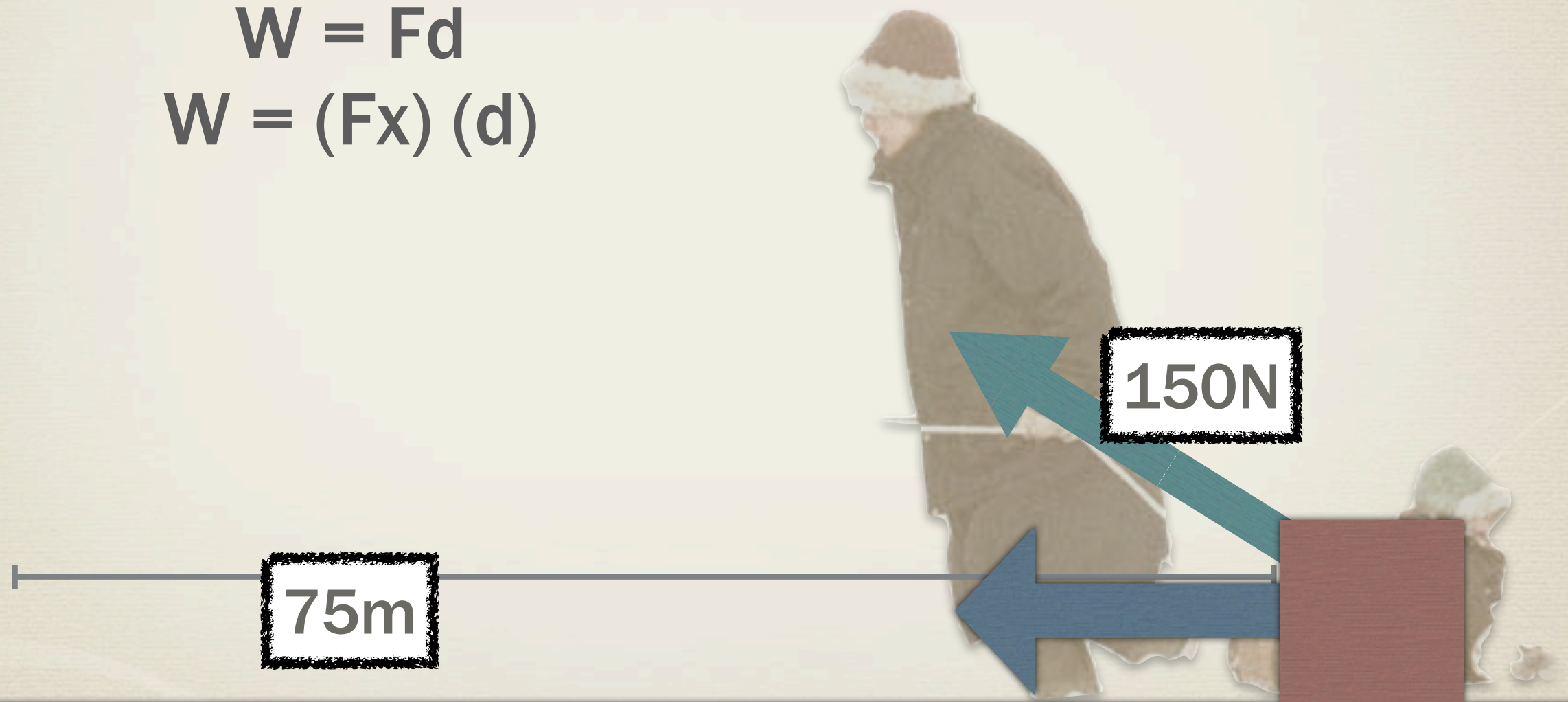
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Work and Power

- ▶ A Father uses a force of 150 N to pull a sled with a total weight of 500 N. The Rope makes an angle of 35 degrees with the horizontal. They go a distance of 75 m in 2 minutes

$$W = Fd$$
$$W = (Fx) (d)$$



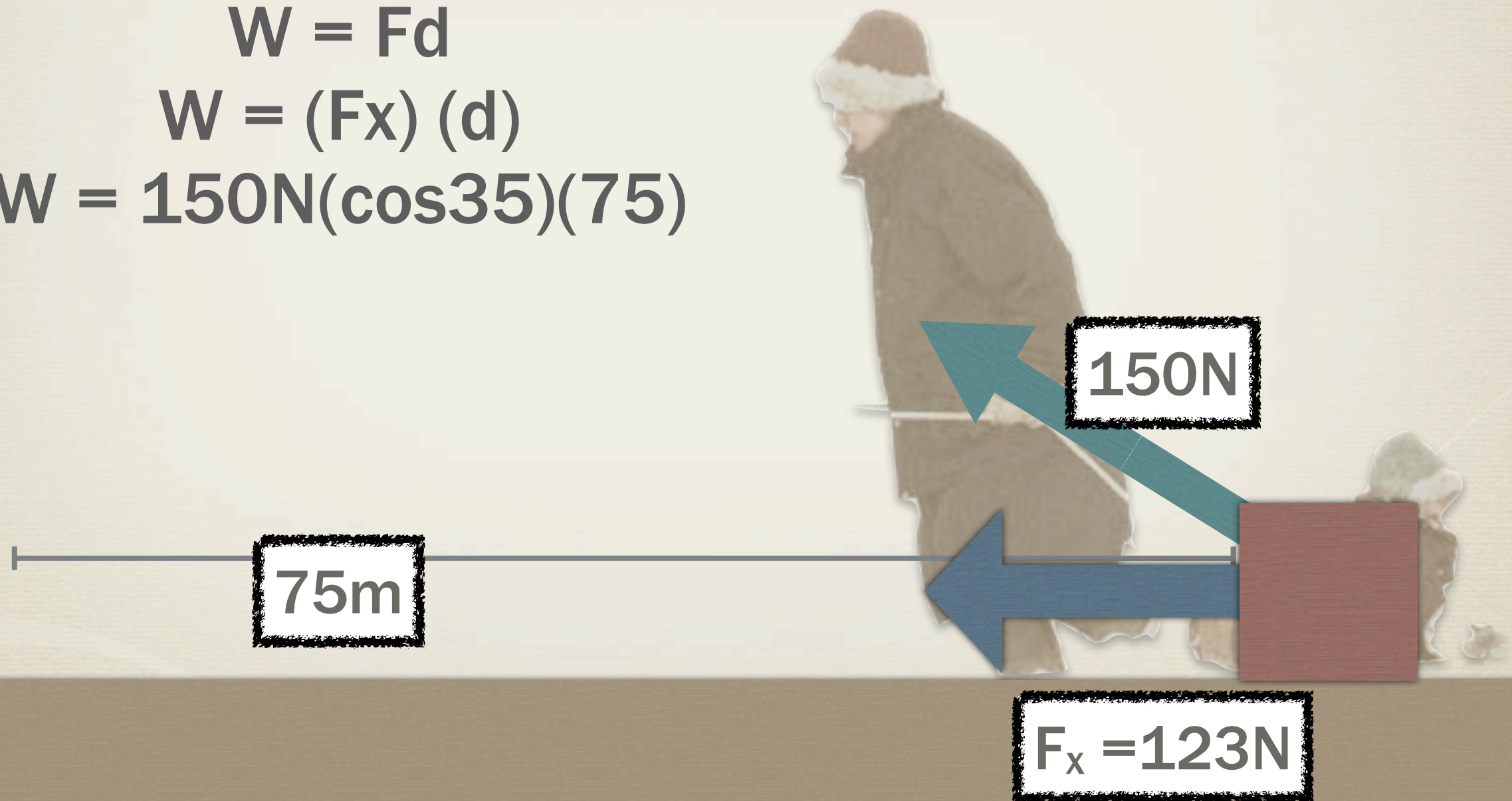
Work and Power

- ▶ A Father uses a force of 150 N to pull a sled with a total weight of 500 N. The Rope makes an angle of 35 degrees with the horizontal. They go a distance of 75 m in 2 minutes

$$W = Fd$$

$$W = (Fx) (d)$$

$$W = 150\text{N}(\cos 35)(75)$$



Work and Power

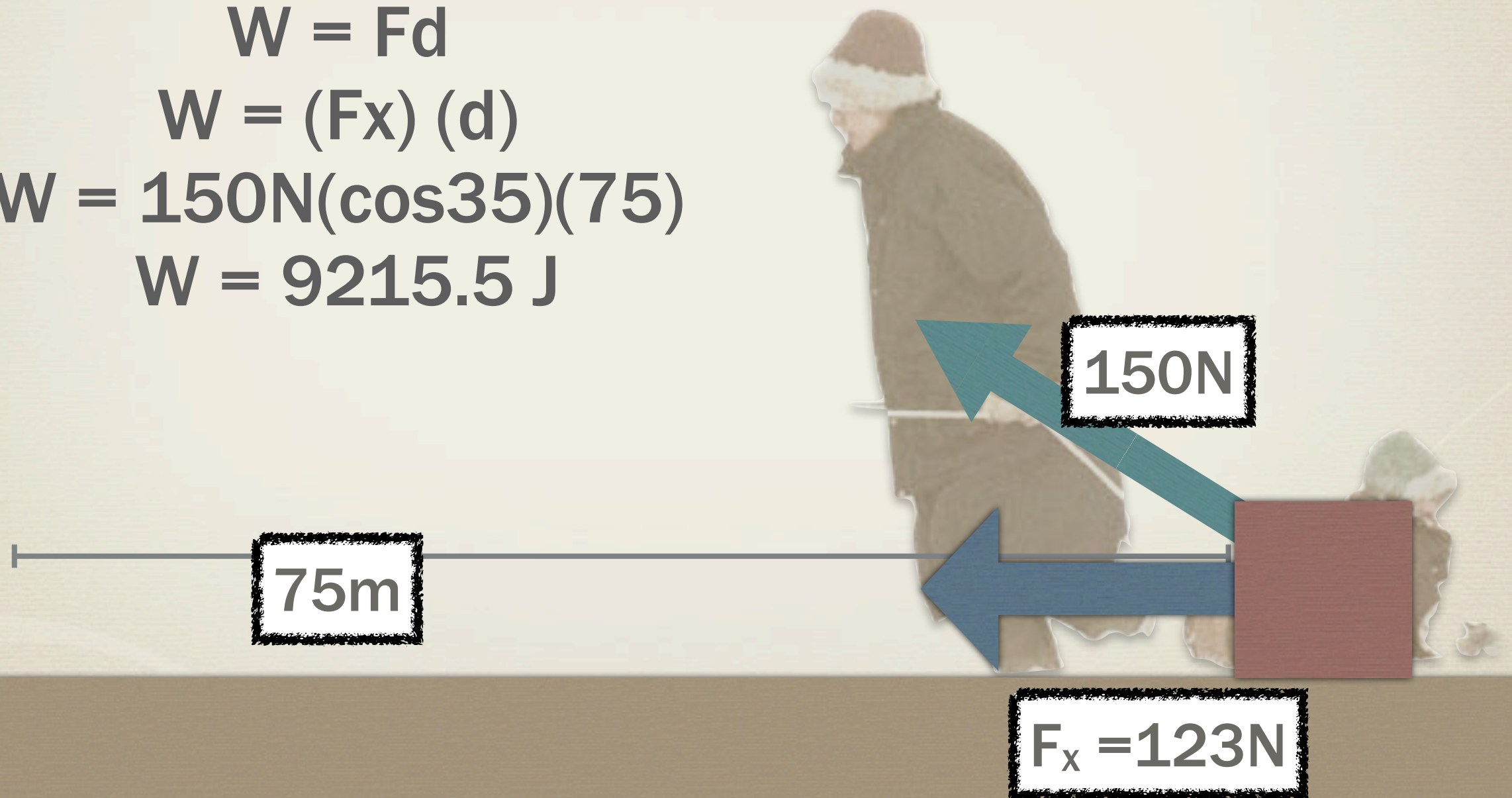
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$$W = 9215.5 \text{ J}$$



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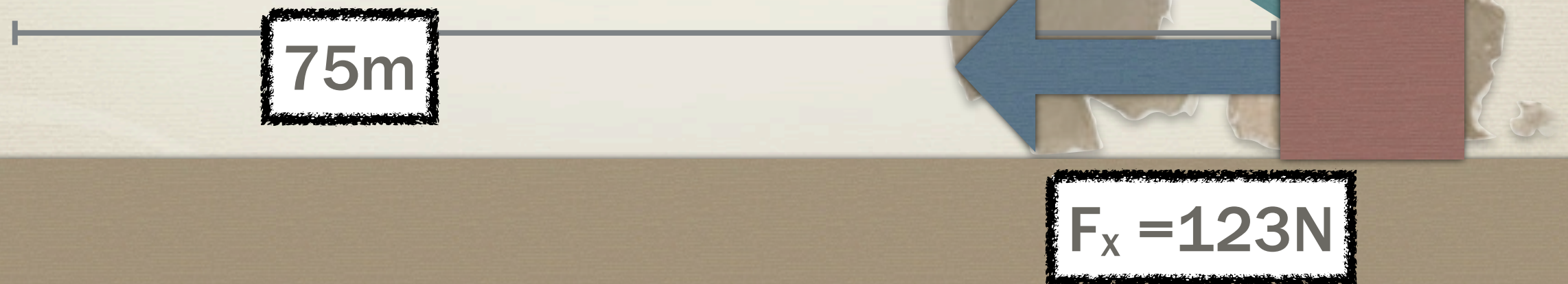
$$W = Fd$$

$$W = (Fx) (d)$$

$$W = 150\text{N}(\cos 35)(75)$$

$$W = 9215.5 \text{ J}$$

note: Only the “x” force was used and 500 N was not important



Work and Power

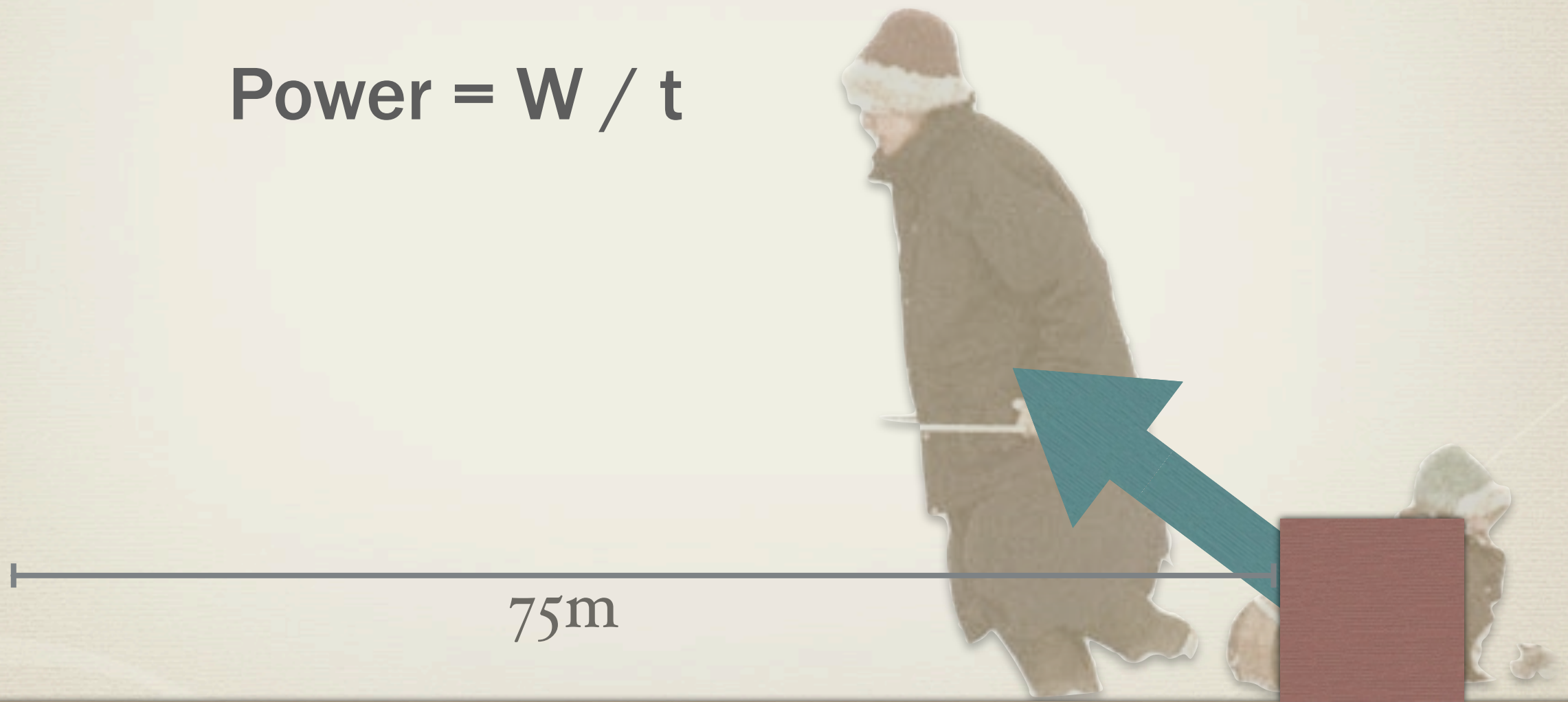
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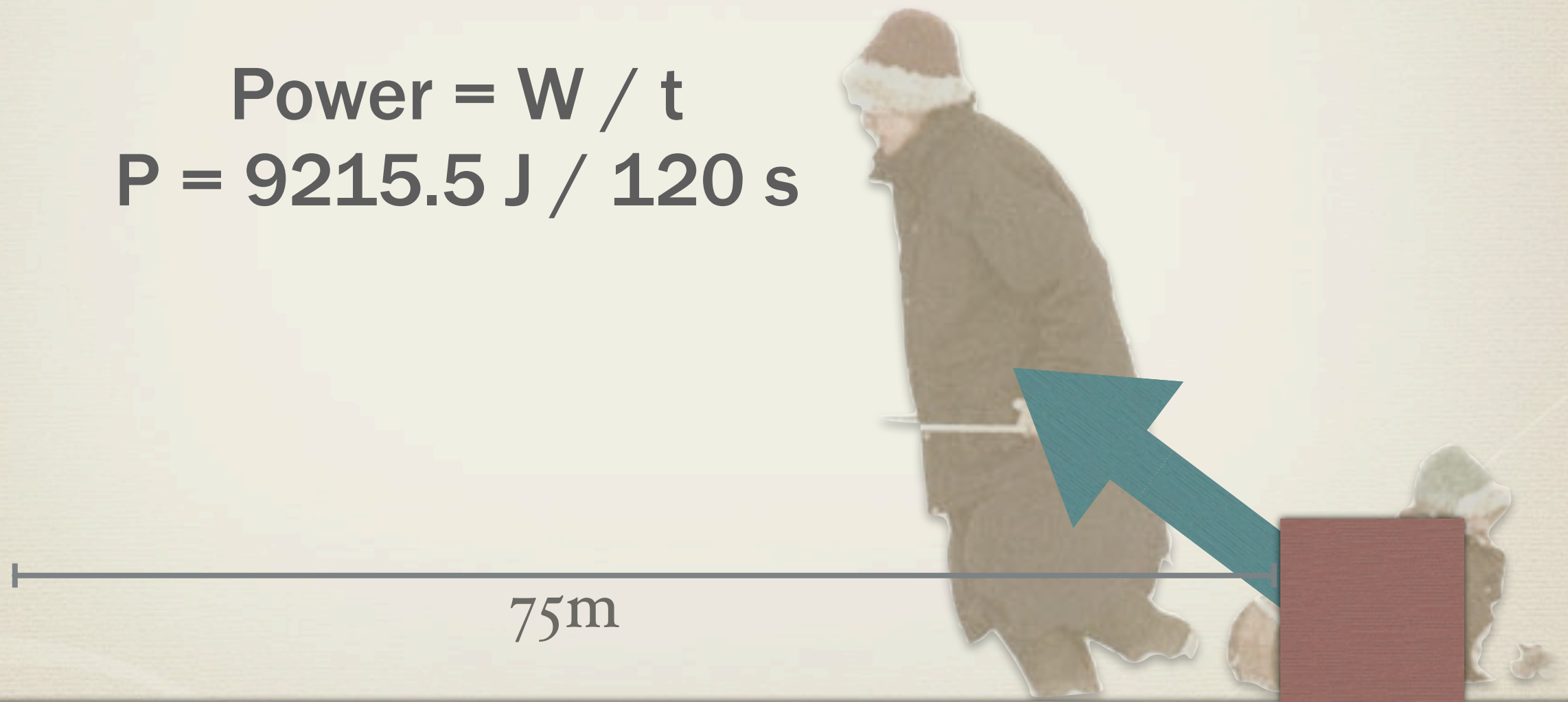
$$\text{Power} = W / t$$



Work and Power

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$$\text{Power} = W / t$$
$$P = 9215.5 \text{ J} / 120 \text{ s}$$



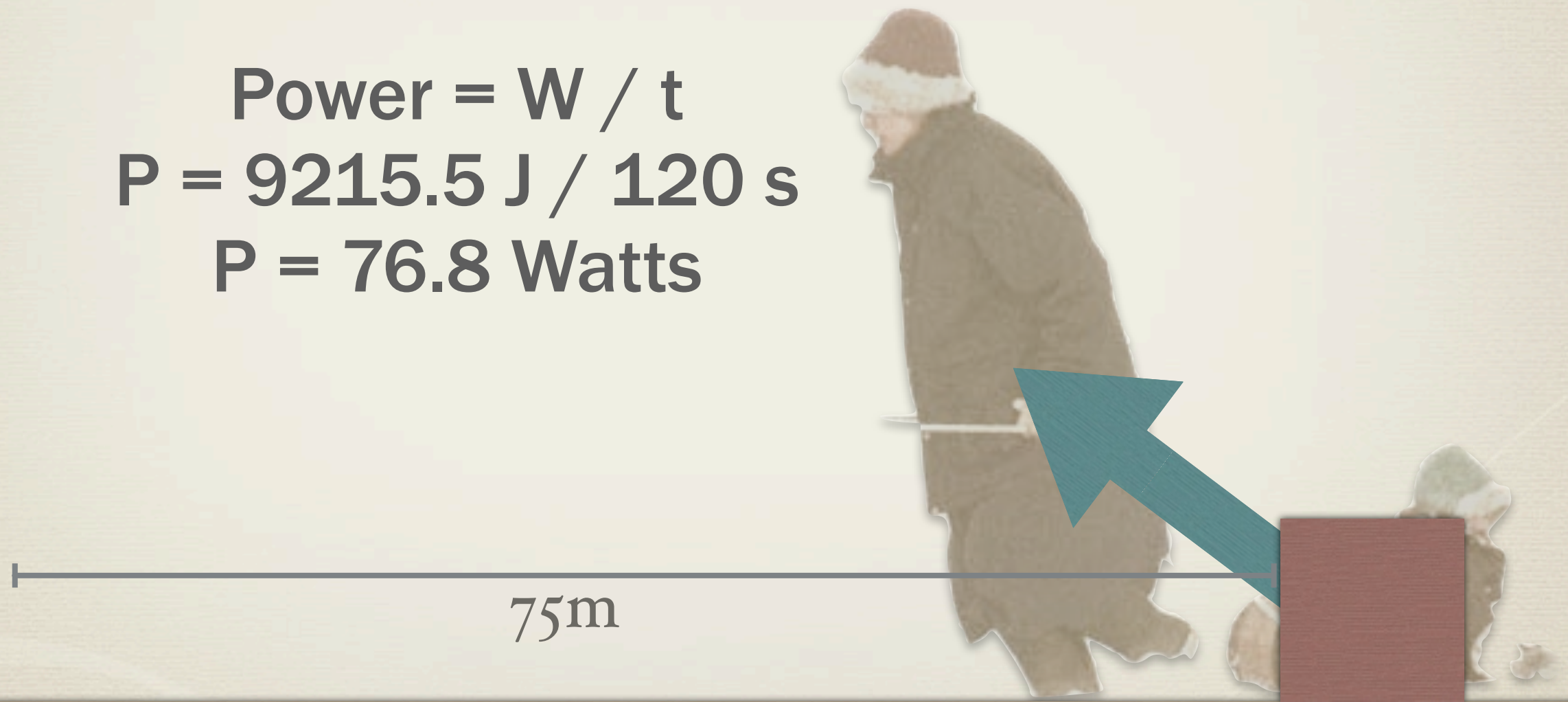
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$$P = 76.8 \text{ Watts}$$



Work and Power

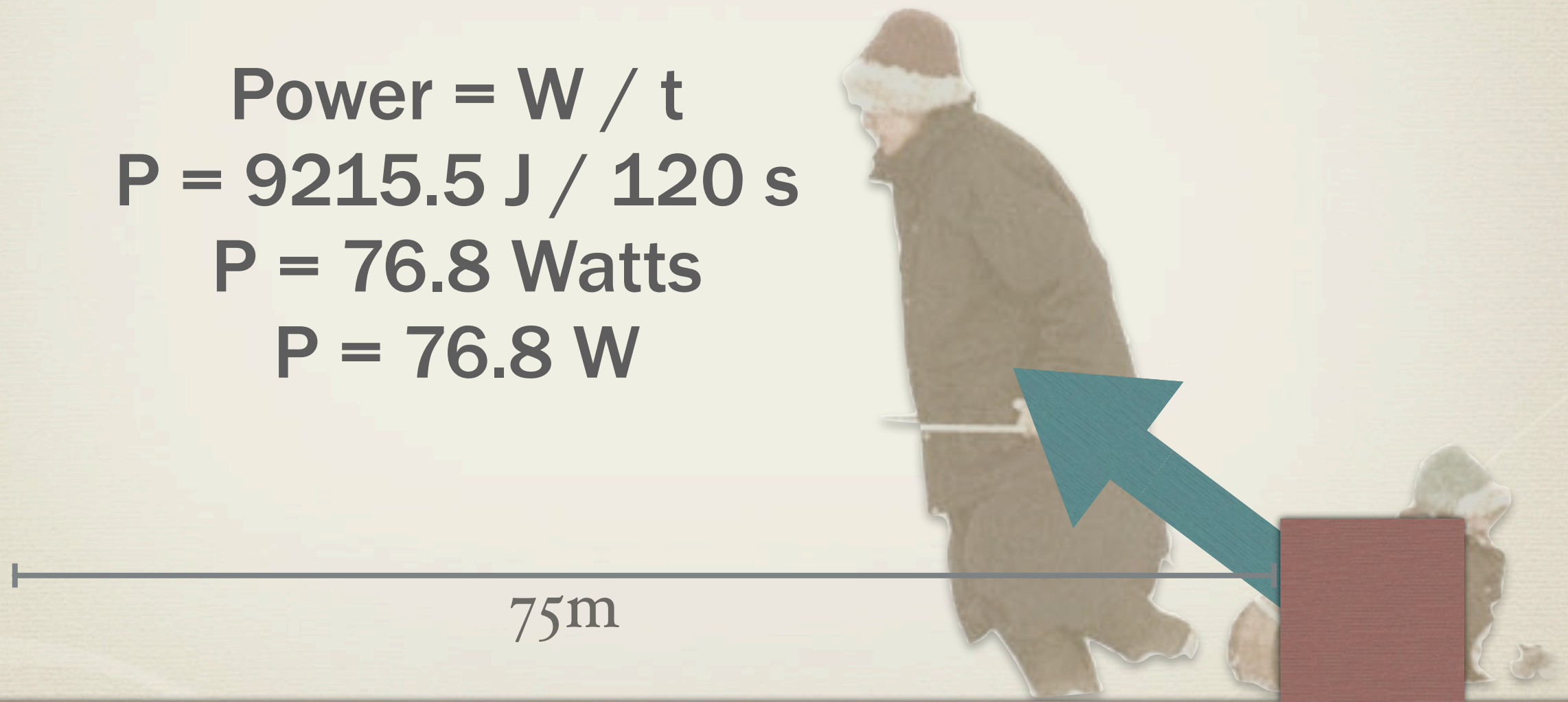
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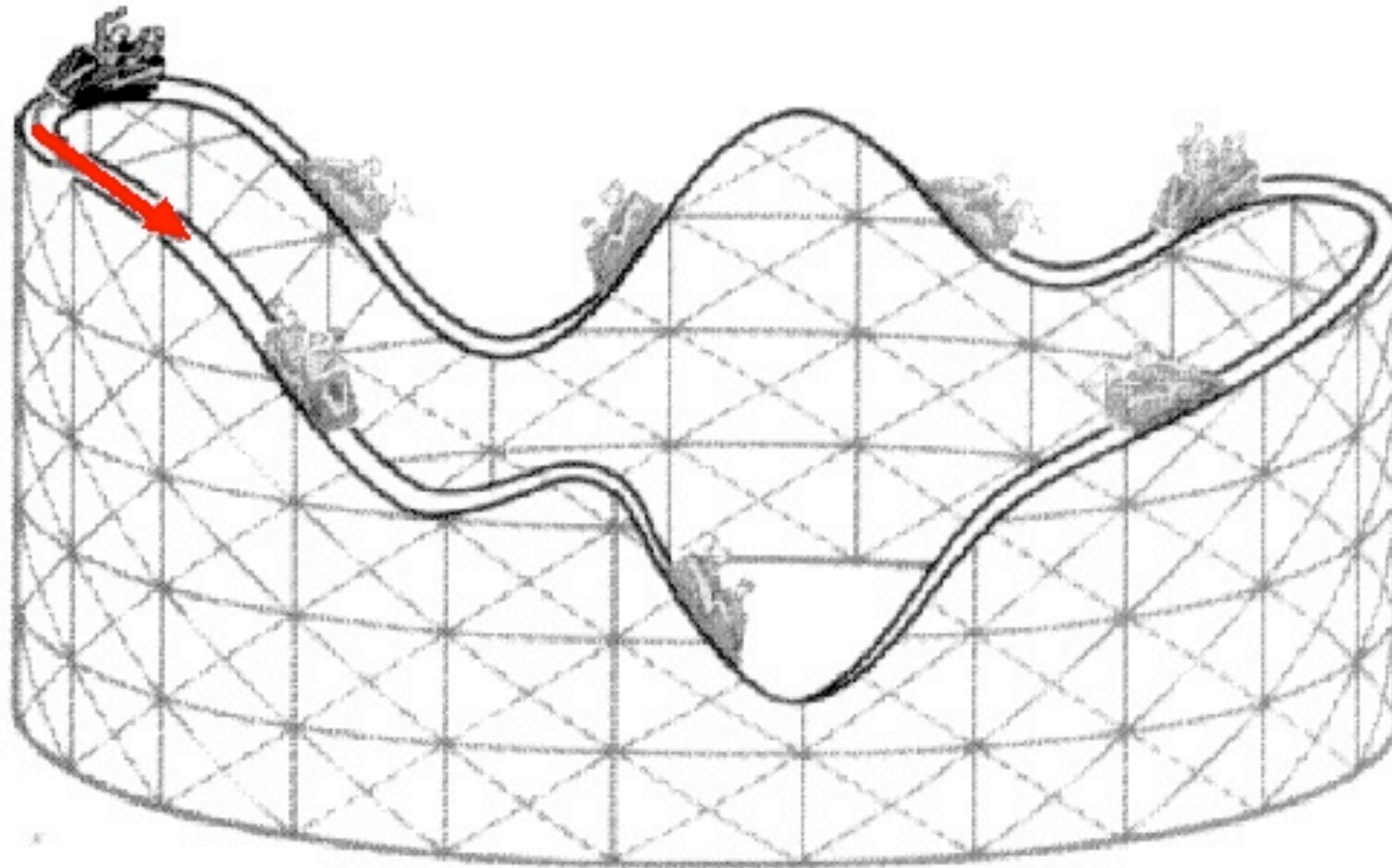
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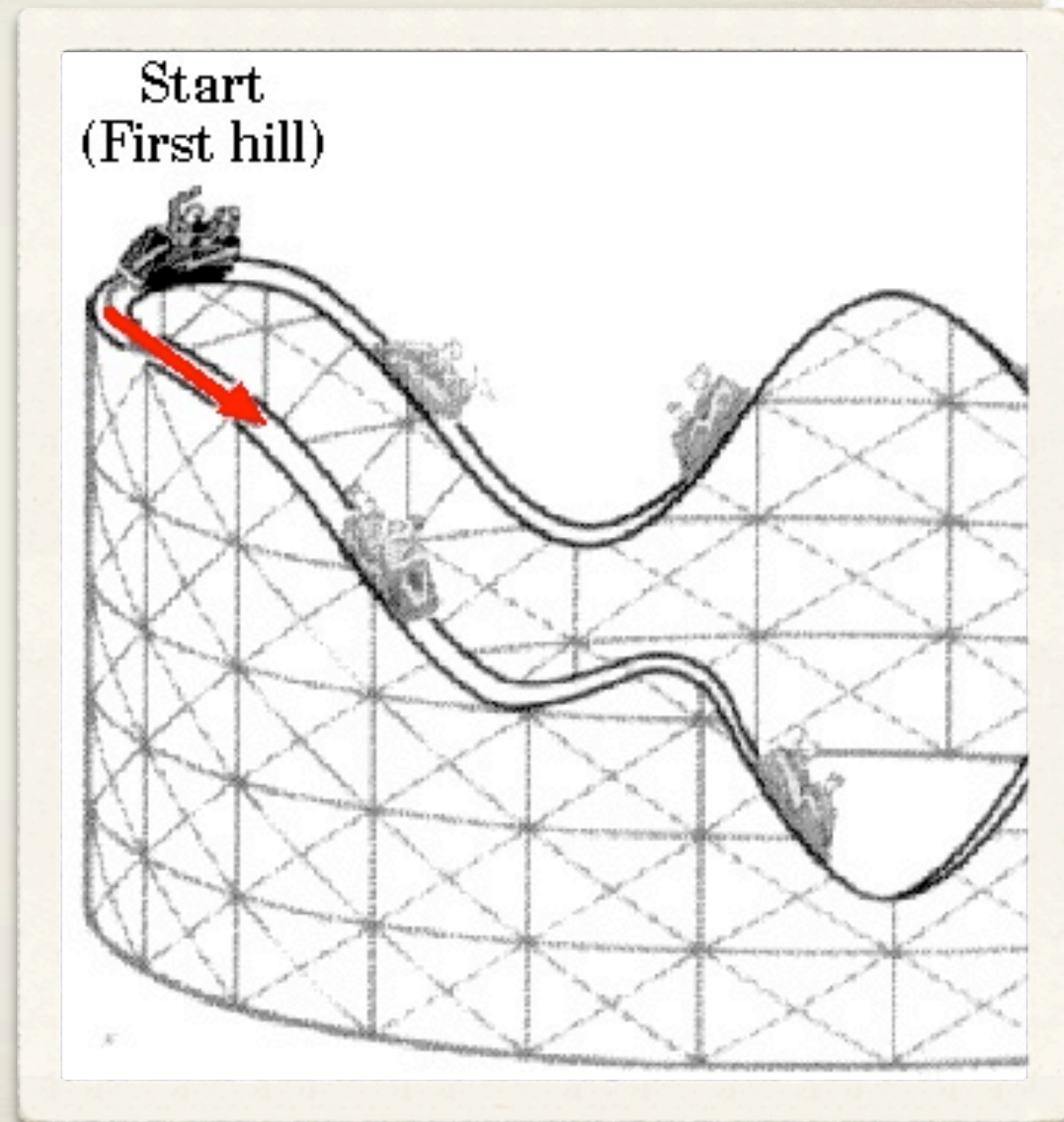
Start
(First hill)



The Roller Coaster

Conservation of Energy Problems

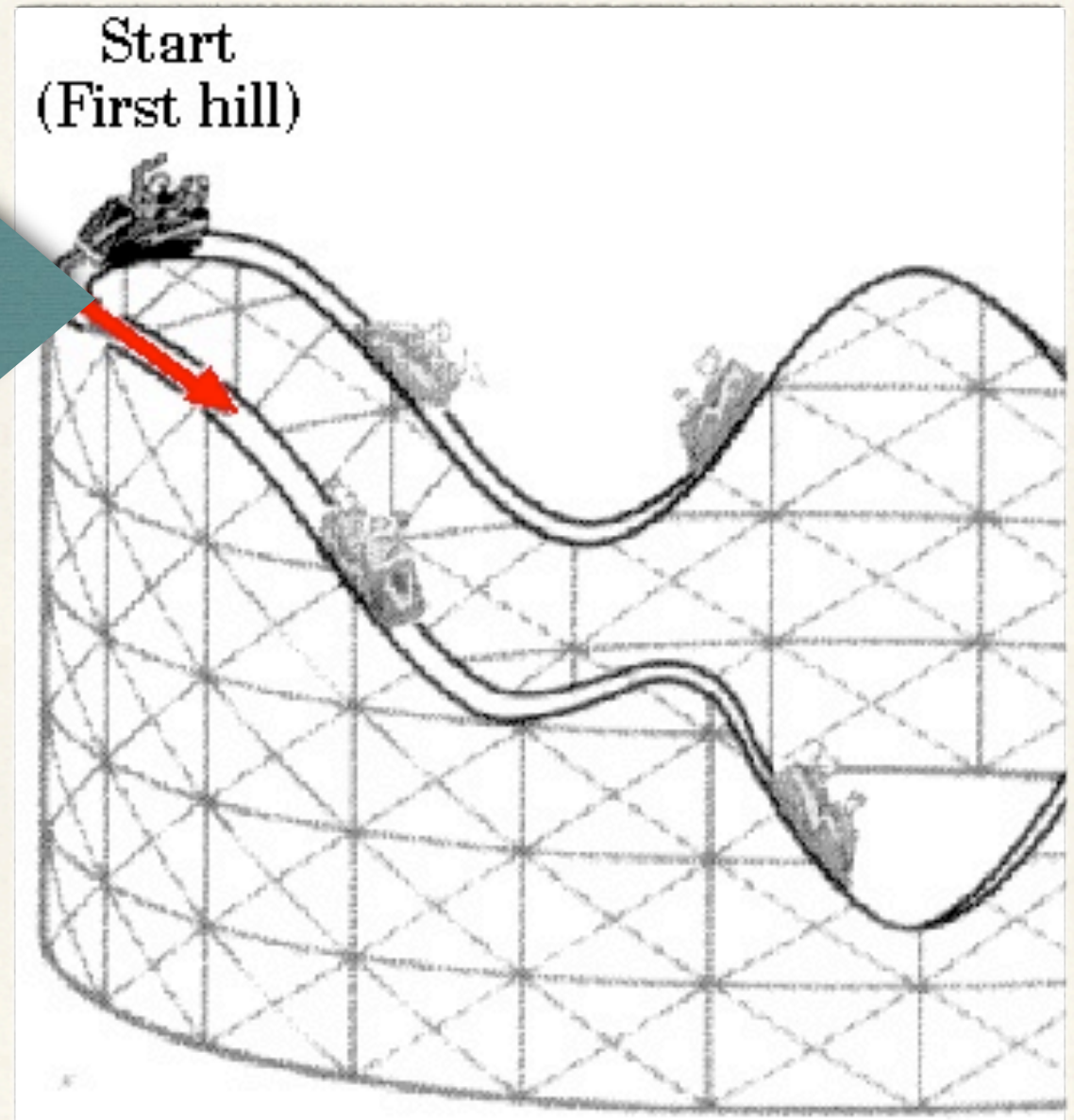
Roller Coaster



Roller Coaster

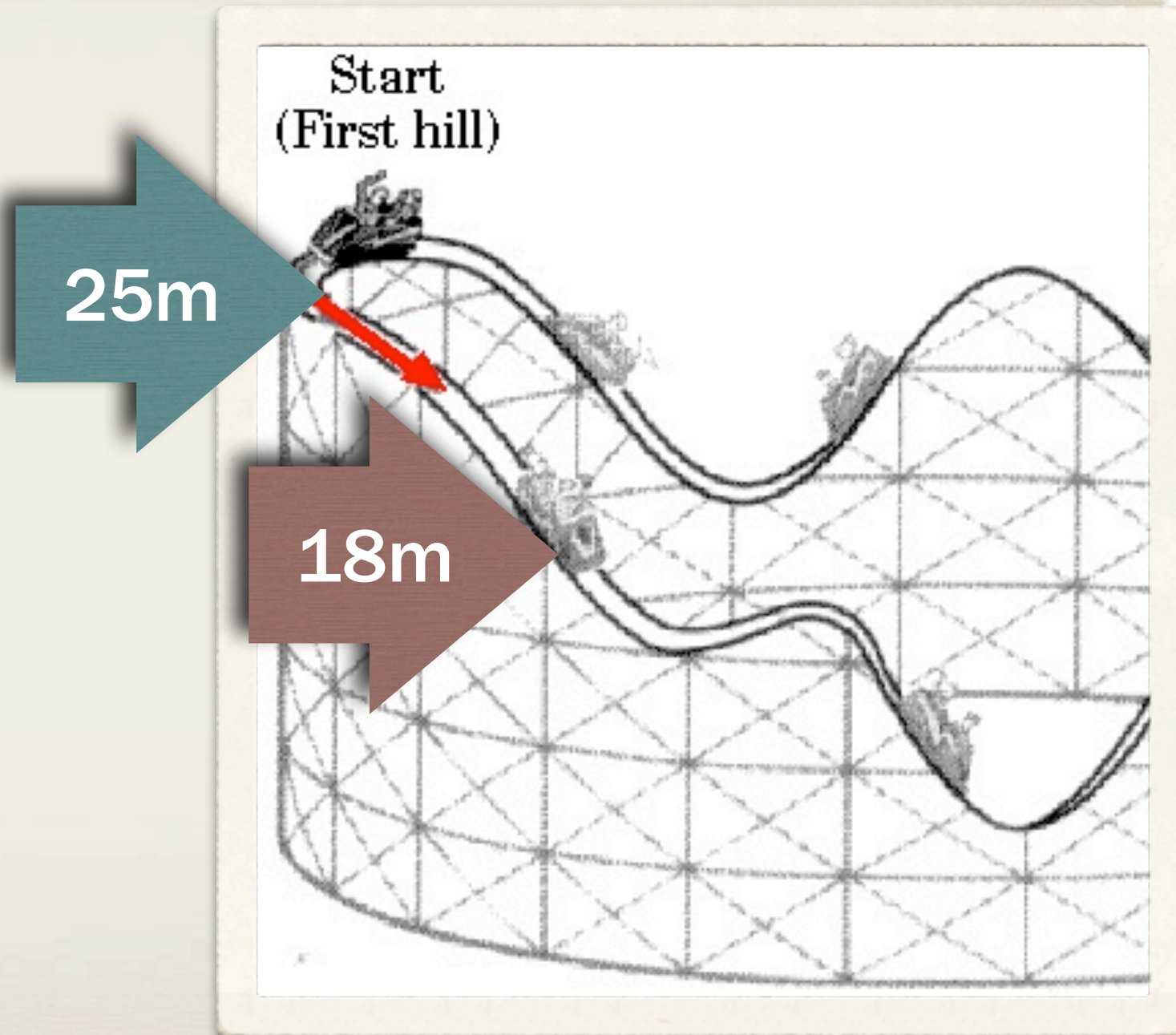
- If the roller coaster car has a total mass of 1000 kg, and starts with almost no velocity at the top...

25m



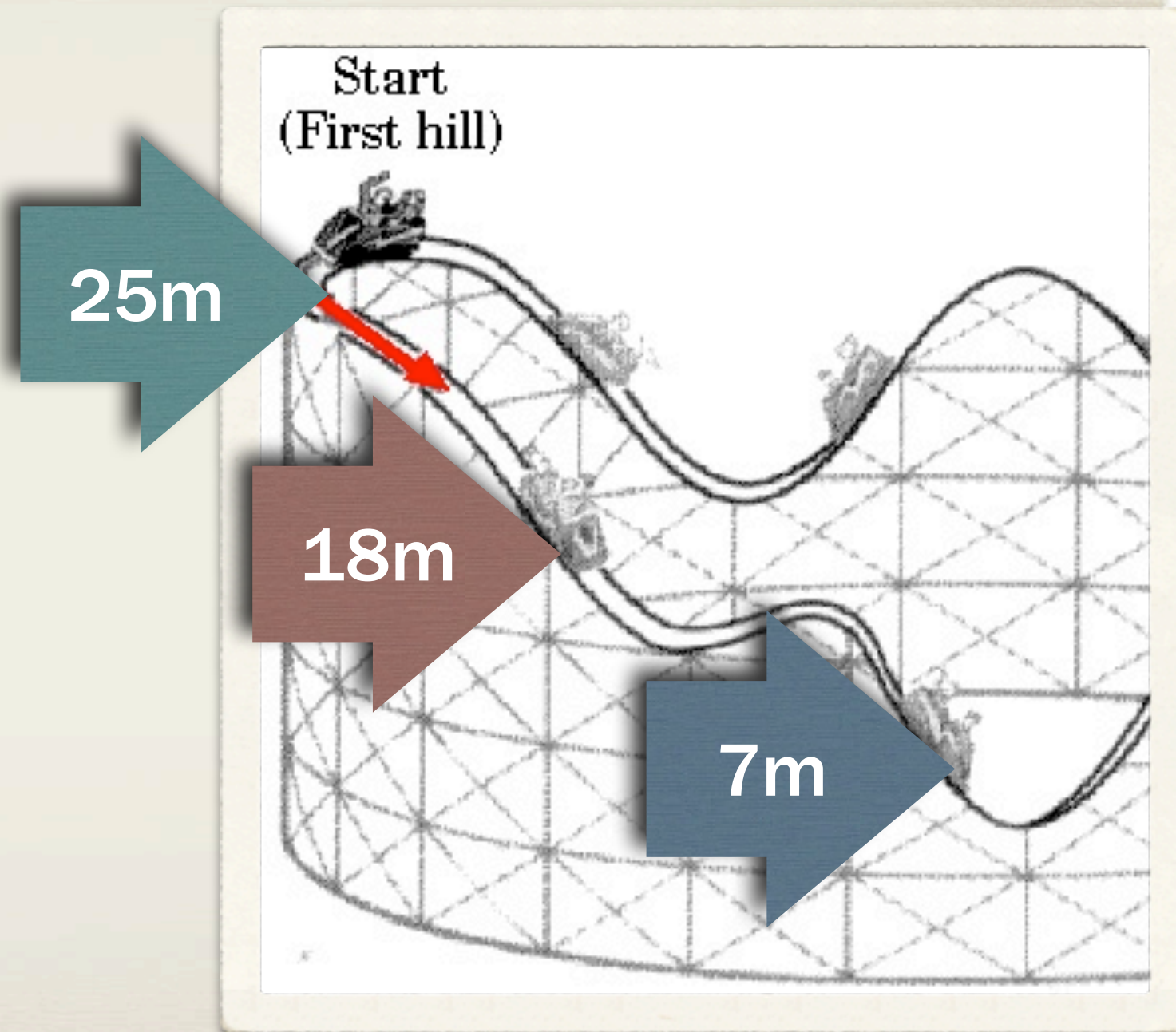
Roller Coaster

- ▶ If the roller coaster car has a total mass of 1000 kg, and starts with almost no velocity at the top...
- ▶ Find the velocity at point B



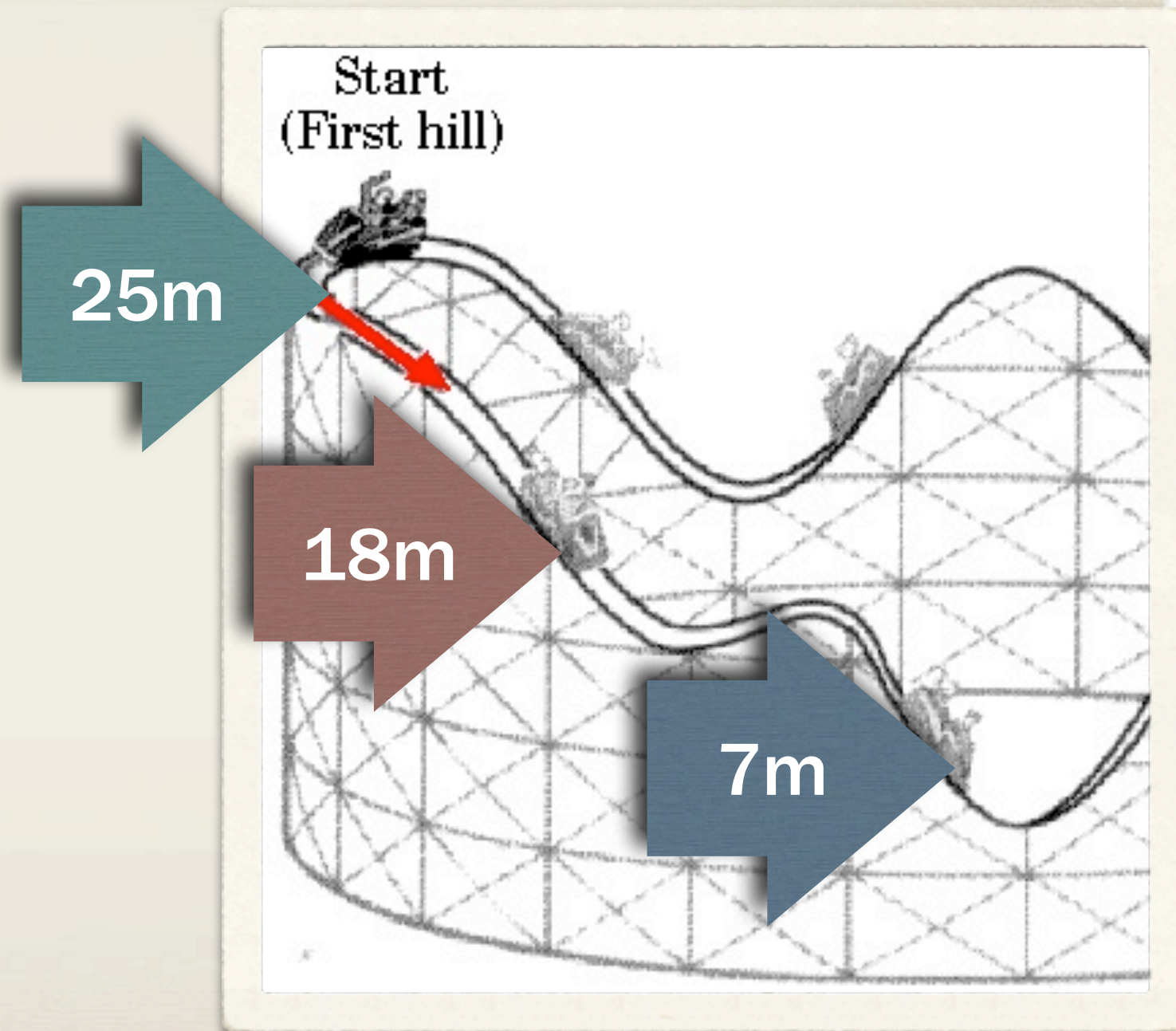
Roller Coaster

- ▶ If the roller coaster car has a total mass of 1000 kg, and starts with almost no velocity at the top...
- ▶ Find the velocity at point B
- ▶ Find the velocity at point C



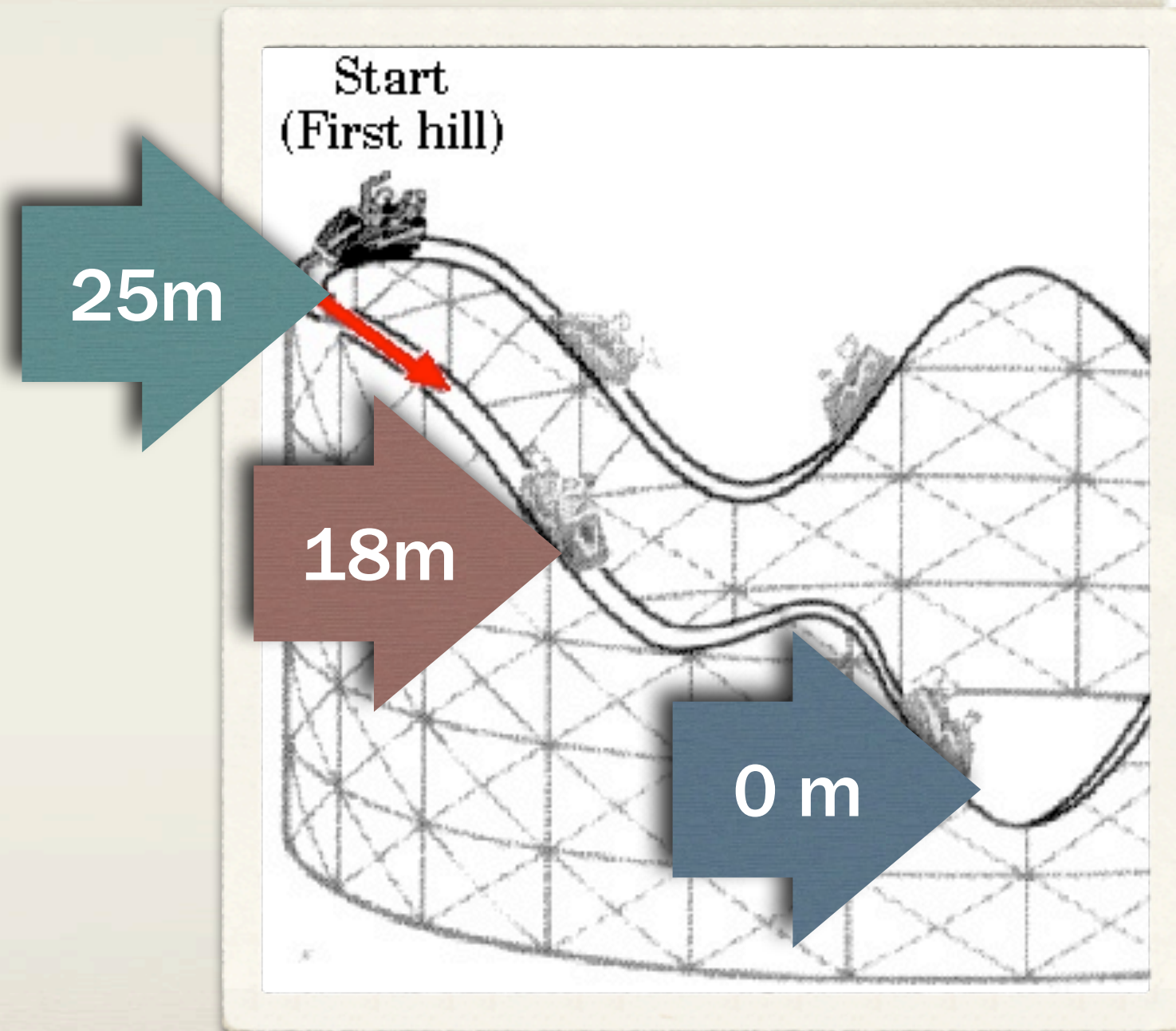
Make it Simple

- ▶ If the roller coaster car has a total mass of 1000 kg, and starts with almost no velocity at the top...
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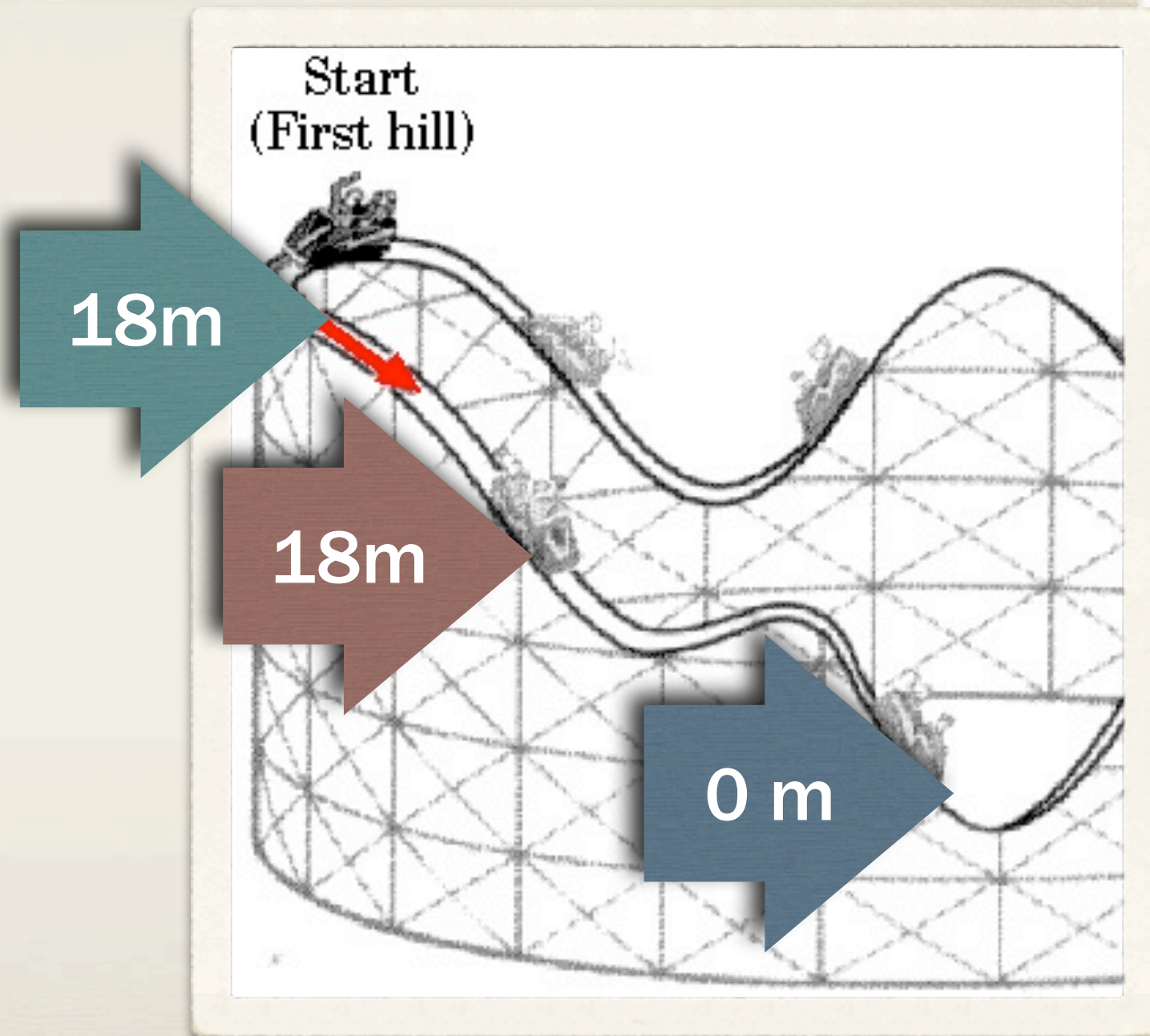
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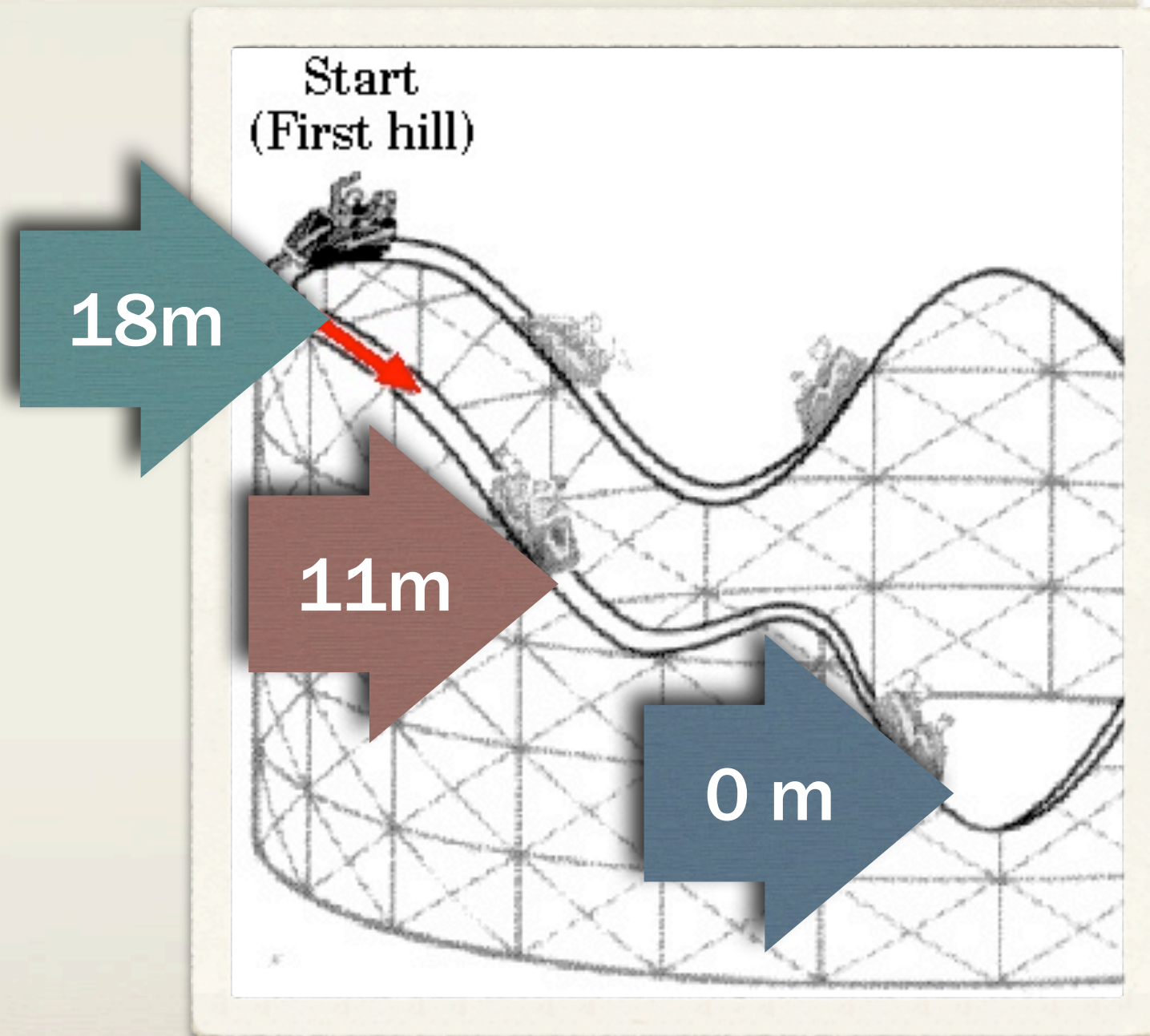
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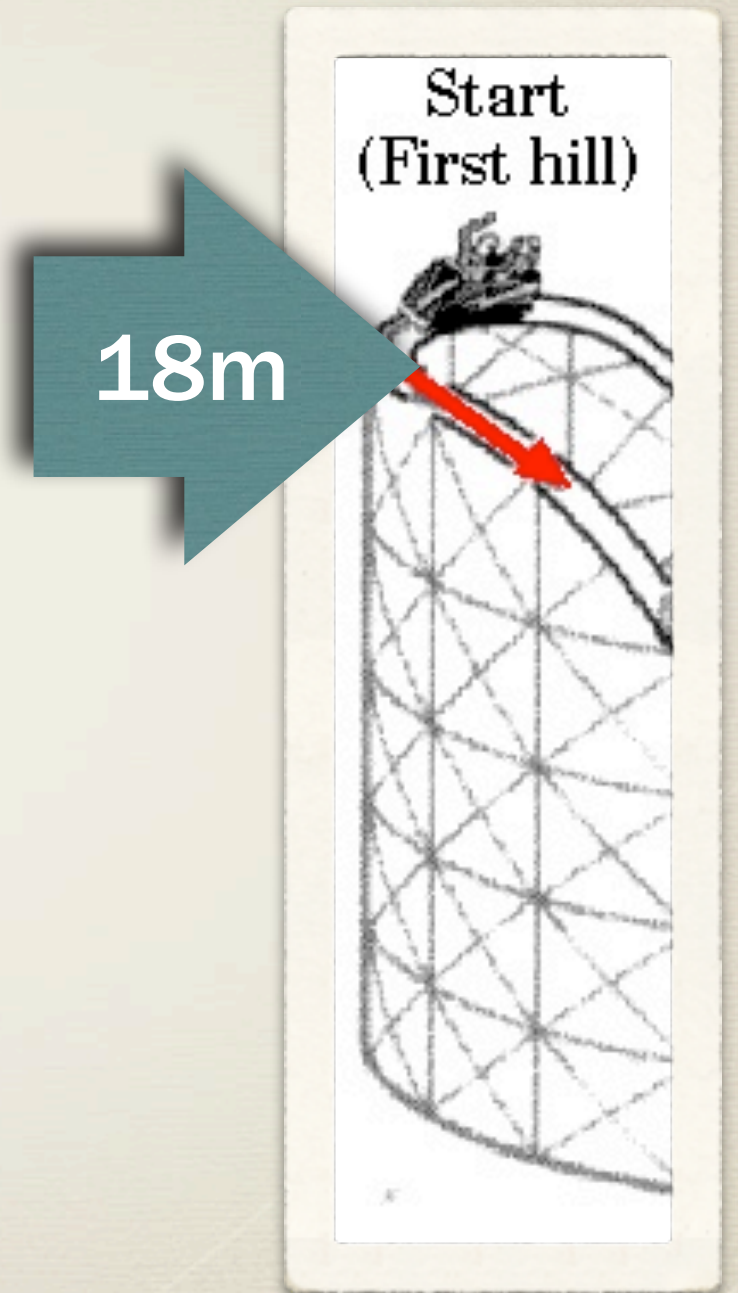


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- ▶ Find the velocity at point C



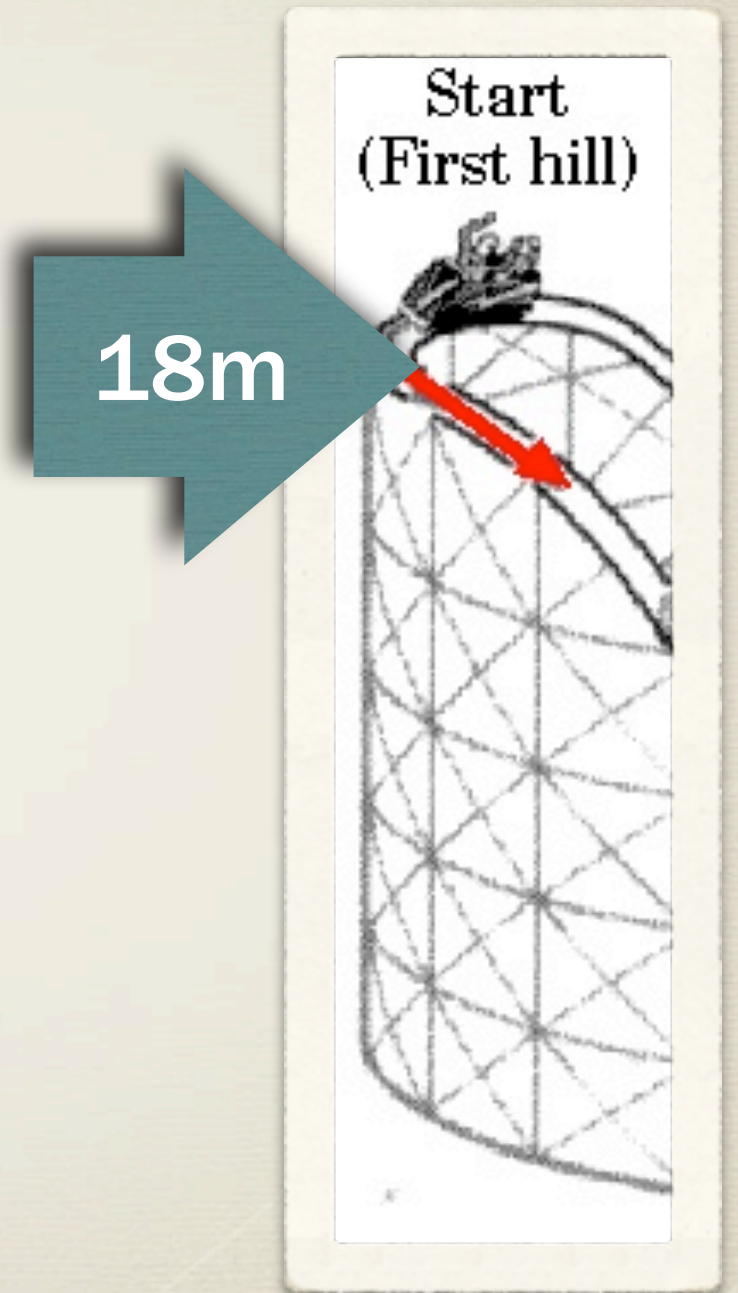
At the top (18m)



At the top (18m)

► Given Info:

- $m = 1000\text{kg}$
- $v = 0\text{ m/s}$
- $h = 18\text{ m}$



At the top (18m)

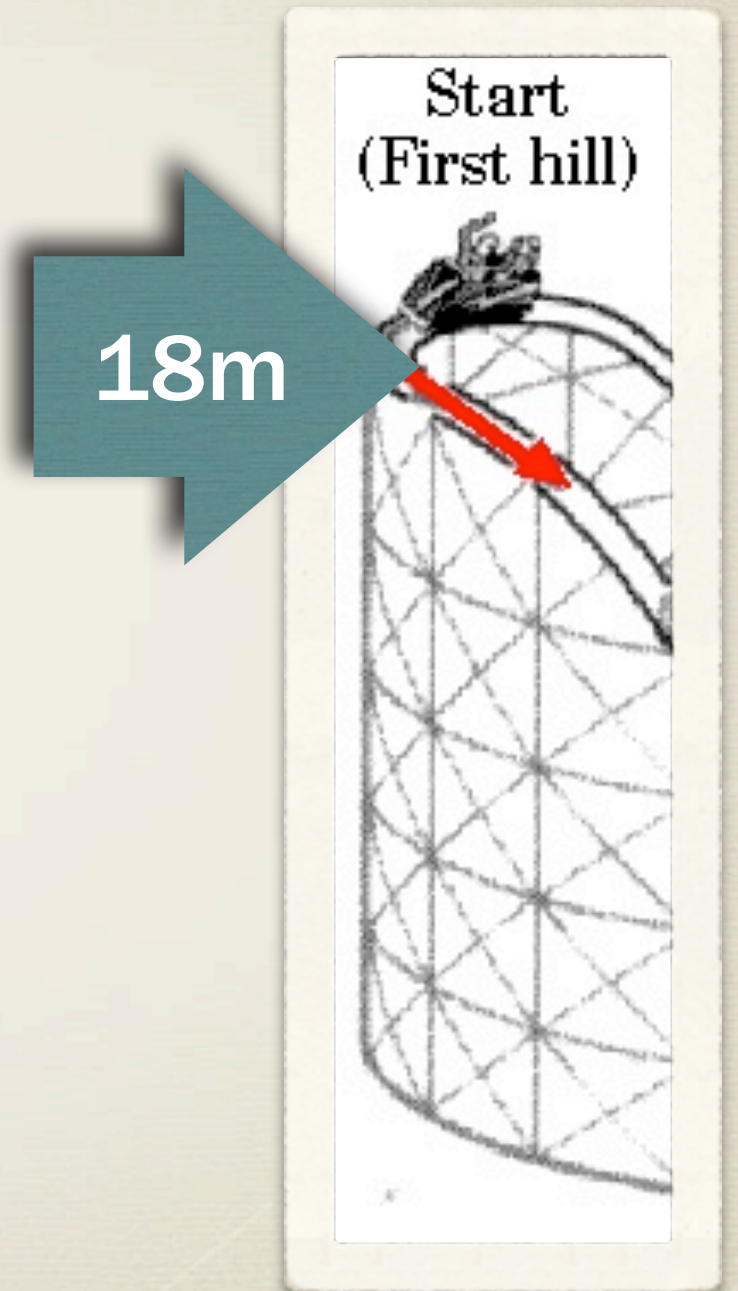
► Given Info:

► $m = 1000\text{kg}$

► $v = 0 \text{ m/s}$

► $h = 18 \text{ m}$

► $PE = mgh$



At the top (18m)

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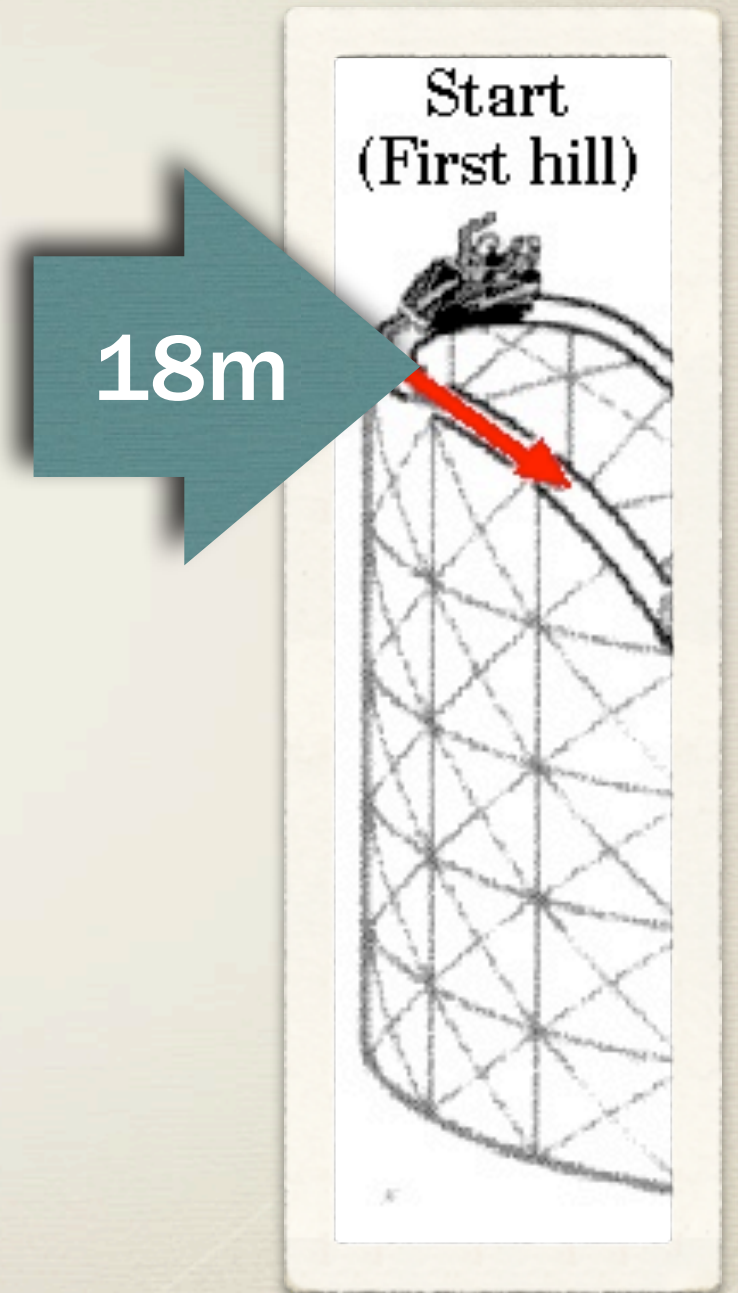
▶ $m = 1000\text{kg}$

▶ $v = 0 \text{ m/s}$

▶ $h = 18 \text{ m}$

▶ $PE = mgh$

▶ $PE = (1000)(9.8)(18)$



At the top (18m)

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▶ $m = 1000\text{kg}$

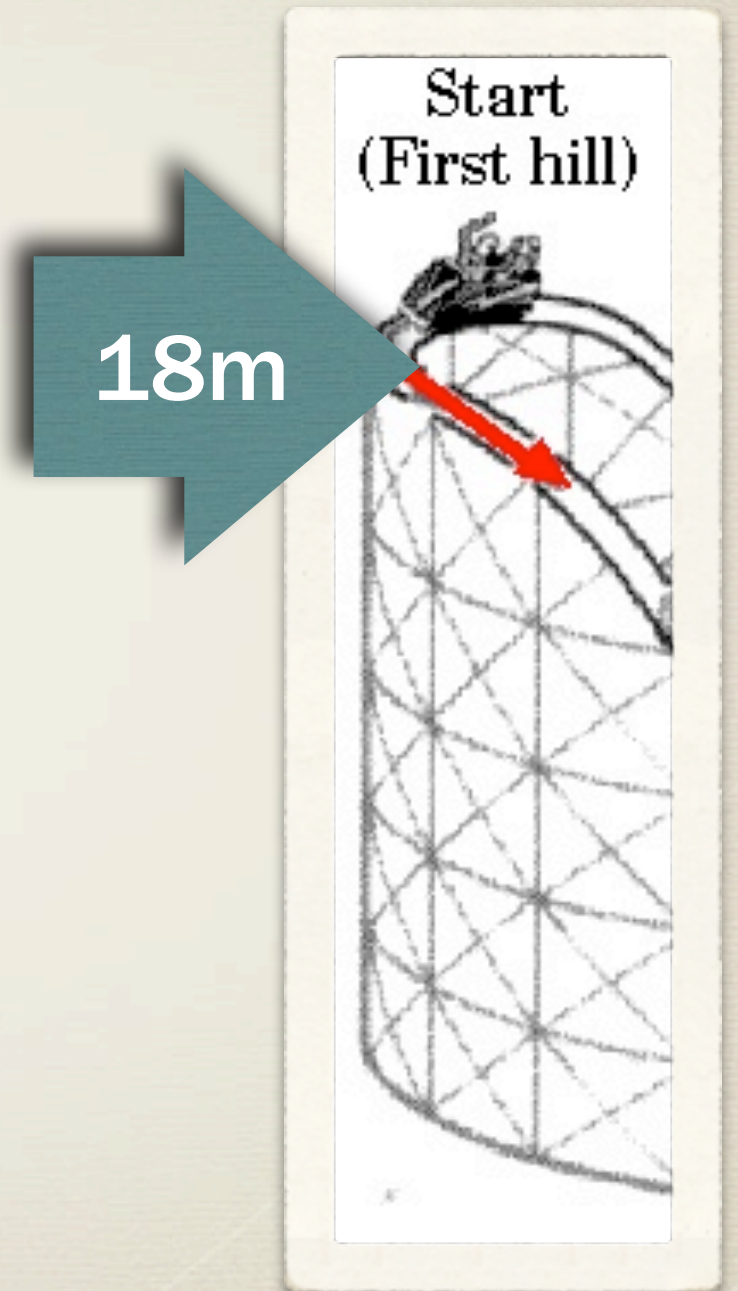
▶ $v = 0 \text{ m/s}$

▶ $h = 18 \text{ m}$

▶ $PE = mgh$

▶ $PE = (1000)(9.8)(18)$

▶ $PE = 176,400\text{J}$



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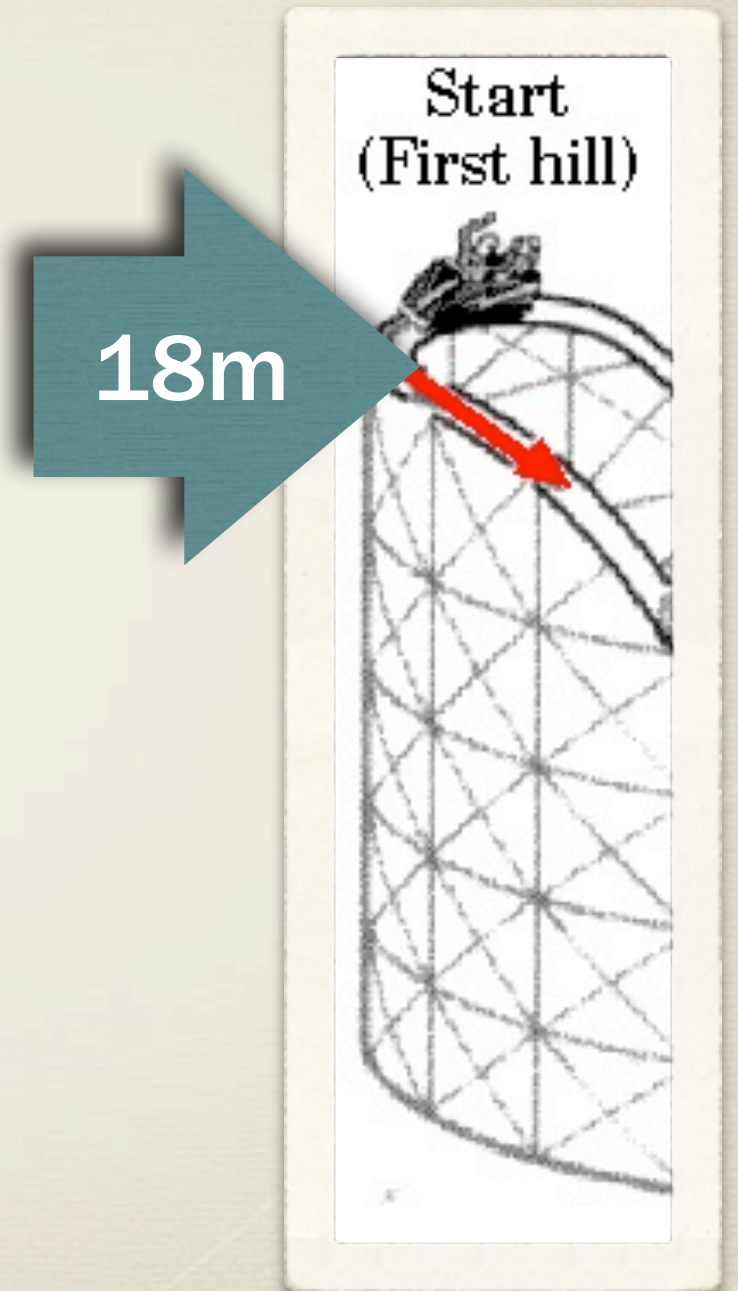
► $h = 18\text{ m}$

► $PE = mgh$

► $PE = (1000)(9.8)(18)$

► $PE = 176,400\text{J}$

► $PE = 176.4\text{ kJ}$



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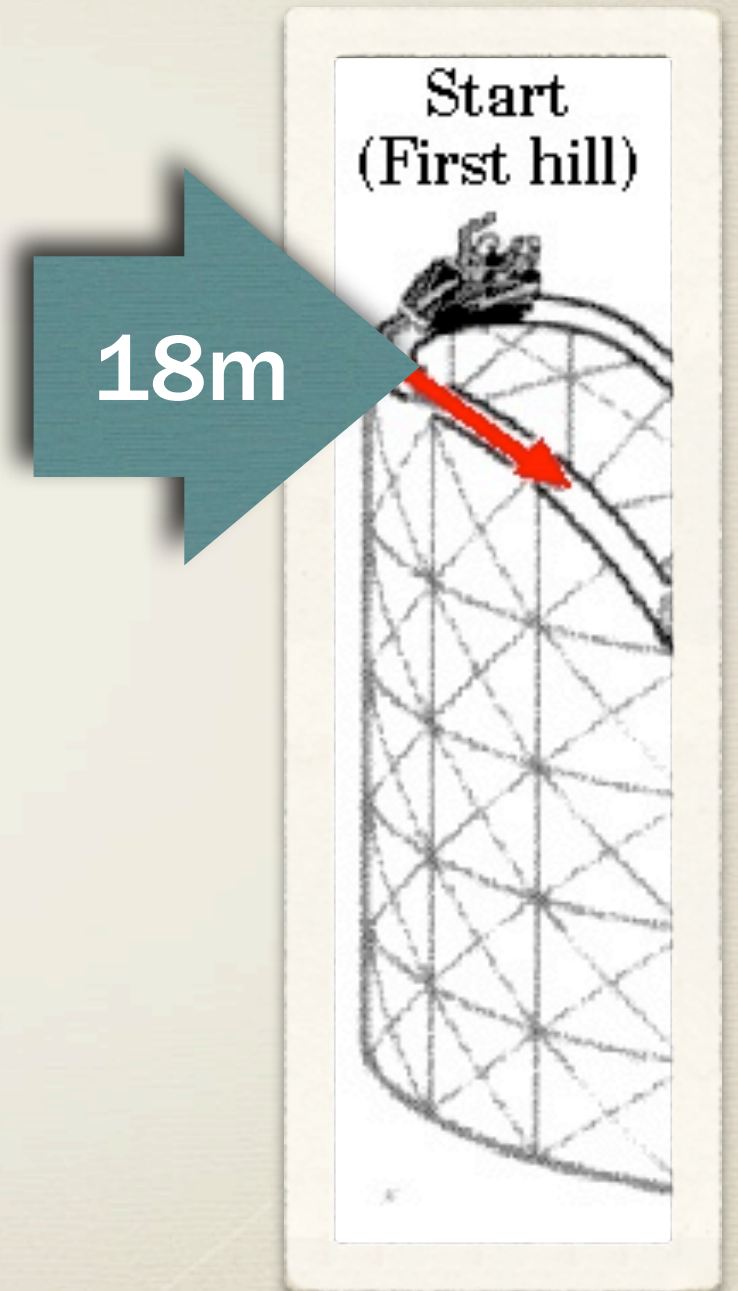
▶ $PE = mgh$

▶ $PE = (1000)(9.8)(18)$

▶ $PE = 176,400\text{J}$

▶ $PE = 176.4 \text{ kJ}$

▶ $KE = \frac{1}{2}(mv^2) = 0 \text{ J}$



At the top (18m)

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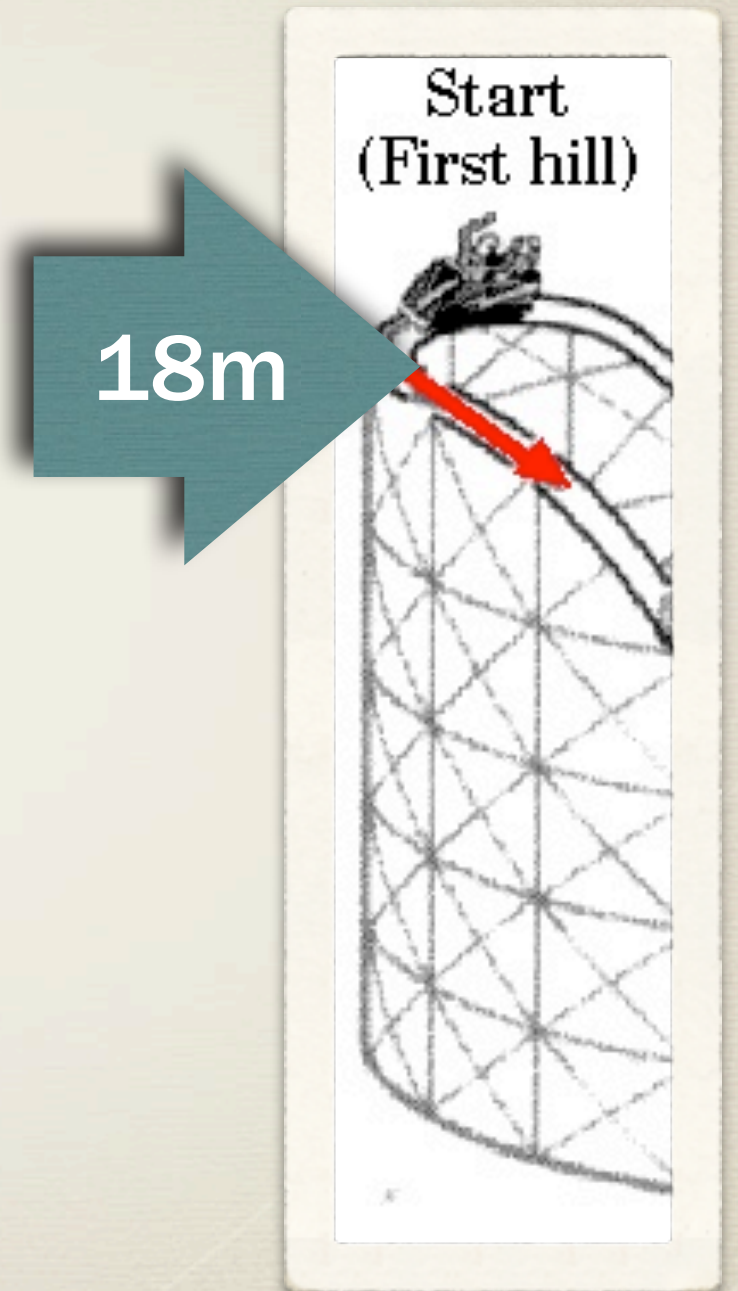
▶ $PE = (1000)(9.8)(18)$

▶ $PE = 176,400\text{J}$

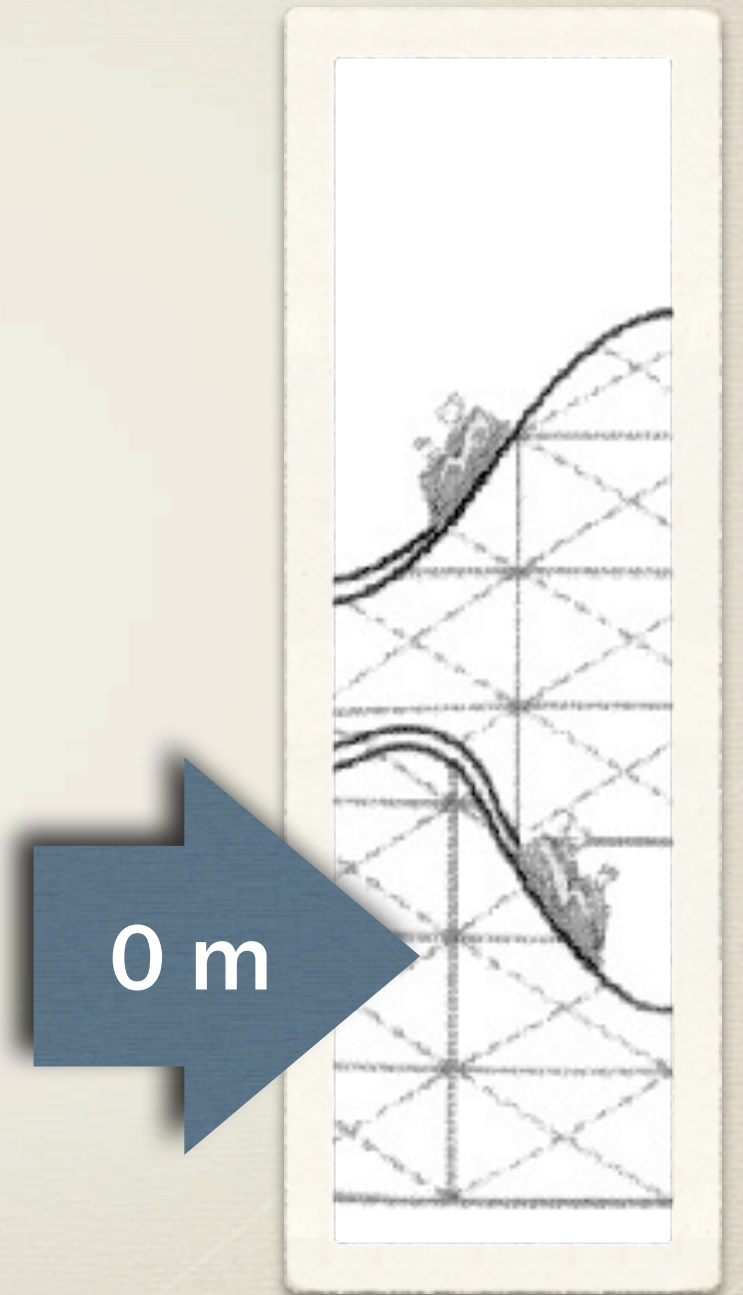
▶ $PE = 176.4 \text{ kJ}$

▶ $KE = \frac{1}{2}(mv^2) = 0 \text{ J}$

▶ $TE = 176.4 \text{ kJ}$



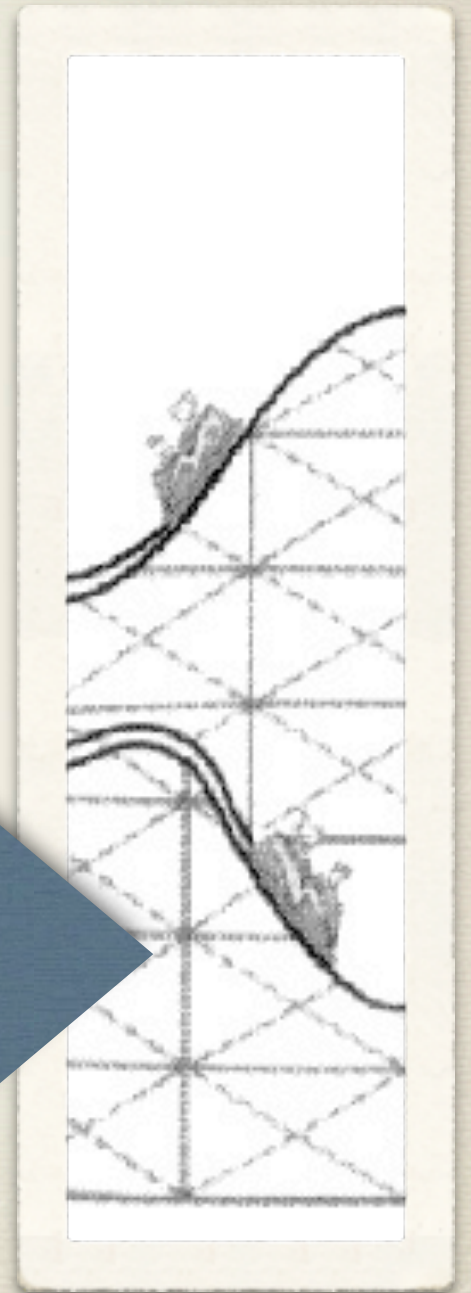
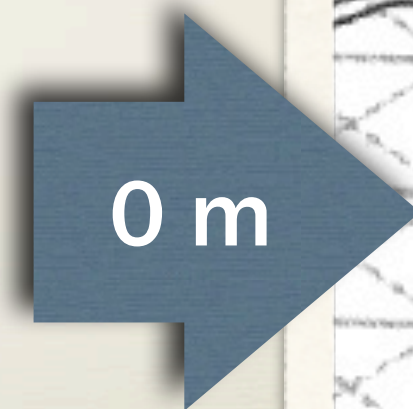
At the bottom (0 m)



At the bottom (0 m)

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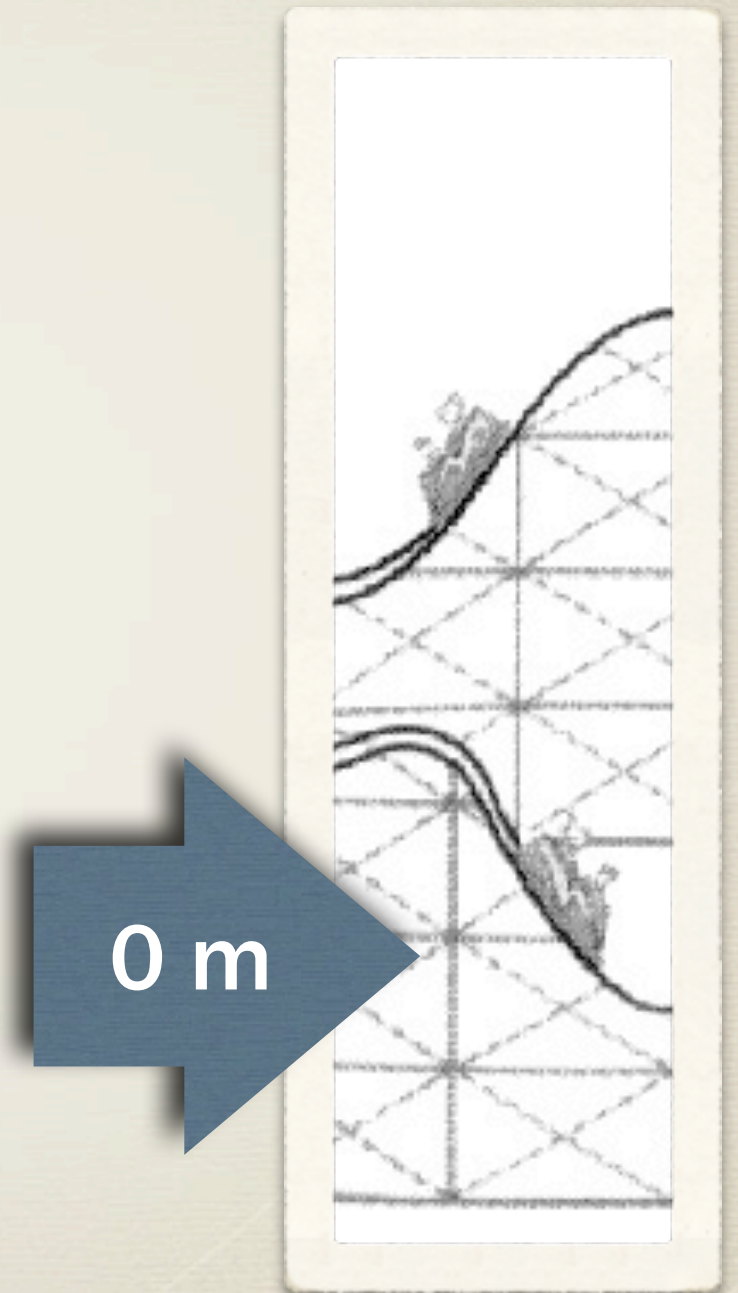
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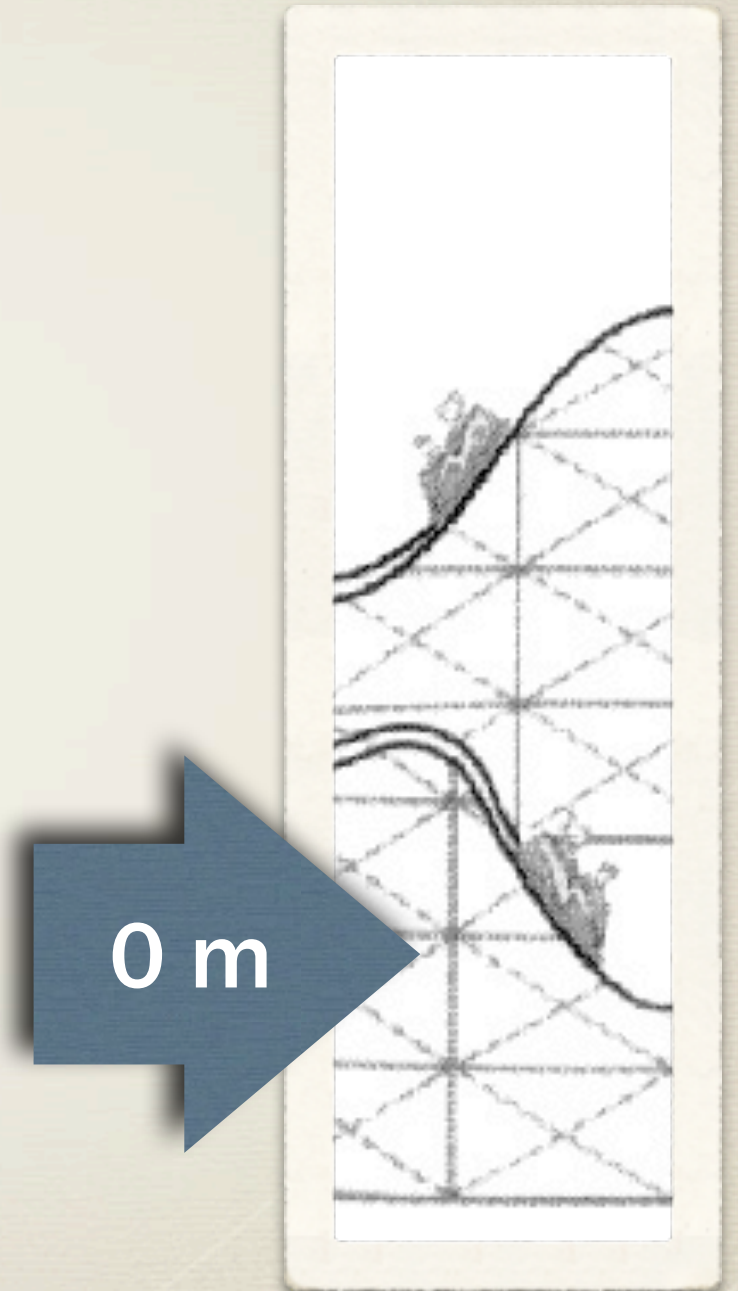
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- $PE = mgh = 0 \text{ J}$



At the bottom (0 m)

▶ Given Info:

- ▶ $m = 1000 \text{ kg}$
- ▶ $h = 0 \text{ m}$
- ▶ $TE = 176.4 \text{ kJ}$
- ▶ $PE = mgh = 0 \text{ J}$
- ▶ $KE = 176,400 \text{ J}$



At the bottom (0 m)

▶ Given Info:

▶ $m = 1000 \text{ kg}$

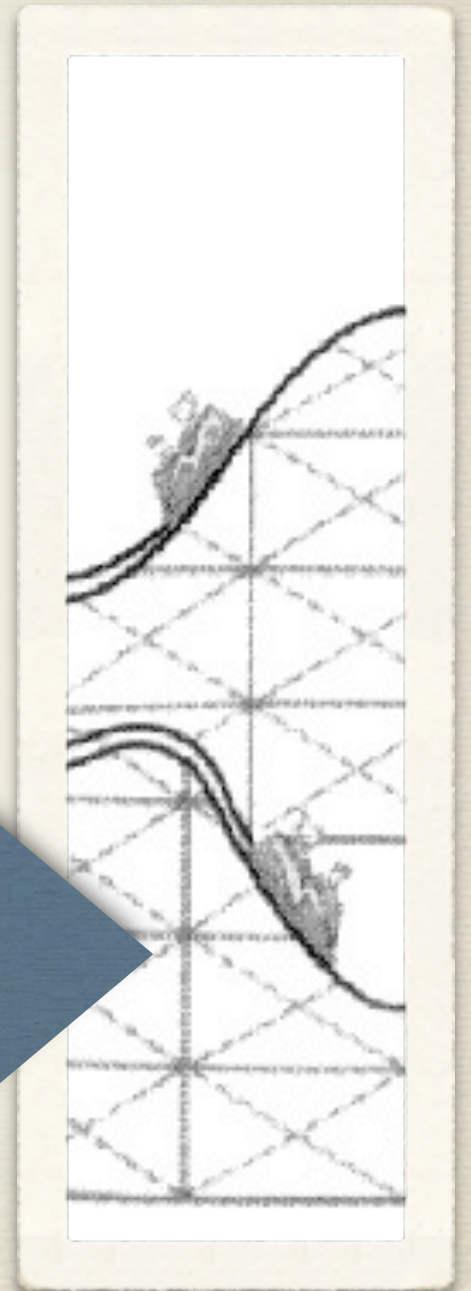
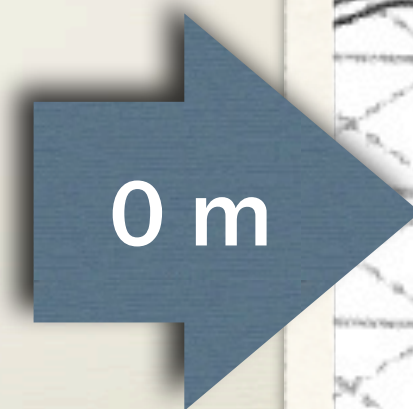
▶ $h = 0 \text{ m}$

▶ $TE = 176.4 \text{ kJ}$

▶ $PE = mgh = 0 \text{ J}$

▶ $KE = 176,400 \text{ J}$

▶ $176,400 \text{ J} = \frac{1}{2}(1000)v^2$



At the bottom (0 m)

► Given Info:

► $m = 1000 \text{ kg}$

► $h = 0 \text{ m}$

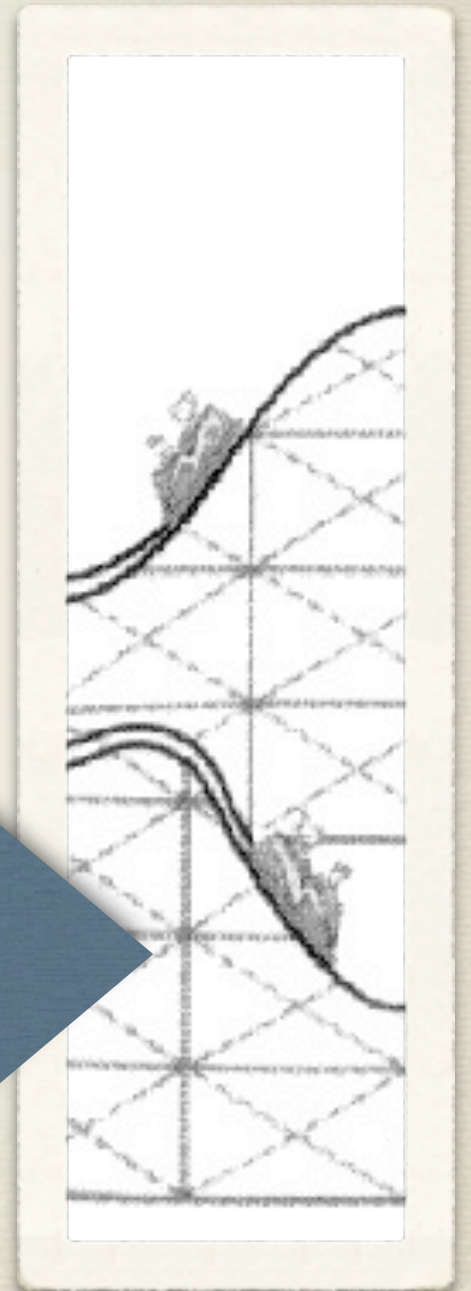
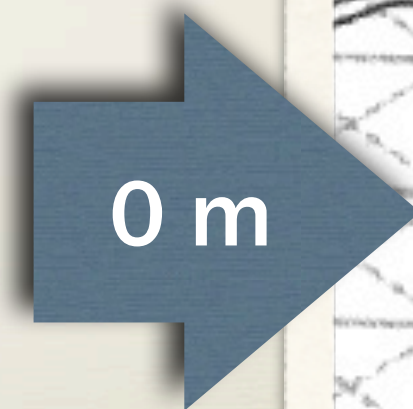
► $TE = 176.4 \text{ kJ}$

► $PE = mgh = 0 \text{ J}$

► $KE = 176,400 \text{ J}$

► $176,400 \text{ J} = \frac{1}{2}(1000)v^2$

► $v^2 = 352.8$



At the bottom (0 m)

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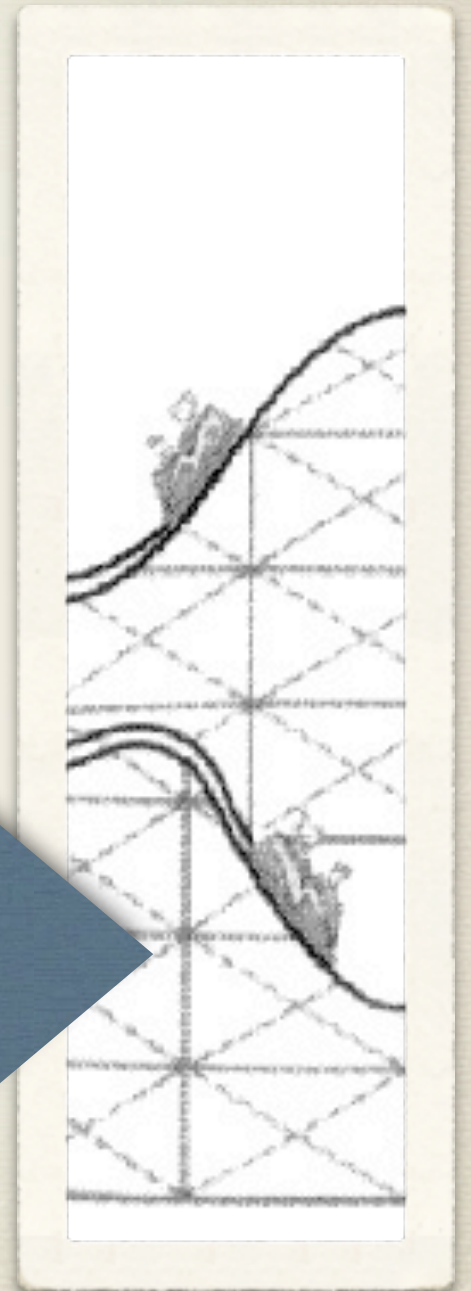
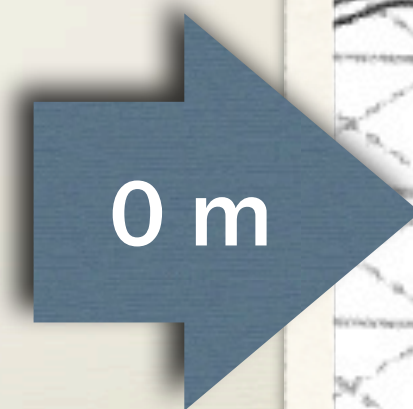
► $PE = mgh = 0 \text{ J}$

► $KE = 176,400 \text{ J}$

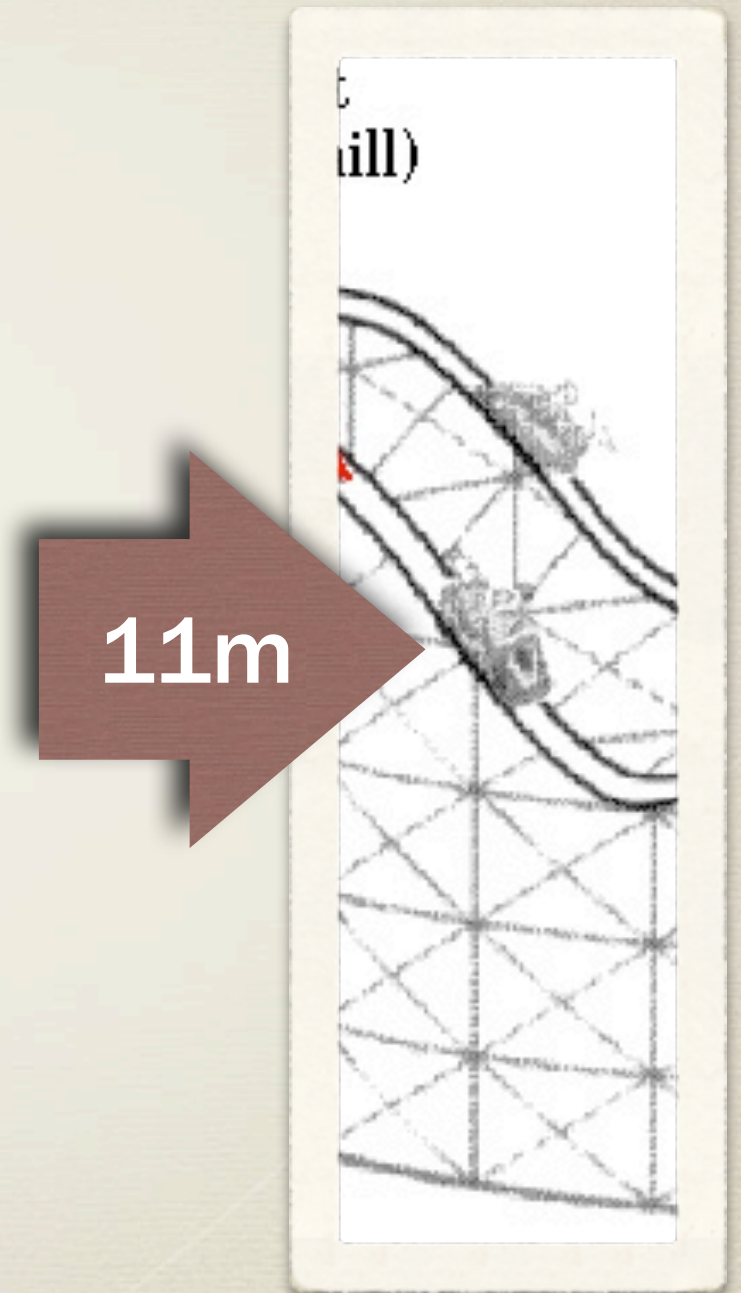
► $176,400 \text{ J} = \frac{1}{2}(1000)v^2$

► $v^2 = 352.8$

► $v = 18.78 \text{ m/s}$

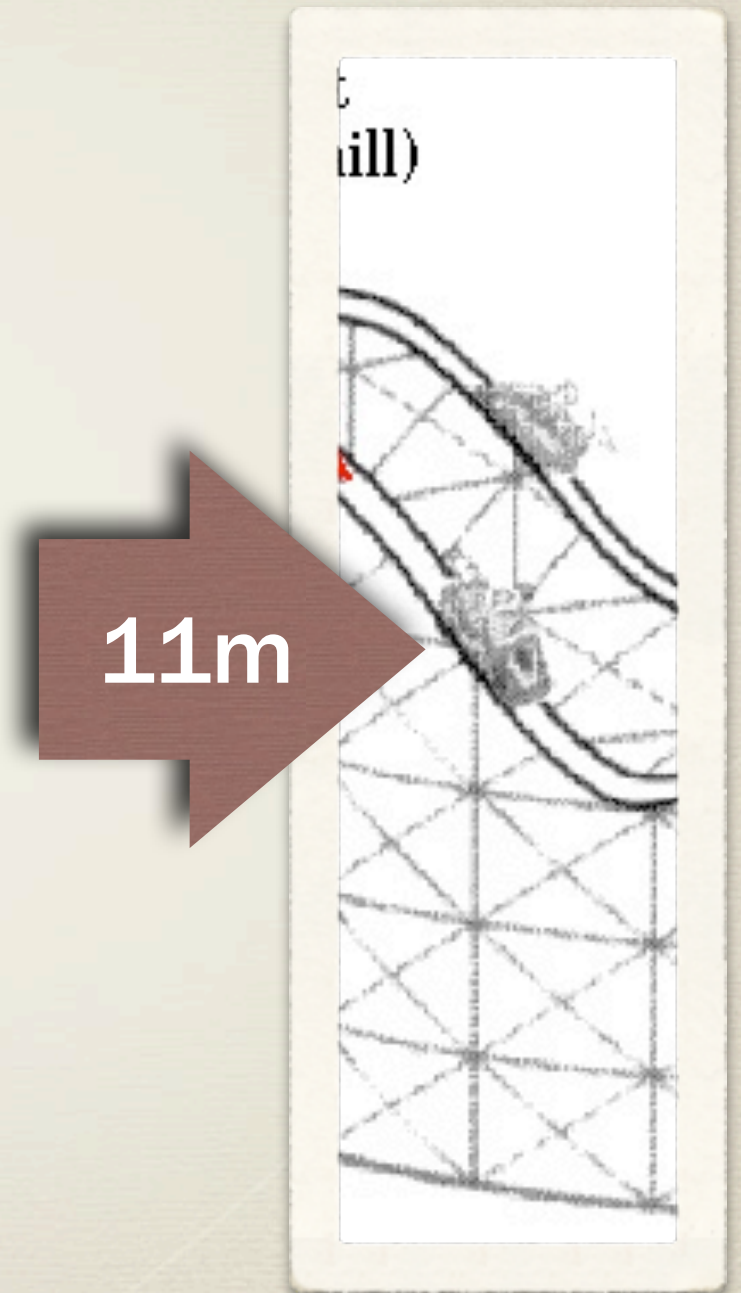


At point B(11m)



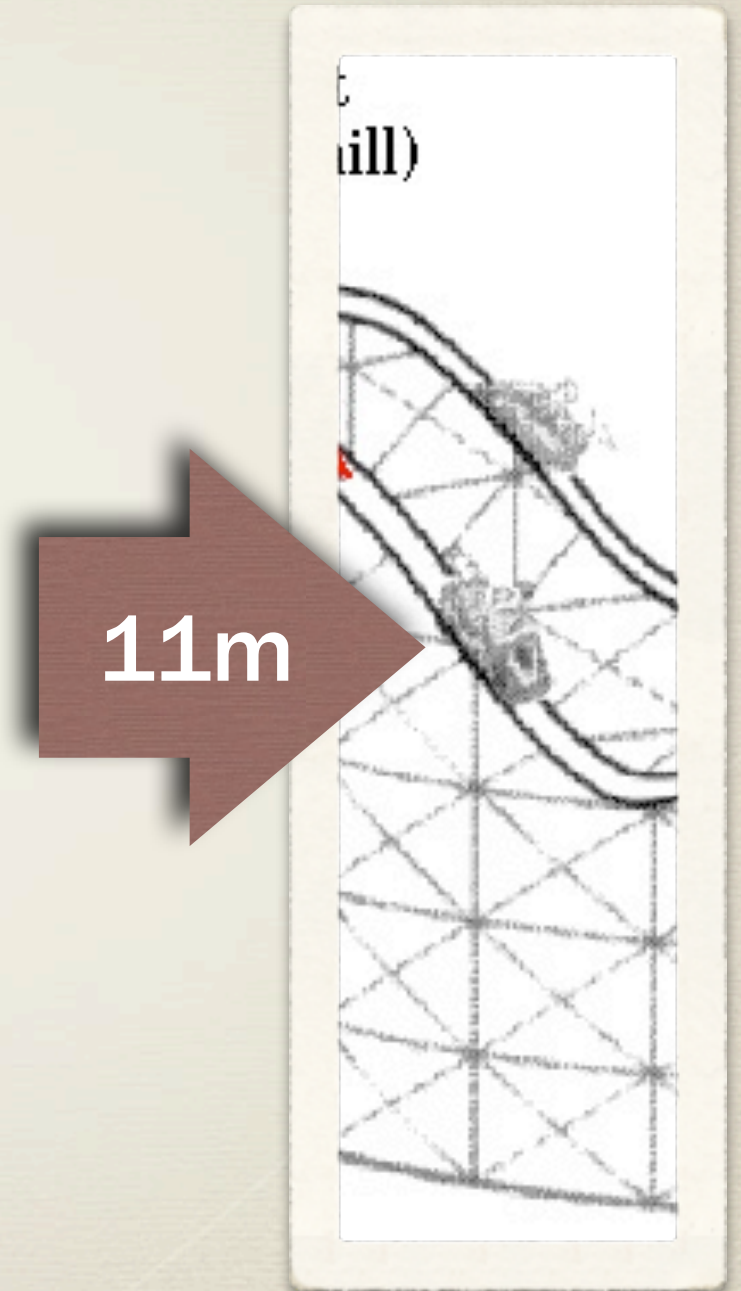
At point B(11m)

- ▶ Given Info:
 - ▶ $m = 1000 \text{ kg}$
 - ▶ $h = 11 \text{ m}$
 - ▶ $TE = 176.4 \text{ kJ}$



At point B(11m)

- ▶ Given Info:
 - ▶ $m = 1000 \text{ kg}$
 - ▶ $h = 11 \text{ m}$
 - ▶ $TE = 176.4 \text{ kJ}$
- ▶ $PE = mgh$



At point B(11m)

► Given Info:

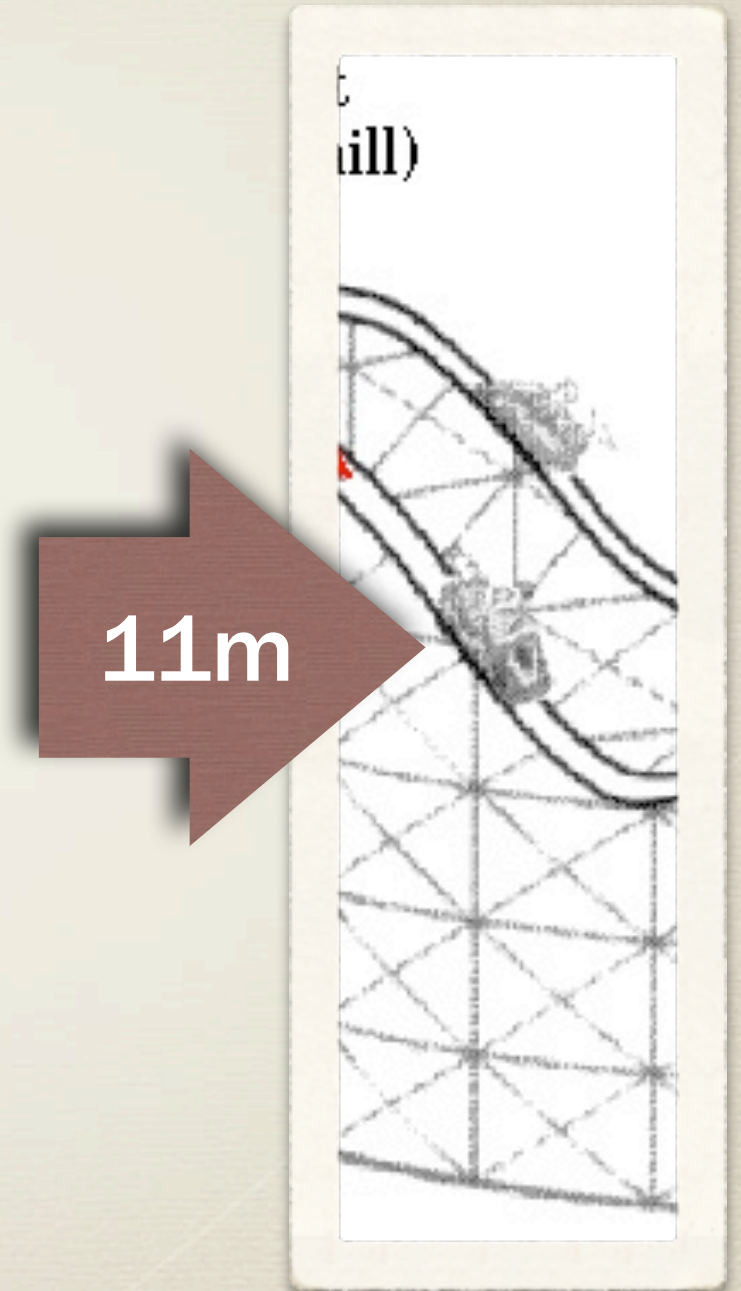
► $m = 1000 \text{ kg}$

► $h = 11 \text{ m}$

► $TE = 176.4 \text{ kJ}$

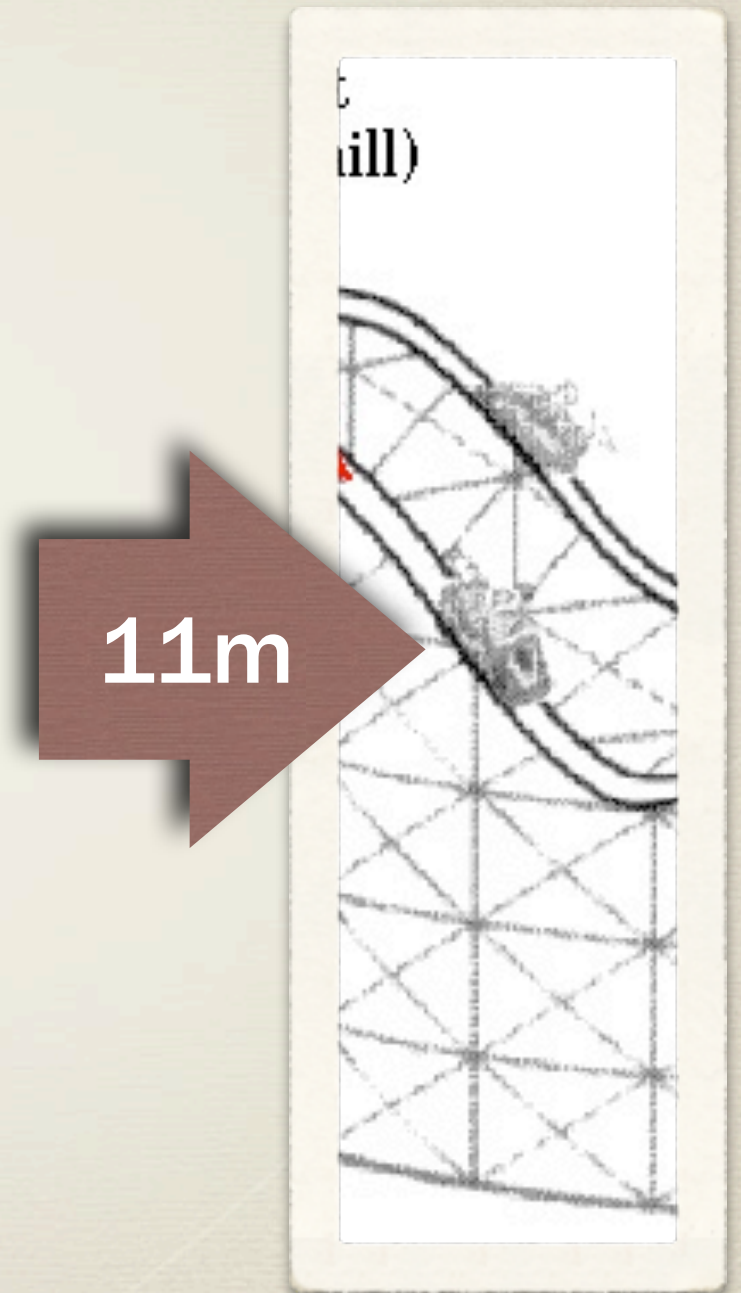
► $PE = mgh$

► $PE = (1000)(9.8)(11)$



At point B(11m)

- ▶ Given Info:
 - ▶ $m = 1000 \text{ kg}$
 - ▶ $h = 11 \text{ m}$
 - ▶ $TE = 176.4 \text{ kJ}$
- ▶ $PE = mgh$
- ▶ $PE = (1000)(9.8)(11)$
- ▶ $PE = 107,800 \text{ J}$



At point B(11m)

► Given Info:

- $m = 1000 \text{ kg}$
- $h = 11 \text{ m}$
- $TE = 176.4 \text{ kJ}$

► $PE = mgh$

► $PE = (1000)(9.8)(11)$

► $PE = 107,800 \text{ J}$

► $KE = 176,400 - 107,800 \text{ J} = 68,600 \text{ J}$

11m



At point B(11m)

► Given Info:

- $m = 1000 \text{ kg}$
- $h = 11 \text{ m}$
- $TE = 176.4 \text{ kJ}$

► $PE = mgh$

► $PE = (1000)(9.8)(11)$

► $PE = 107,800 \text{ J}$

► $KE = 176,400 - 107,800 \text{ J} = 68,600 \text{ J}$

► $KE = 68,600 \text{ J} = \frac{1}{2}(mv^2)$

11m



At point B(11m)

► Given Info:

- $m = 1000 \text{ kg}$
- $h = 11 \text{ m}$
- $TE = 176.4 \text{ kJ}$

► $PE = mgh$

► $PE = (1000)(9.8)(11)$

► $PE = 107,800 \text{ J}$

► $KE = 176,400 - 107,800 \text{ J} = 68,600 \text{ J}$

► $KE = 68,600 \text{ J} = \frac{1}{2}(mv^2)$

► $68,600 \text{ J} = \frac{1}{2}(1000)v^2$

11m



At point B(11m)

► Given Info:

- $m = 1000 \text{ kg}$
- $h = 11 \text{ m}$
- $TE = 176.4 \text{ kJ}$

► $PE = mgh$

► $PE = (1000)(9.8)(11)$

► $PE = 107,800 \text{ J}$

► $KE = 176,400 - 107,800 \text{ J} = 68,600 \text{ J}$

► $KE = 68,600 \text{ J} = \frac{1}{2}(mv^2)$

► $68,600 \text{ J} = \frac{1}{2}(1000)v^2$

► $v = 11.71 \text{ m/s}$

11m



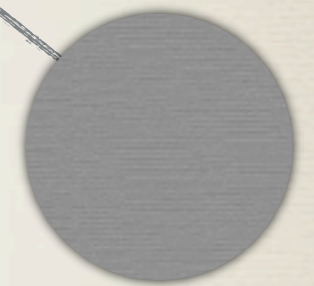


Pendulum Swing

Conservation of Energy Problems

Find the Speed

- ▶ A pendulum bob on a 2m string is released from a height of 80cm.
- ▶ What is the maximum velocity of the pendulum?
- ▶ What is the speed at half the height?

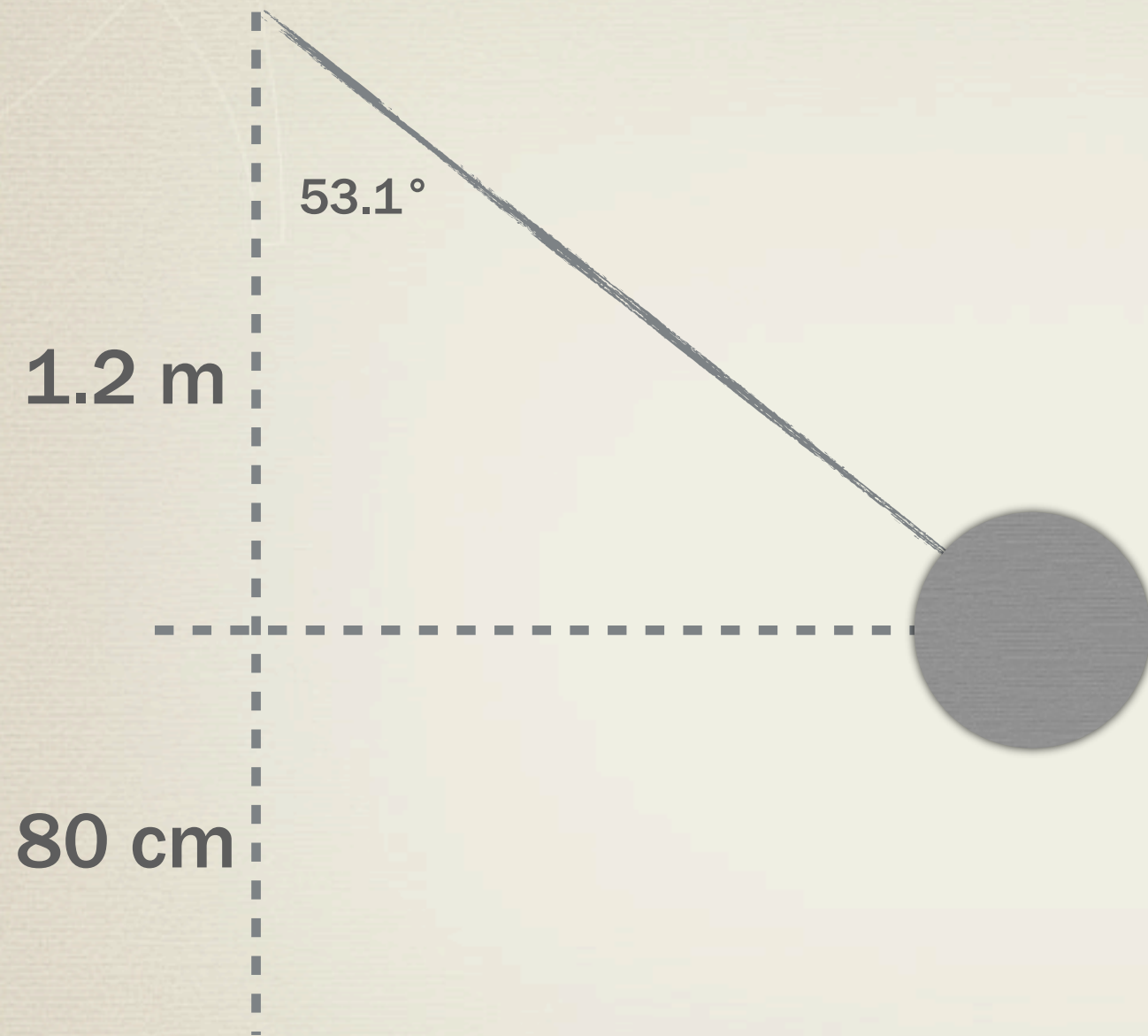


Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

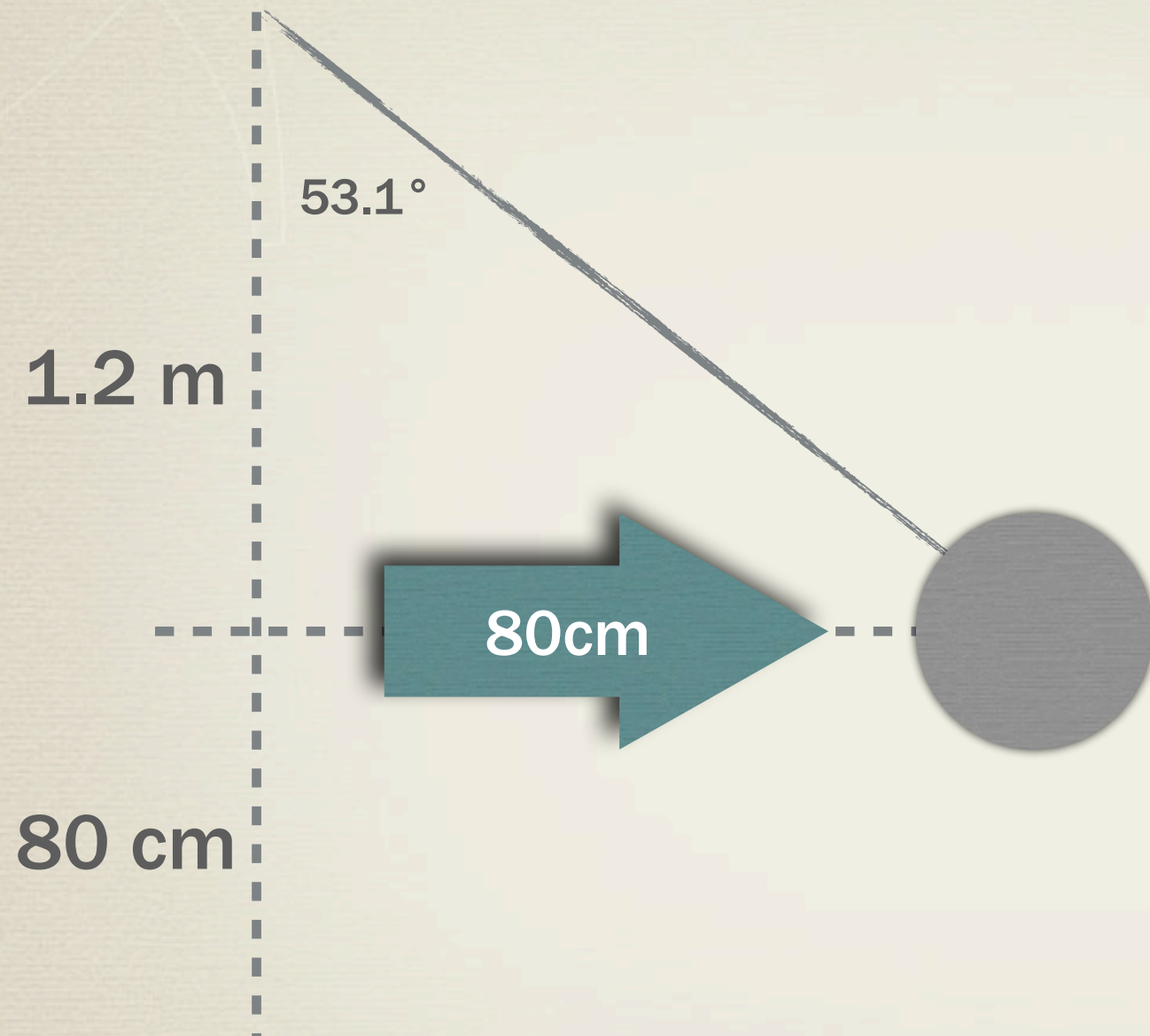


Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

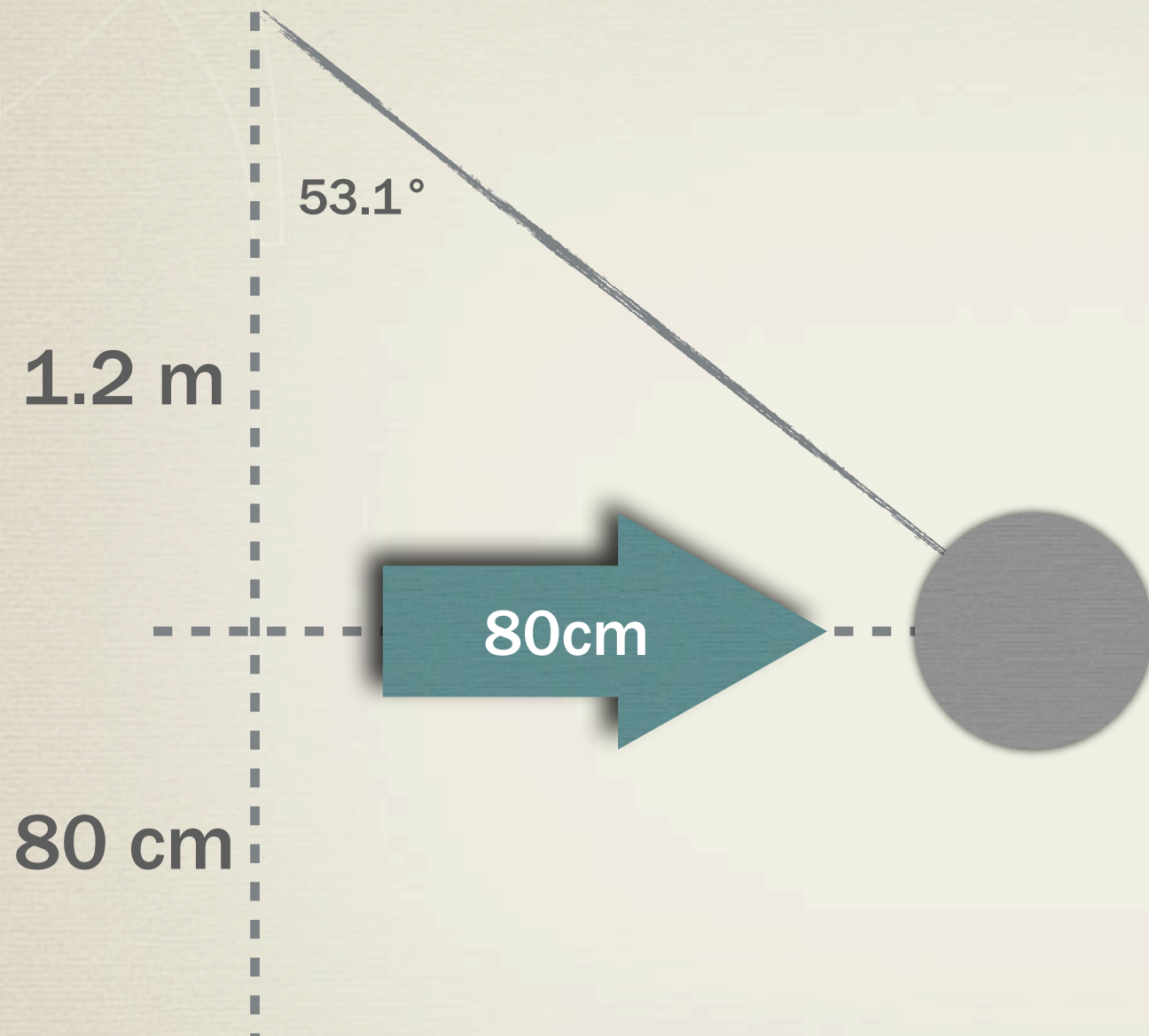


Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?



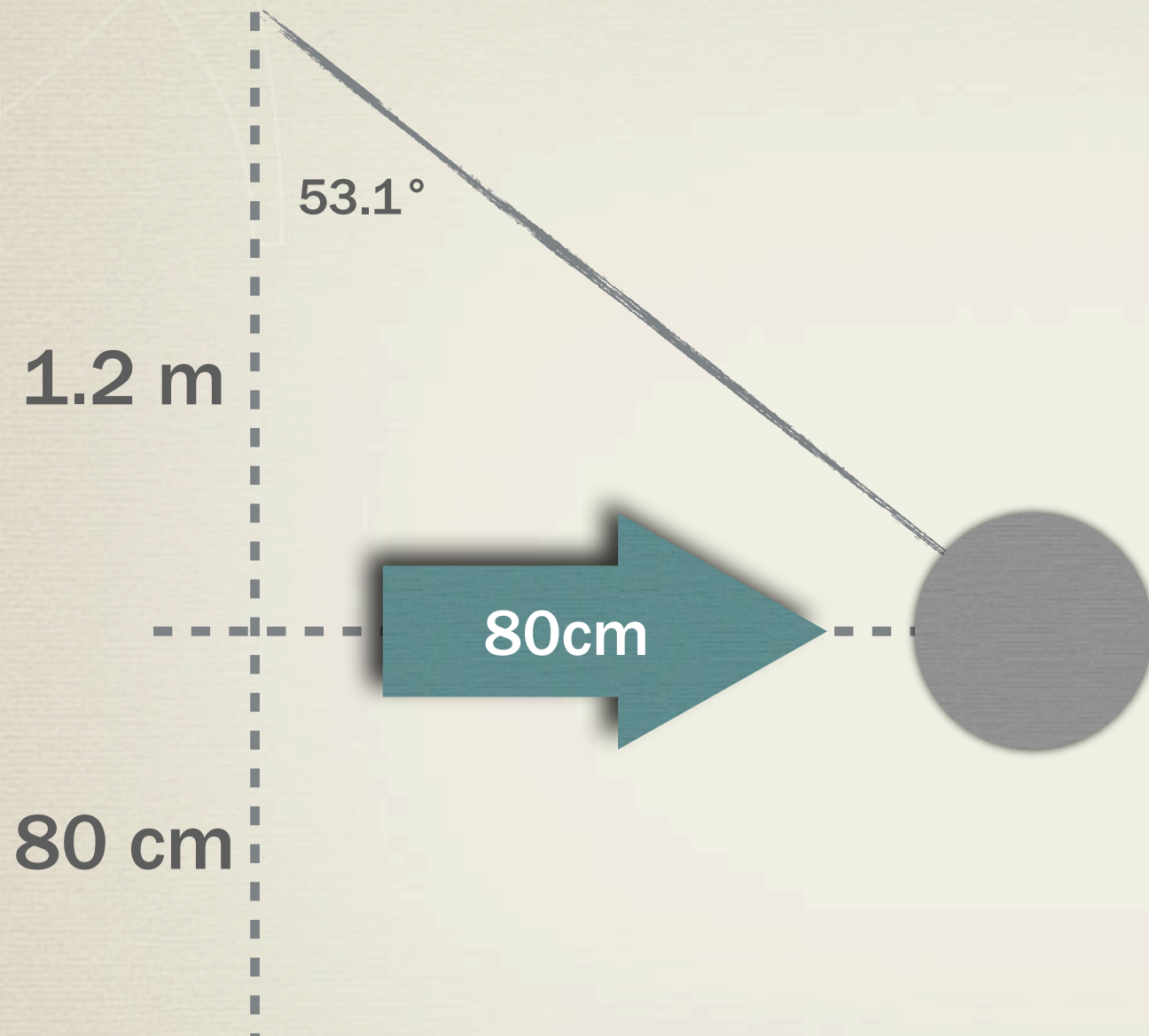
► Mass = 0.1 kg

Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?



► Mass = 0.1 kg

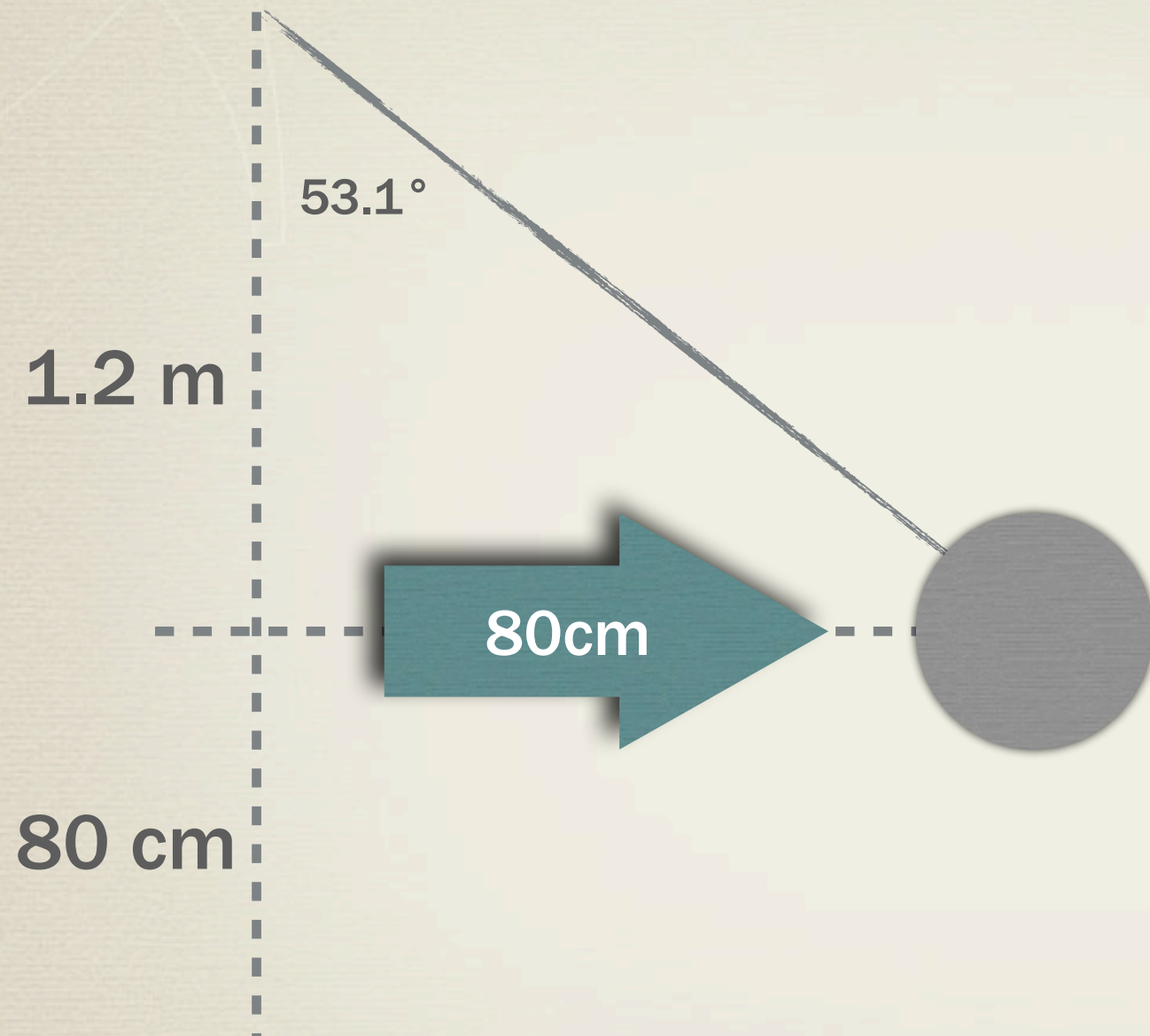
► $h = 0.8 \text{ m}$

Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?



▶ Mass = 0.1 kg

▶ $h = 0.8 \text{ m}$

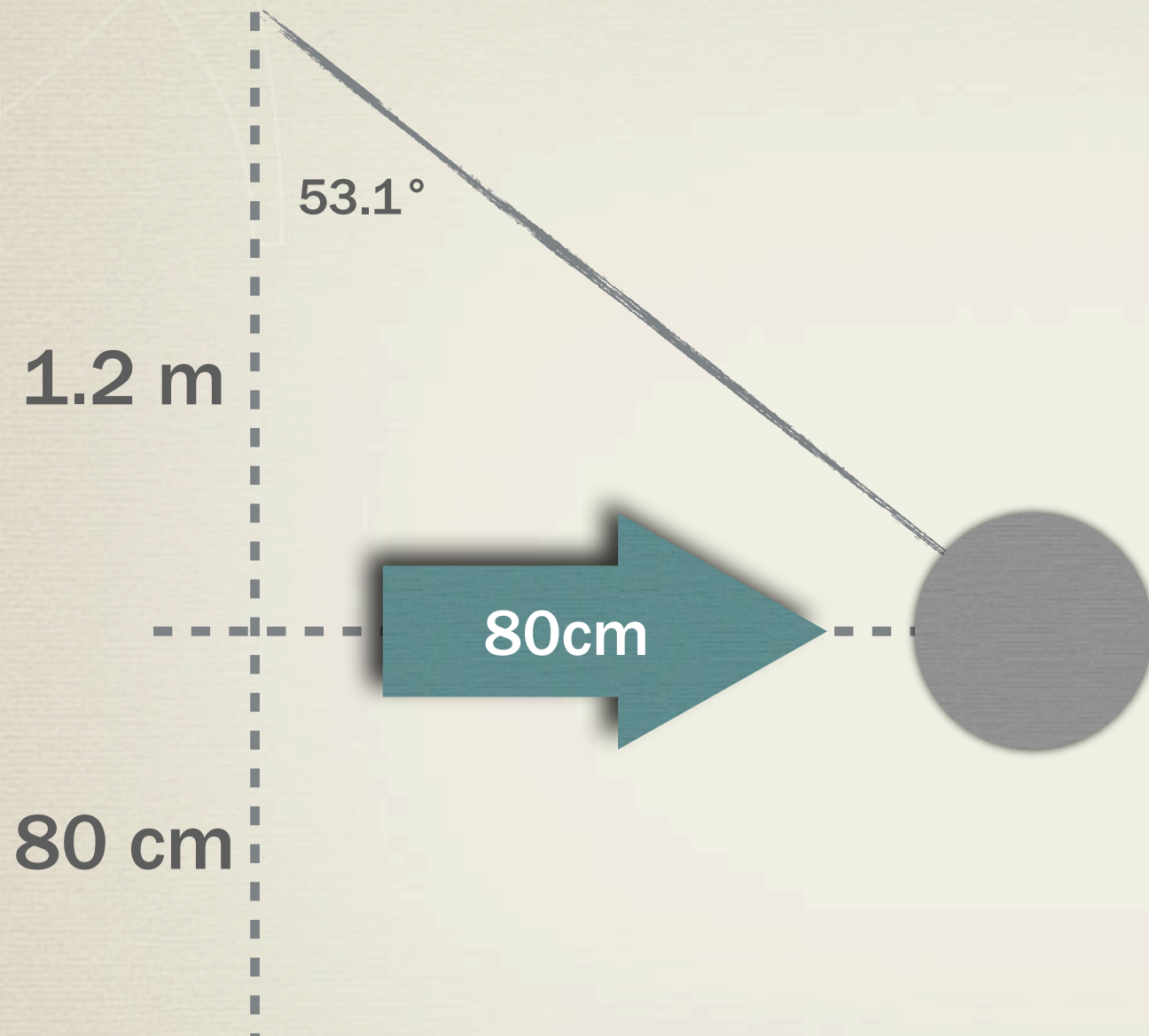
▶ $PE = mgh = 0.784 \text{ J}$

Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

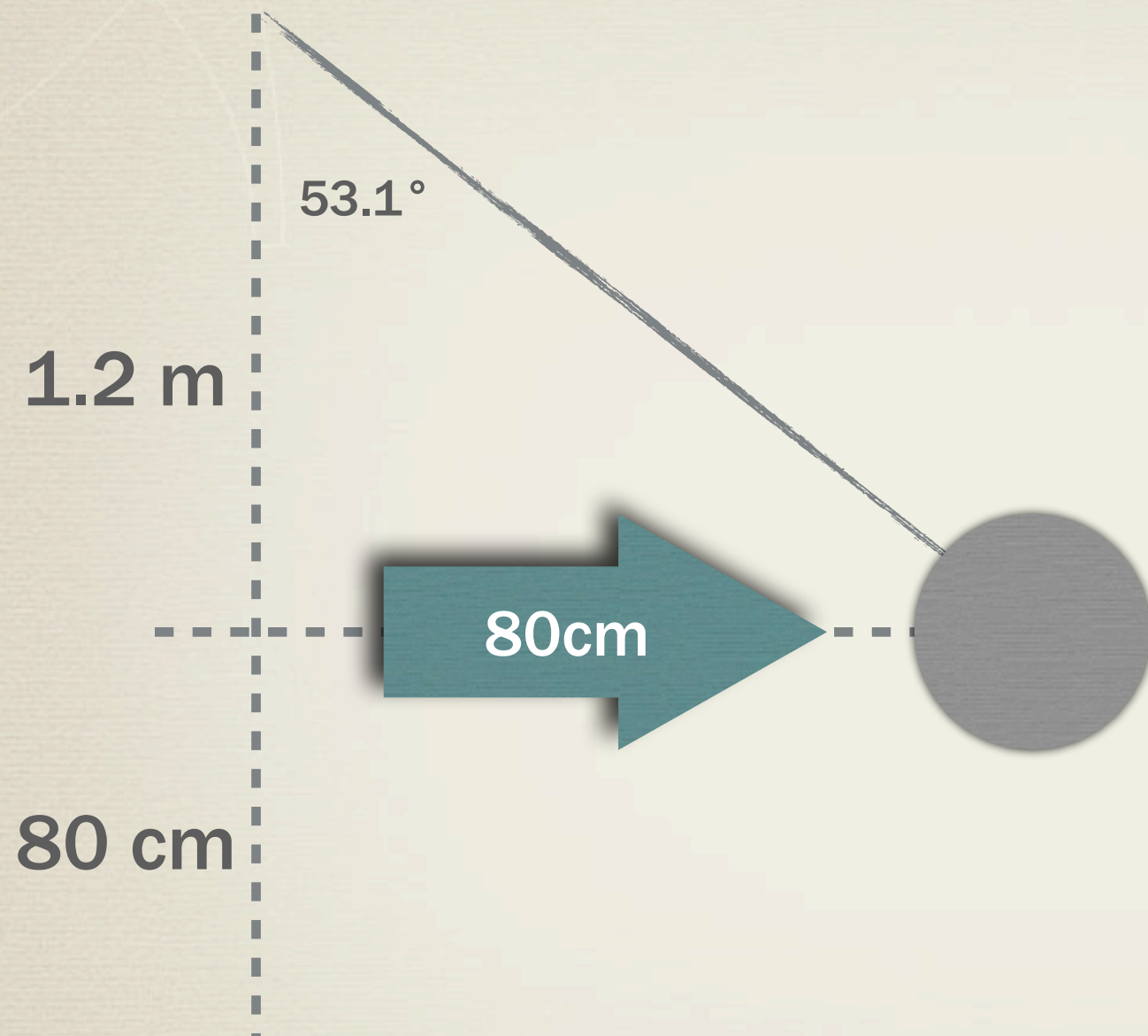
What is the maximum velocity of the pendulum?

What is the speed at half the height?



- ▶ Mass = 0.1 kg
- ▶ $h = 0.8 \text{ m}$
- ▶ $PE = mgh = 0.784 \text{ J}$
- ▶ Velocity = 0 m/s

Find the Speed



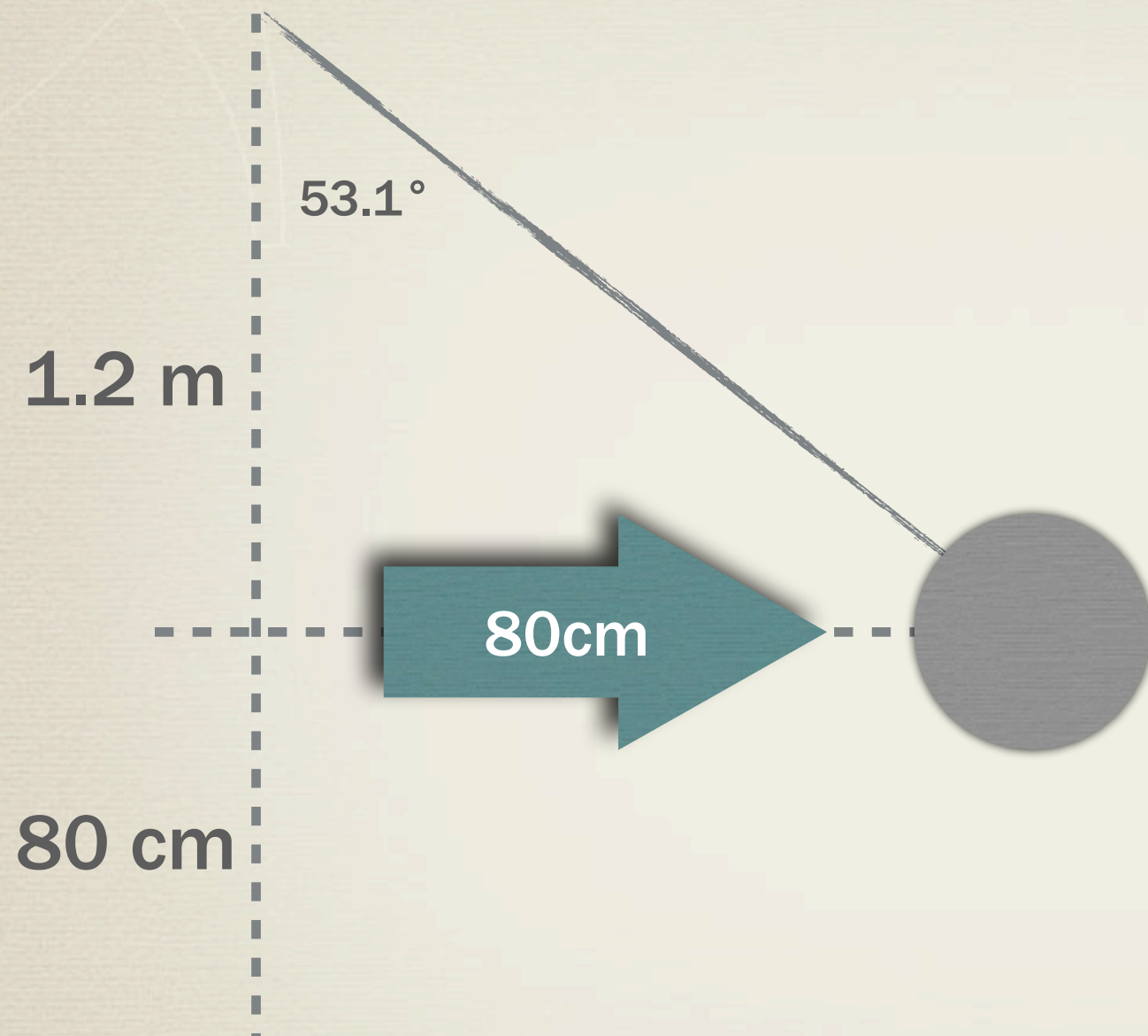
A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

- ▶ Mass = 0.1 kg
- ▶ $h = 0.8 \text{ m}$
- ▶ $PE = mgh = 0.784 \text{ J}$
- ▶ Velocity = 0 m/s
- ▶ $KE = 0 \text{ J}$

Find the Speed



A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

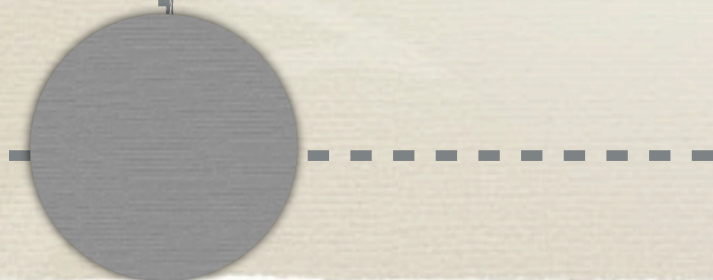
What is the speed at half the height?

- ▶ Mass = 0.1 kg
- ▶ $h = 0.8$ m
- ▶ $PE = mgh = 0.784\text{J}$
- ▶ Velocity = 0 m/s
- ▶ $KE = 0$ J
- ▶ $TE = 0.784\text{J}$

Find the Speed

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$



A 100g pendulum bob on a 2m string is released from a height of 80cm.

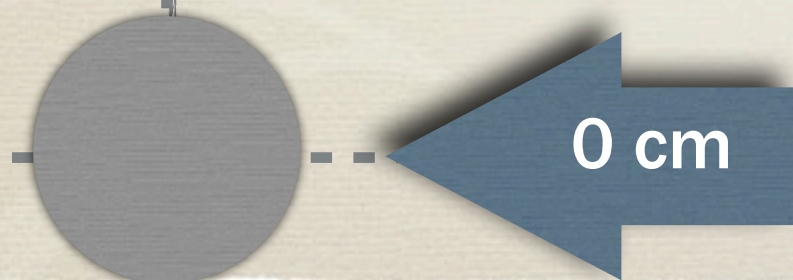
What is the maximum velocity of the pendulum?

What is the speed at half the height?

Find the Speed

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$



A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

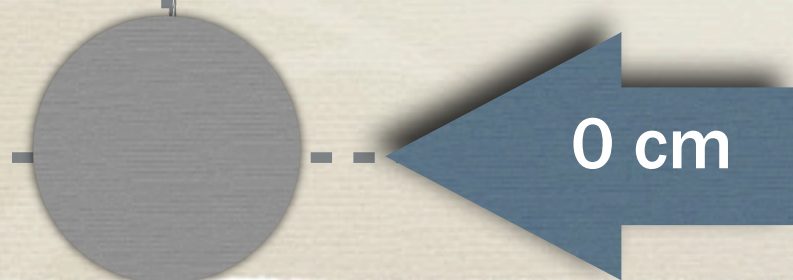
What is the speed at half the height?

80cm

- ▶ $PE = 0.784J$
- ▶ $KE = 0 J$
- ▶ $TE = 0.784J$

▶ Given Info:

- ▶ Mass = 0.1 kg
- ▶ $TE = 0.784J$
- ▶ $h = 0.0 m$



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

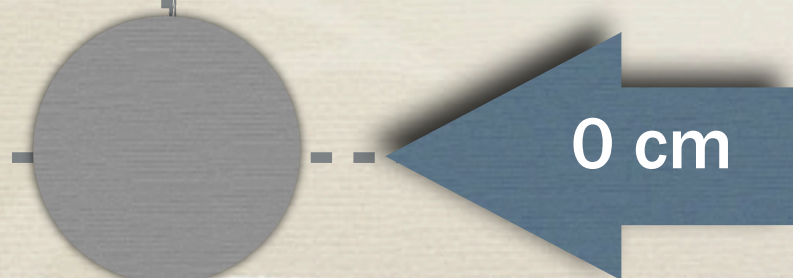
What is the speed at half the height?

80cm

- ▶ $PE = 0.784J$
- ▶ $KE = 0 J$
- ▶ $TE = 0.784J$

▶ Given Info:

- ▶ Mass = 0.1 kg
- ▶ $TE = 0.784J$
- ▶ $h = 0.0 m$
- ▶ $PE = mgh = 0 J$



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

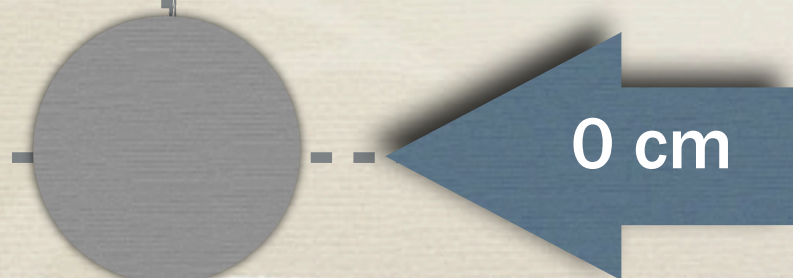
What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$

▶ Given Info:

- ▶ Mass = 0.1 kg
- ▶ $TE = 0.784\text{J}$
- ▶ $h = 0.0\text{ m}$
- ▶ $PE = mgh = 0\text{ J}$
- ▶ $KE = 0.784\text{ J} = \frac{1}{2}(mv^2)$



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

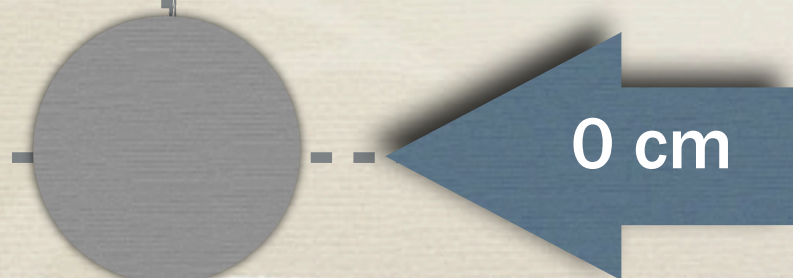
What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$

▶ Given Info:

- ▶ Mass = 0.1 kg
- ▶ $TE = 0.784\text{J}$
- ▶ $h = 0.0\text{ m}$
- ▶ $PE = mgh = 0\text{ J}$
- ▶ $KE = 0.784\text{ J} = \frac{1}{2}(mv^2)$
- ▶ $0.784\text{ J} = \frac{1}{2}(0.1)(v^2)$



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

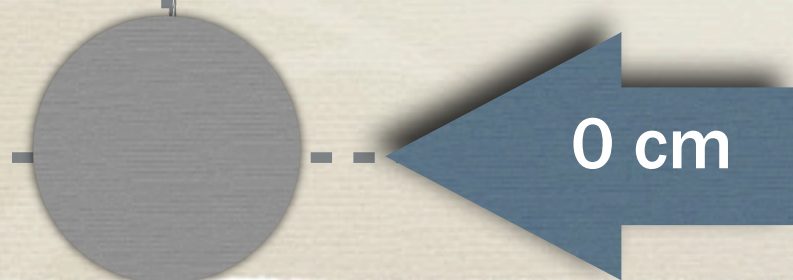
What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$

▶ Given Info:

- ▶ Mass = 0.1 kg
- ▶ $TE = 0.784\text{J}$
- ▶ $h = 0.0\text{ m}$
- ▶ $PE = mgh = 0\text{ J}$
- ▶ $KE = 0.784\text{ J} = \frac{1}{2}(mv^2)$
- ▶ $0.784\text{ J} = \frac{1}{2}(0.1)(v^2)$
- ▶ $v = 3.96\text{ m/s}$



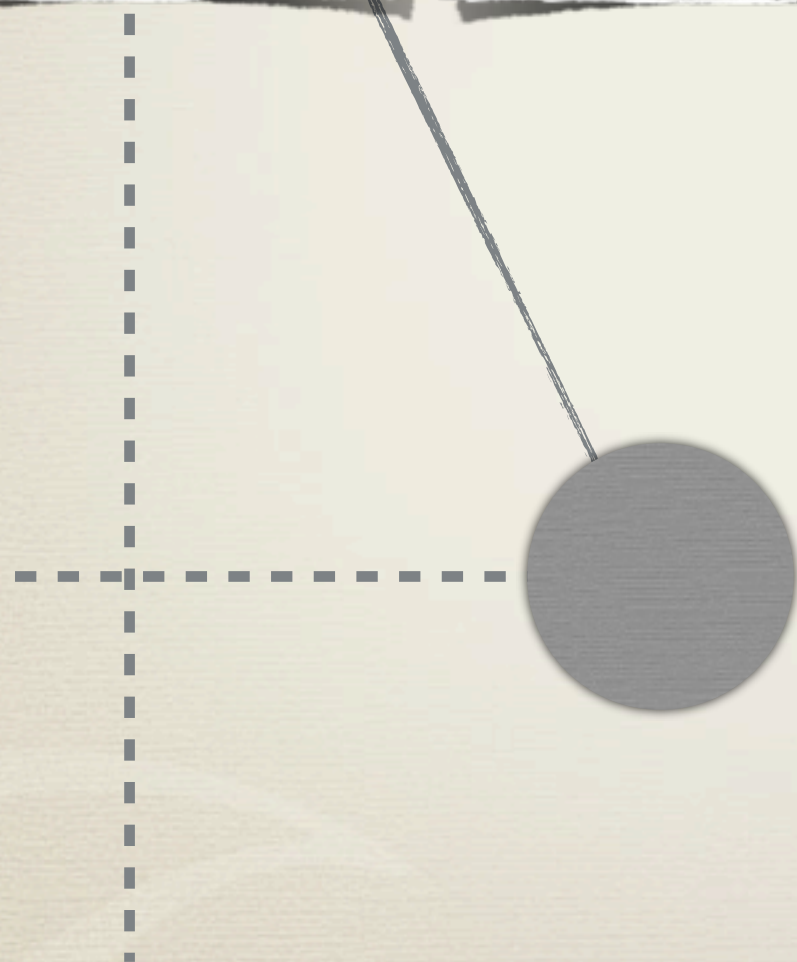
Find the Speed

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 0.0\text{ m/s}$

0cm

- ▶ $PE = 0\text{ J}$
- ▶ $KE = 0.784\text{J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 3.96\text{ m/s}$



A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 0.0\text{ m/s}$

0cm

- ▶ $PE = 0\text{ J}$
- ▶ $KE = 0.784\text{J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 3.96\text{ m/s}$



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What is the maximum velocity of the pendulum?

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80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 0.0\text{ m/s}$

0cm

- ▶ $PE = 0\text{ J}$
- ▶ $KE = 0.784\text{J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 3.96\text{ m/s}$

▶ **Given Info:**

- ▶ $m = 0.1\text{ kg}$
- ▶ $TE = 0.784\text{J}$
- ▶ $h = 0.4\text{ m}$



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 0.0\text{ m/s}$

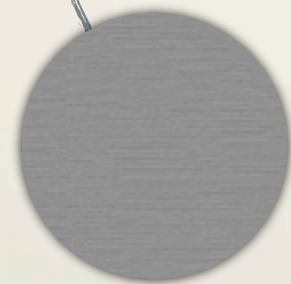
0cm

- ▶ $PE = 0\text{ J}$
- ▶ $KE = 0.784\text{J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 3.96\text{ m/s}$

▶ **Given Info:**

- ▶ $m = 0.1\text{ kg}$
- ▶ $TE = 0.784\text{J}$
- ▶ $h = 0.4\text{ m}$
- ▶ $PE = mgh = 0.392\text{ J}$

40cm



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 0.0\text{ m/s}$

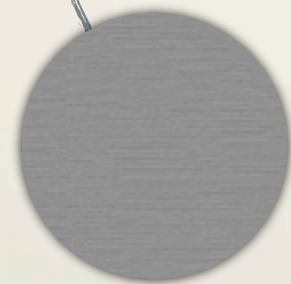
0cm

- ▶ $PE = 0\text{ J}$
- ▶ $KE = 0.784\text{J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 3.96\text{ m/s}$

▶ **Given Info:**

- ▶ $m = 0.1\text{ kg}$
- ▶ $TE = 0.784\text{J}$
- ▶ $h = 0.4\text{ m}$
- ▶ $PE = mgh = 0.392\text{ J}$
- ▶ $KE = 0.392\text{ J} = \frac{1}{2}(mv^2)$

40cm



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 0.0\text{ m/s}$

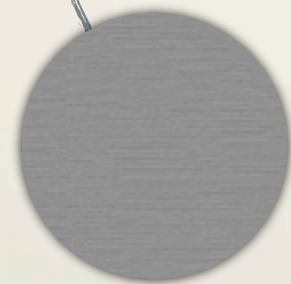
0cm

- ▶ $PE = 0\text{ J}$
- ▶ $KE = 0.784\text{J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 3.96\text{ m/s}$

▶ Given Info:

- ▶ $m = 0.1\text{ kg}$
- ▶ $TE = 0.784\text{J}$
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- ▶ $PE = mgh = 0.392\text{ J}$
- ▶ $KE = 0.392\text{ J} = \frac{1}{2}(mv^2)$
- ▶ $0.392\text{ J} = \frac{1}{2}(0.1)(v^2)$

40cm



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

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What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 0.0\text{ m/s}$

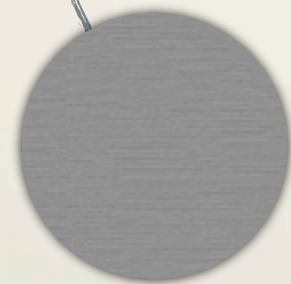
0cm

- ▶ $PE = 0\text{ J}$
- ▶ $KE = 0.784\text{J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 3.96\text{ m/s}$

▶ **Given Info:**

- ▶ $m = 0.1\text{ kg}$
- ▶ $TE = 0.784\text{J}$
- ▶ $h = 0.4\text{ m}$
- ▶ $PE = mgh = 0.392\text{ J}$
- ▶ $KE = 0.392\text{ J} = \frac{1}{2}(mv^2)$
- ▶ $0.392\text{ J} = \frac{1}{2}(0.1)(v^2)$
- ▶ $v^2 = 7.84$

40cm



Find the Speed

A 100g pendulum bob on a 2m string is released from a height of 80cm.

What is the maximum velocity of the pendulum?

What is the speed at half the height?

80cm

- ▶ $PE = 0.784\text{J}$
- ▶ $KE = 0\text{ J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 0.0\text{ m/s}$

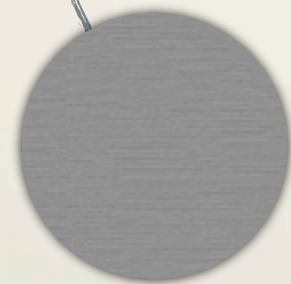
0cm

- ▶ $PE = 0\text{ J}$
- ▶ $KE = 0.784\text{J}$
- ▶ $TE = 0.784\text{J}$
- ▶ $v = 3.96\text{ m/s}$

▶ Given Info:

- ▶ $m = 0.1\text{ kg}$
- ▶ $TE = 0.784\text{J}$
- ▶ $h = 0.4\text{ m}$
- ▶ $PE = mgh = 0.392\text{ J}$
- ▶ $KE = 0.392\text{ J} = \frac{1}{2}(mv^2)$
- ▶ $0.392\text{ J} = \frac{1}{2}(0.1)(v^2)$
- ▶ $v^2 = 7.84$
- ▶ $v = 2.8\text{ m/s}$
- ▶ *(not half the maximum speed)*

40cm



Find the Speed

honors style

- ▶ A 250g pendulum bob on a 2m string is released from an angle of 60° .
- ▶ What is the speed when the string forms a 20° angle with the vertical



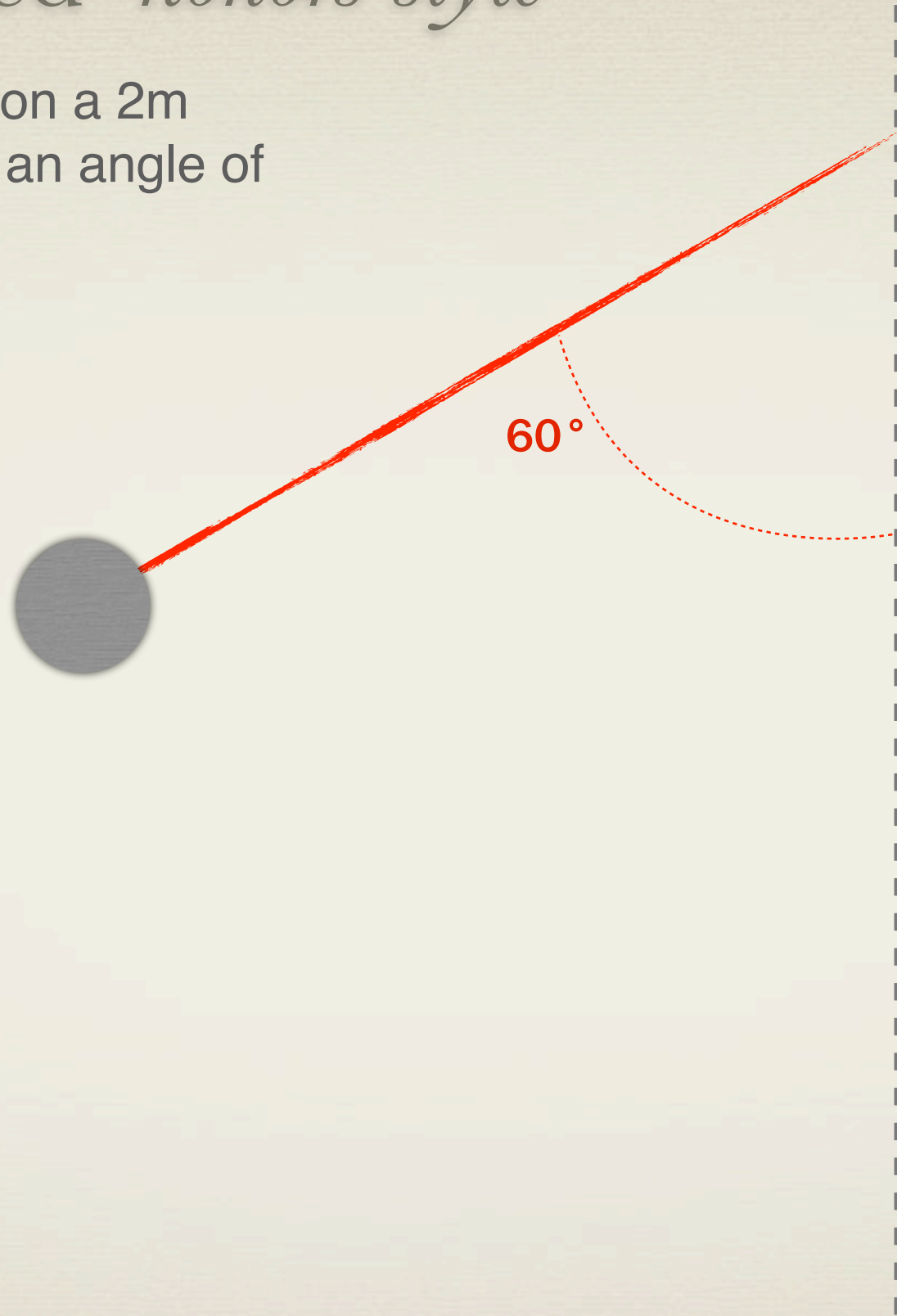
Find the Speed- *honors style*

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

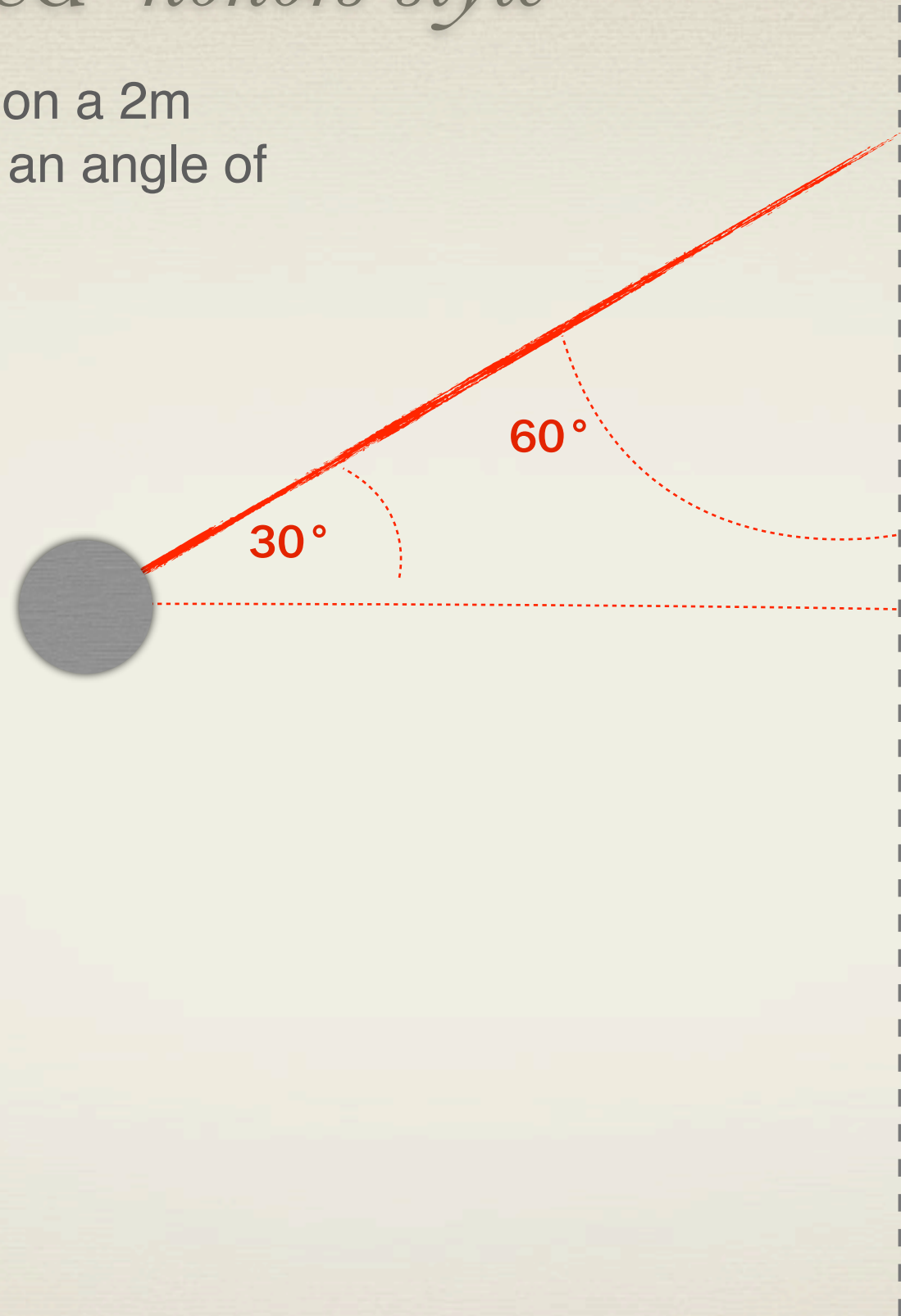
Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.



Find the Speed- *honors style*

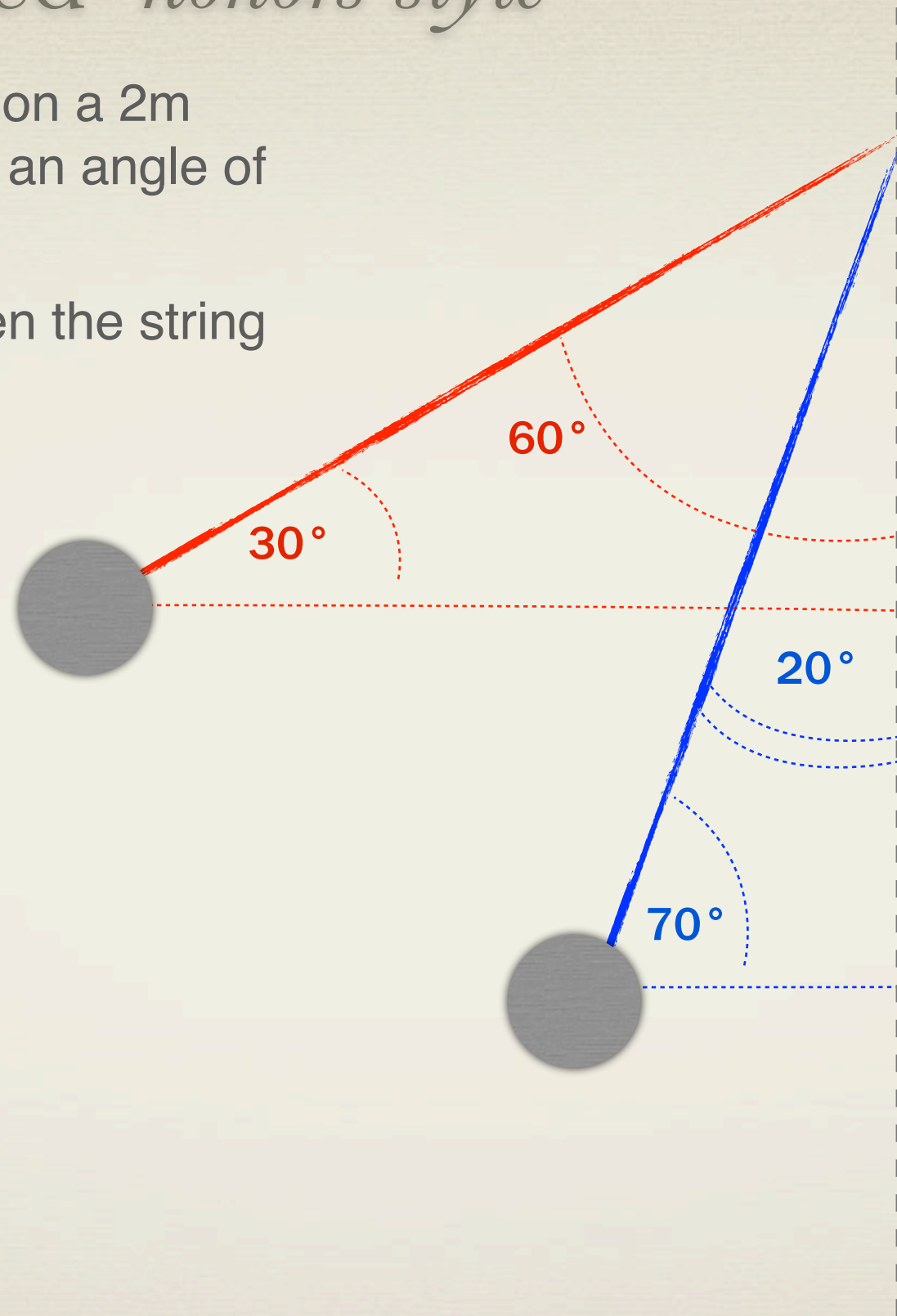
A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.



Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

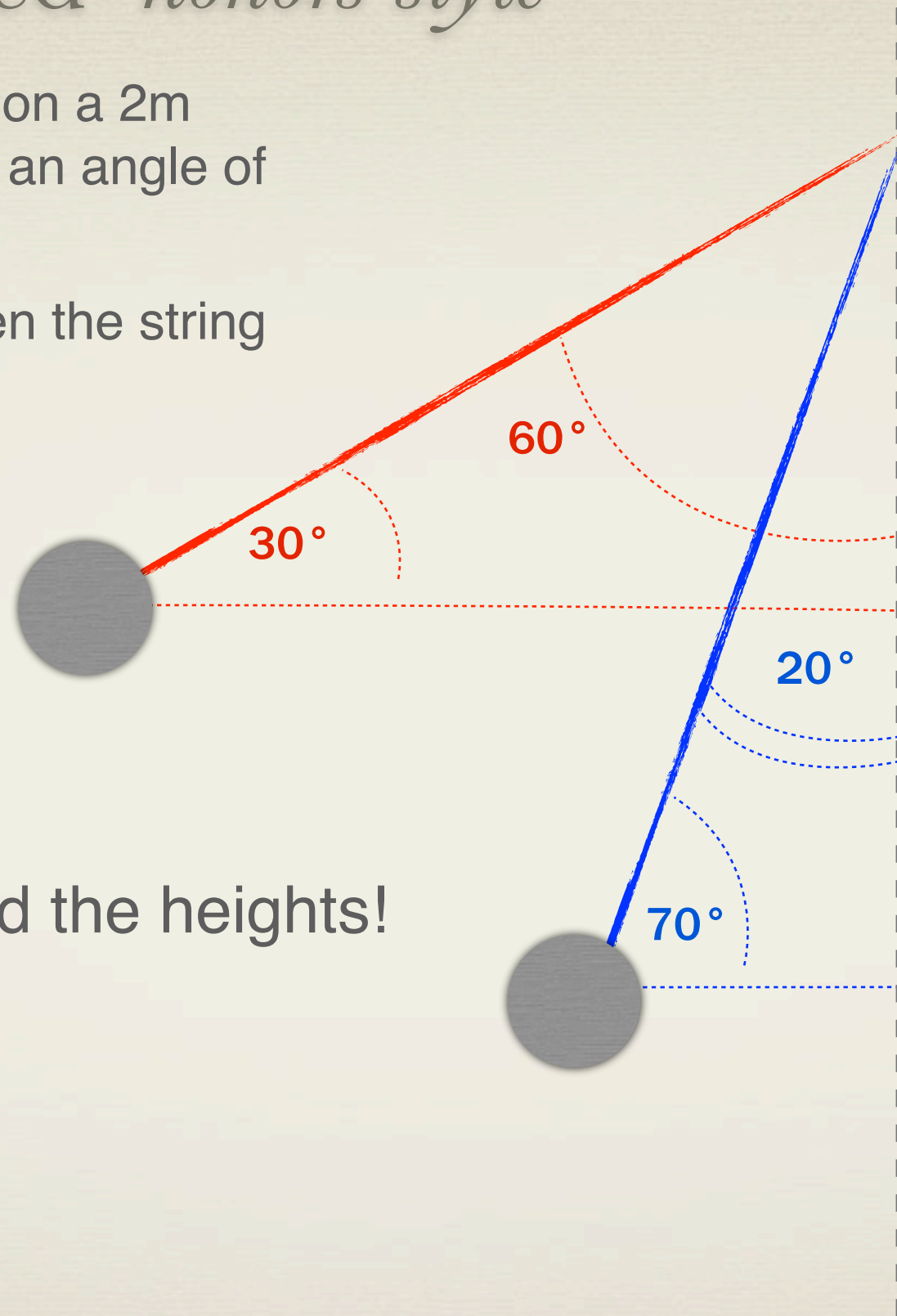
What is the speed when the string forms a 20° angle?



Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?

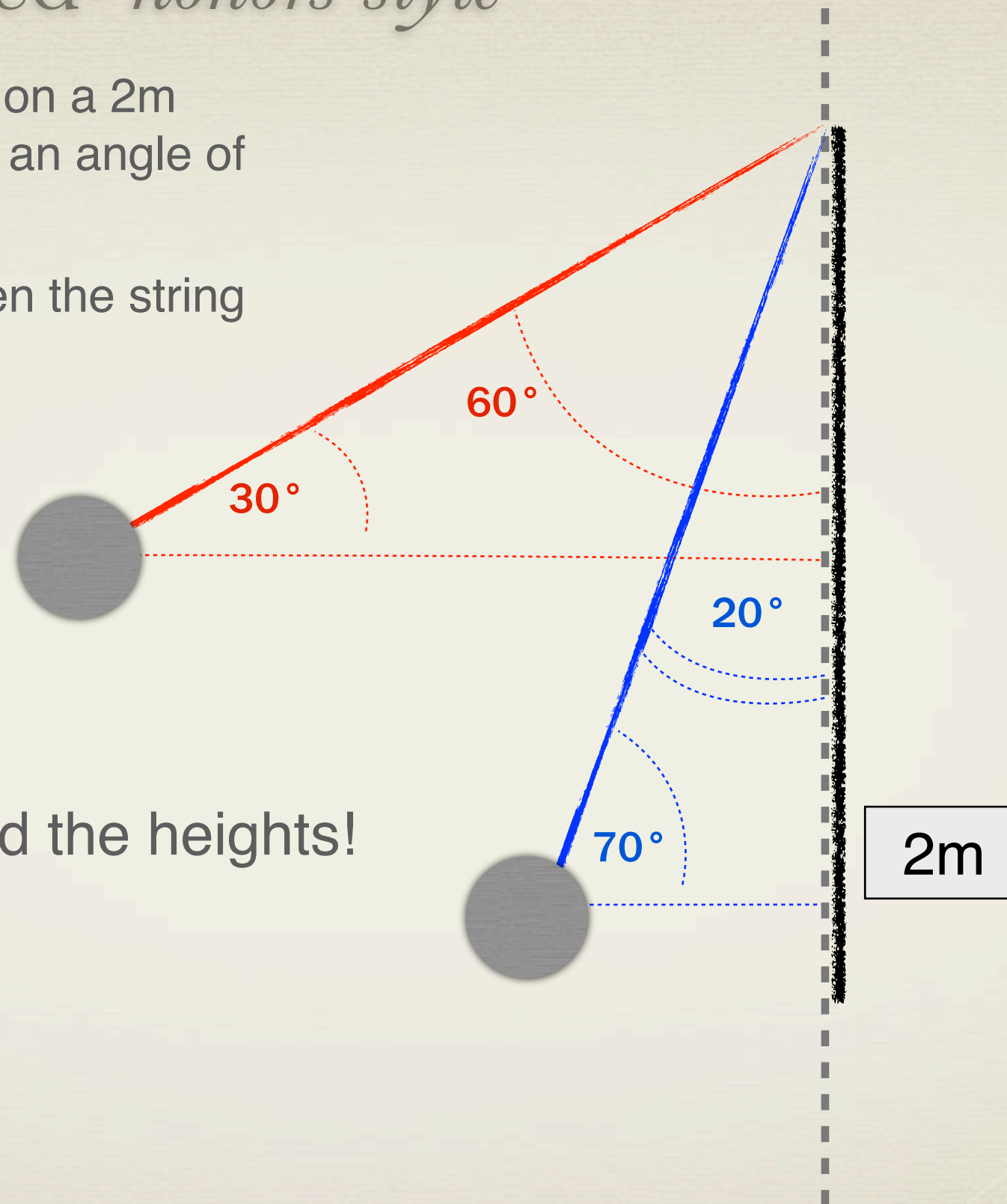


So, you need to find the heights!

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?

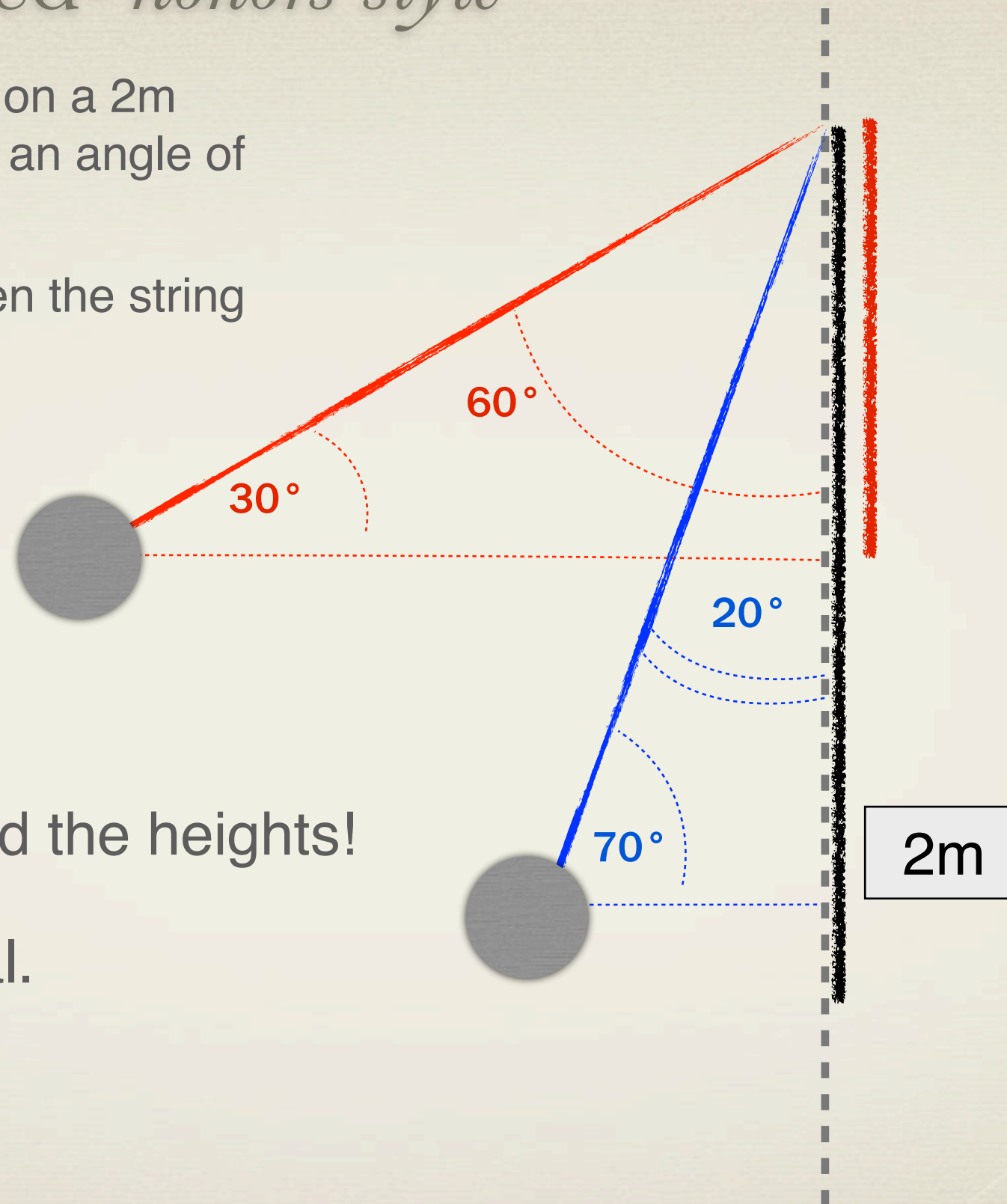


So, you need to find the heights!

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?



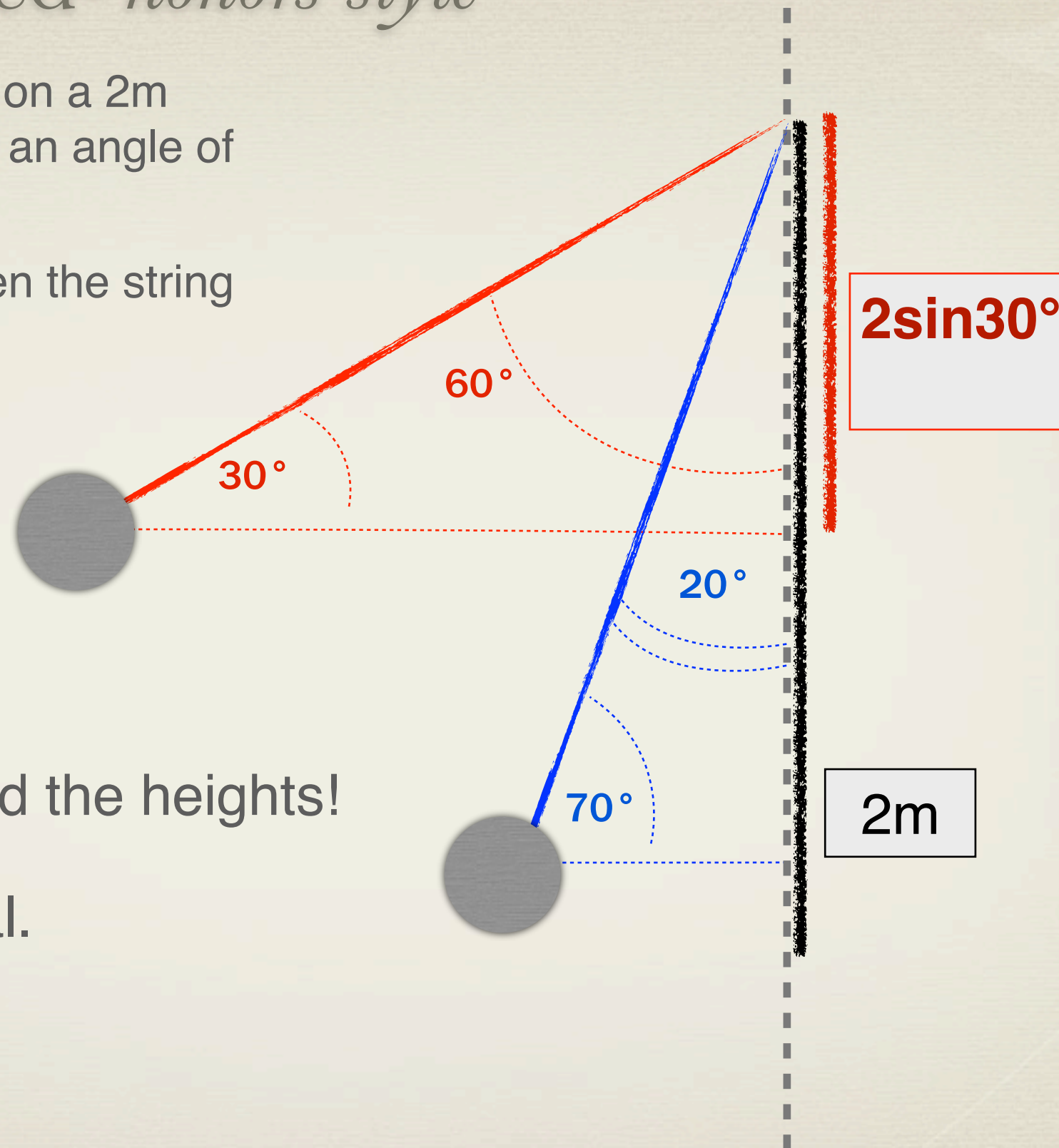
So, you need to find the heights!

60° with the vertical.

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?



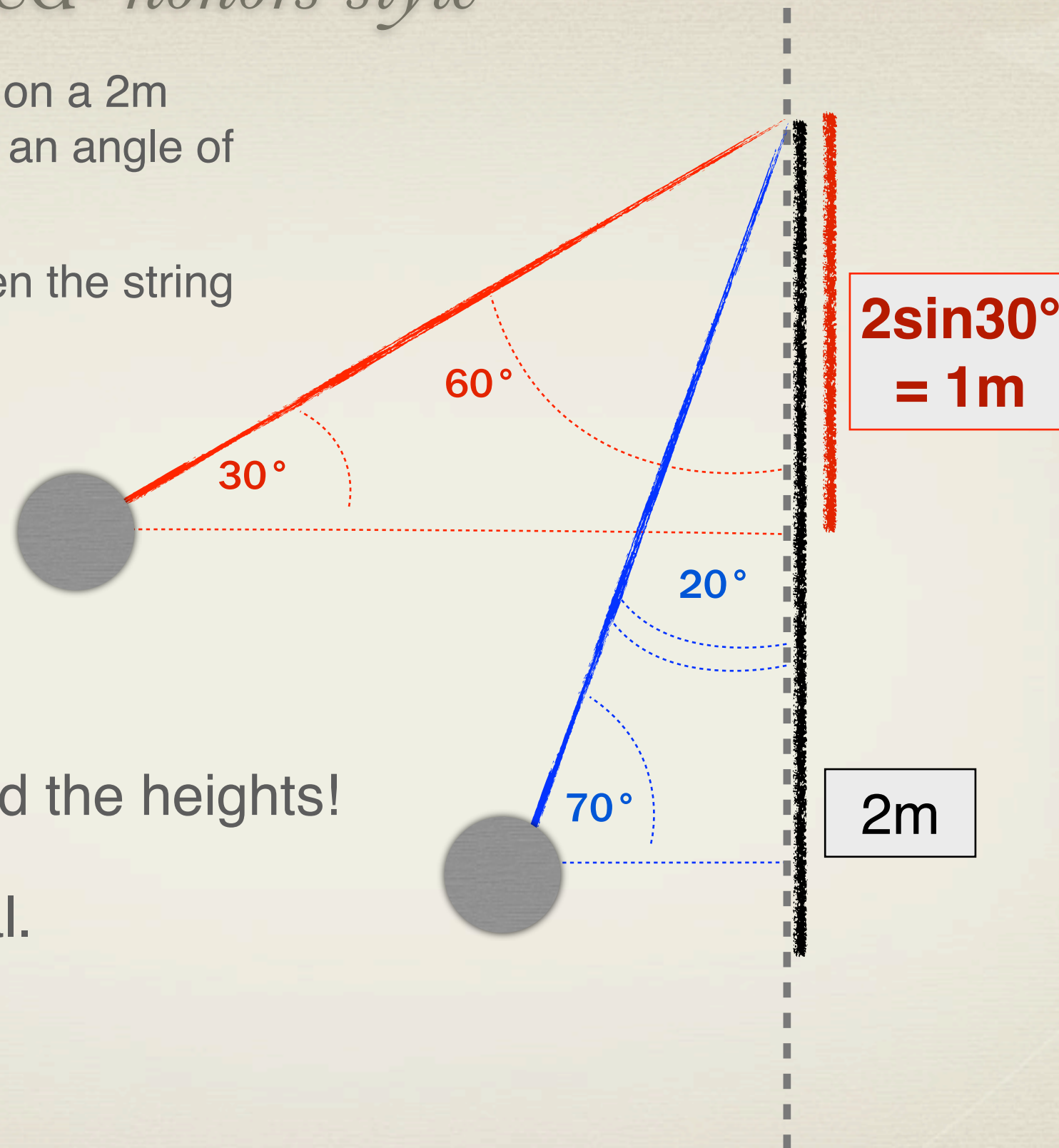
So, you need to find the heights!

60° with the vertical.

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?



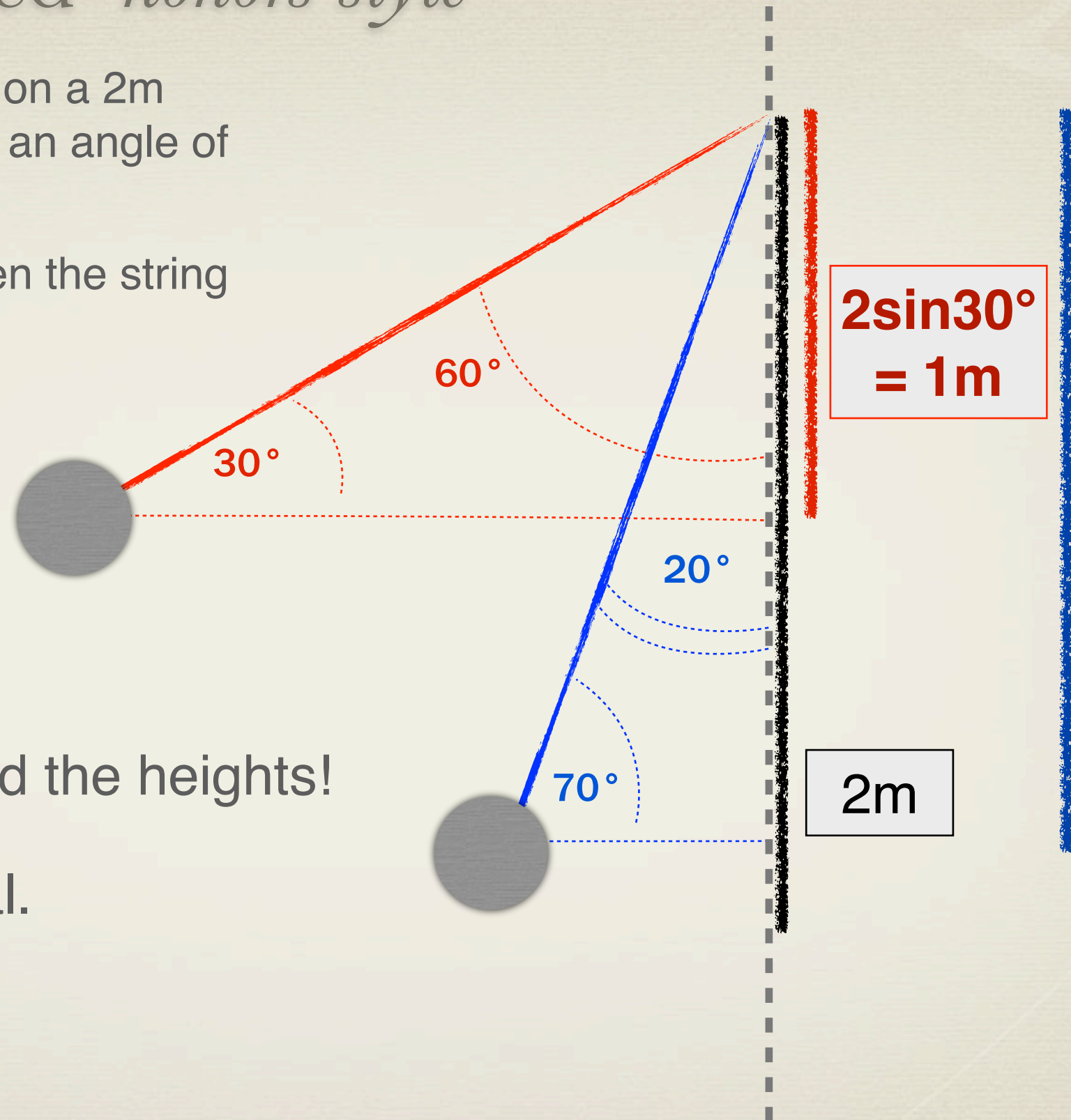
So, you need to find the heights!

60° with the vertical.

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?



So, you need to find the heights!

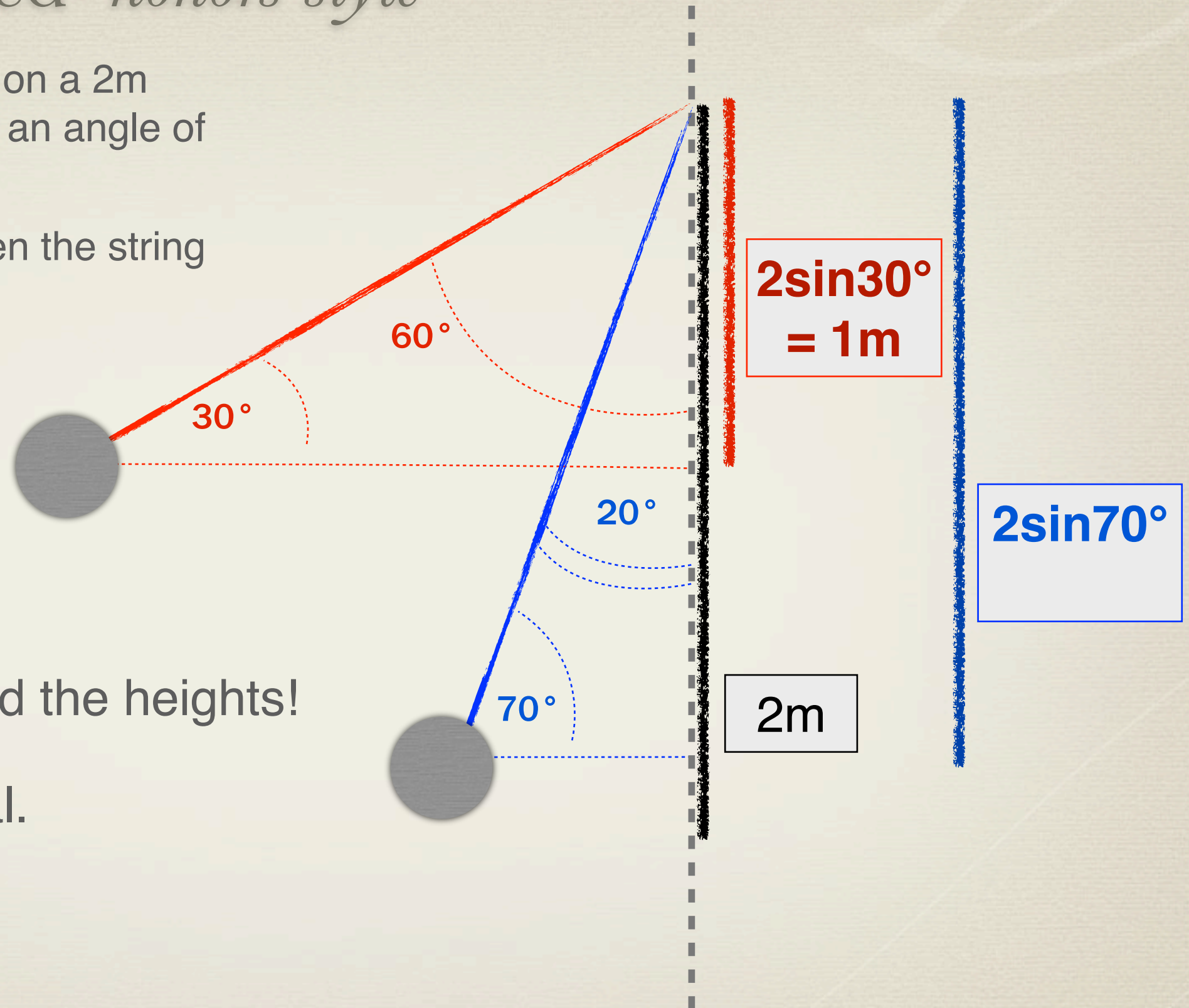
60° with the vertical.

20° angle?

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?



So, you need to find the heights!

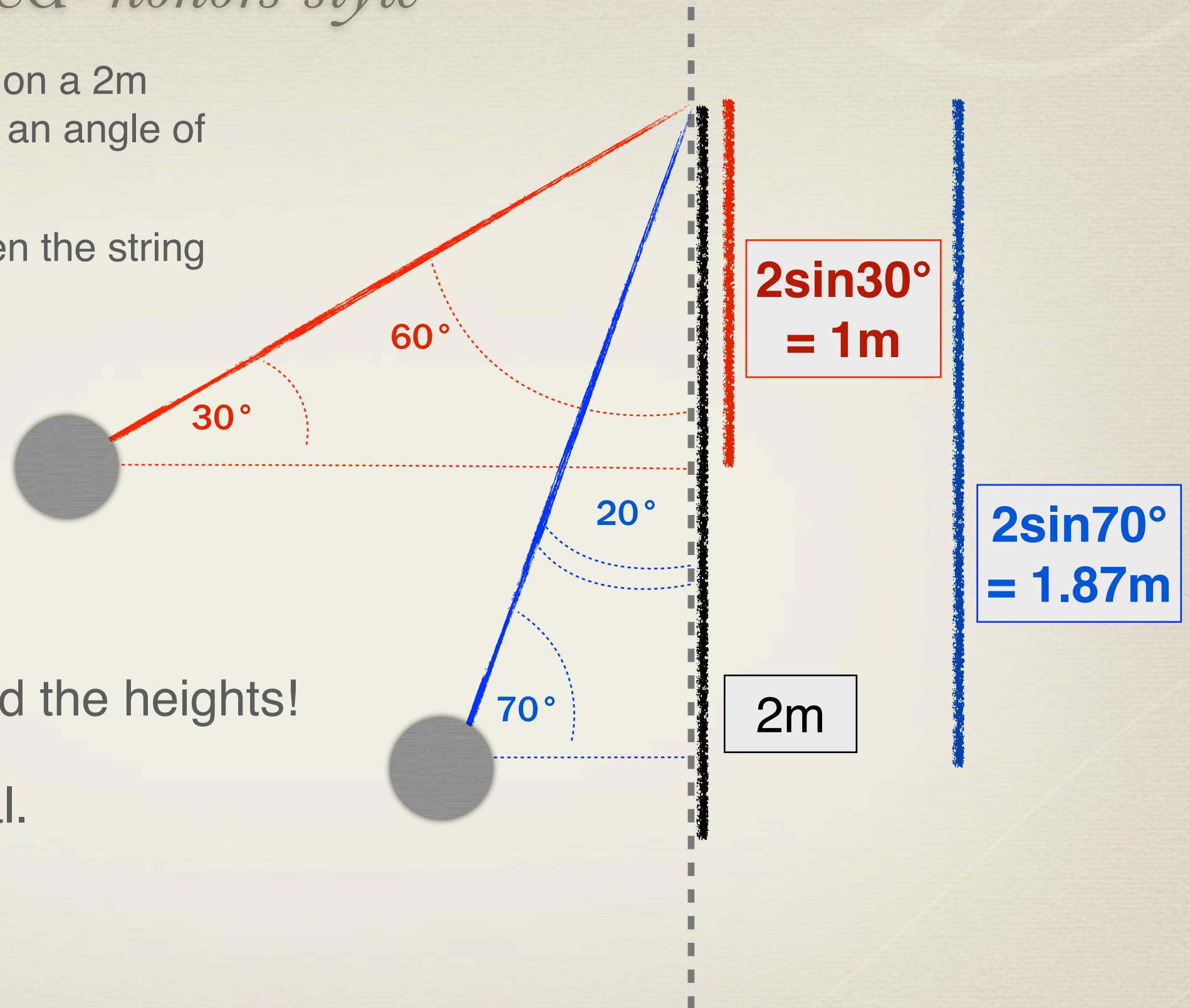
60° with the vertical.

20° angle?

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?



So, you need to find the heights!

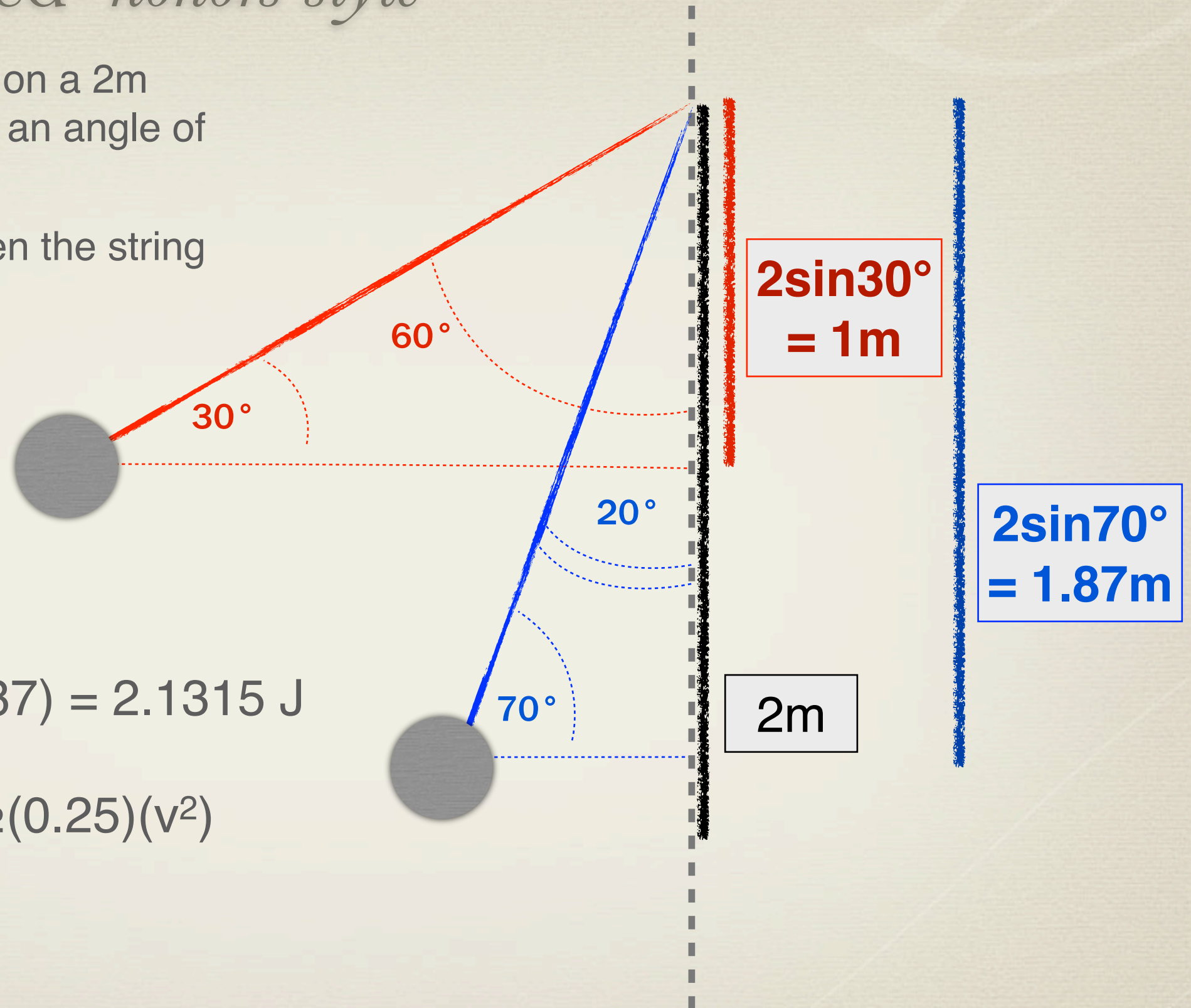
60° with the vertical.

20° angle?

Find the Speed- *honors style*

A 250g pendulum bob on a 2m string is released from an angle of 60° with the vertical.

What is the speed when the string forms a 20° angle?



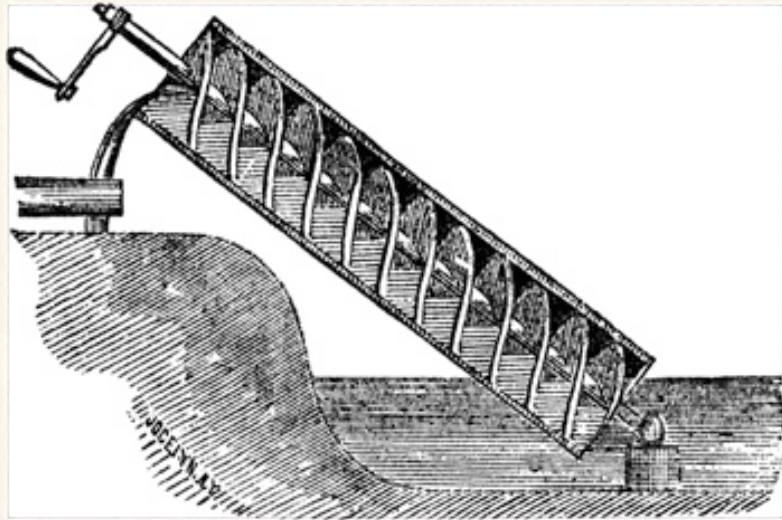
$$\text{PE} = (0.25)(9.8)(0.87) = 2.1315 \text{ J}$$

$$\text{KE} = 2.1315 \text{ J} = \frac{1}{2}(0.25)(v^2)$$

$$v = 4.13 \text{ m/s}$$

SIMPLE MACHINES

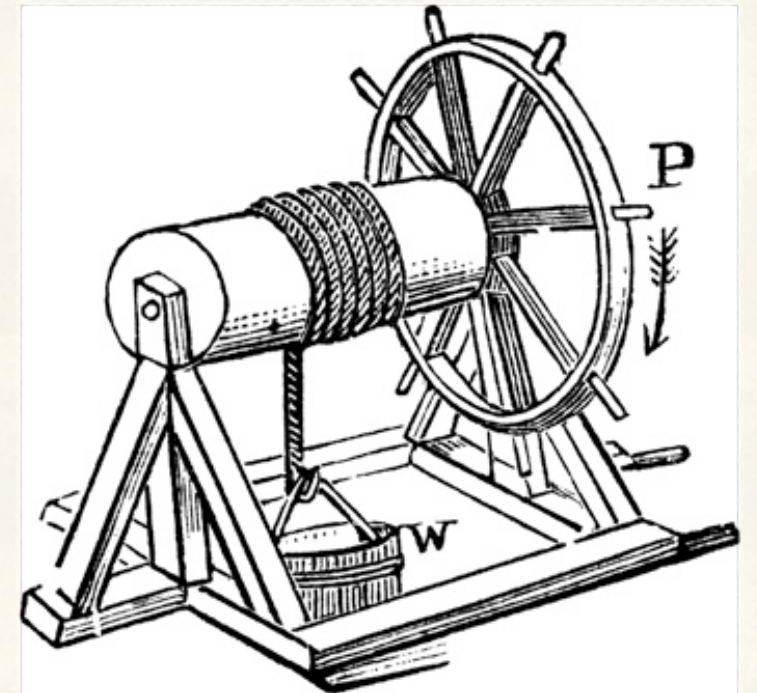
Simple Machines



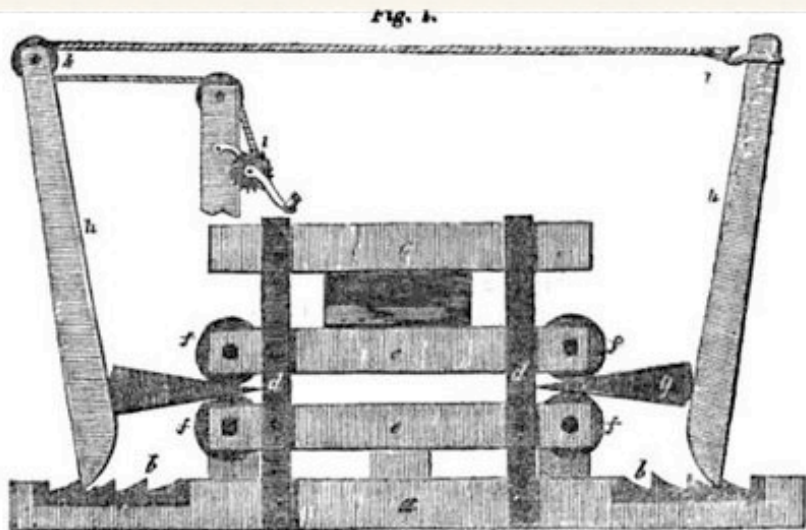
File:Archimedes screw.JPG - Wikimedia Foundation



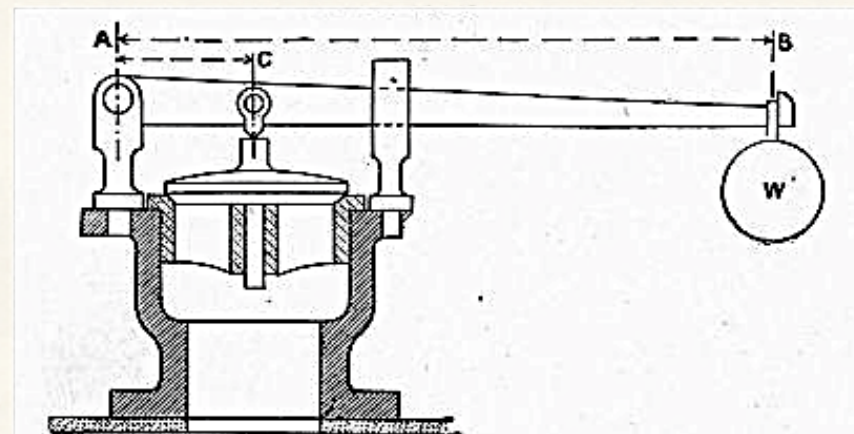
File:Opfindelsernes bog3 figo43.png - Wikimedia Foundation



File:Wheelaxle quackenbos.gif - Wikimedia Foundation



File:19th century knowledge mechanisms wedge lever press.jpg - Wikimedia Foundation



File:Lever safety valve (Heat Engines, 1913).jpg - Wikimedia Foundation

Simple Machines

Simple Machines

- ▶ IMA - the Ideal Mechanical Advantage
 - ▶ based on the geometry of the system

Simple Machines

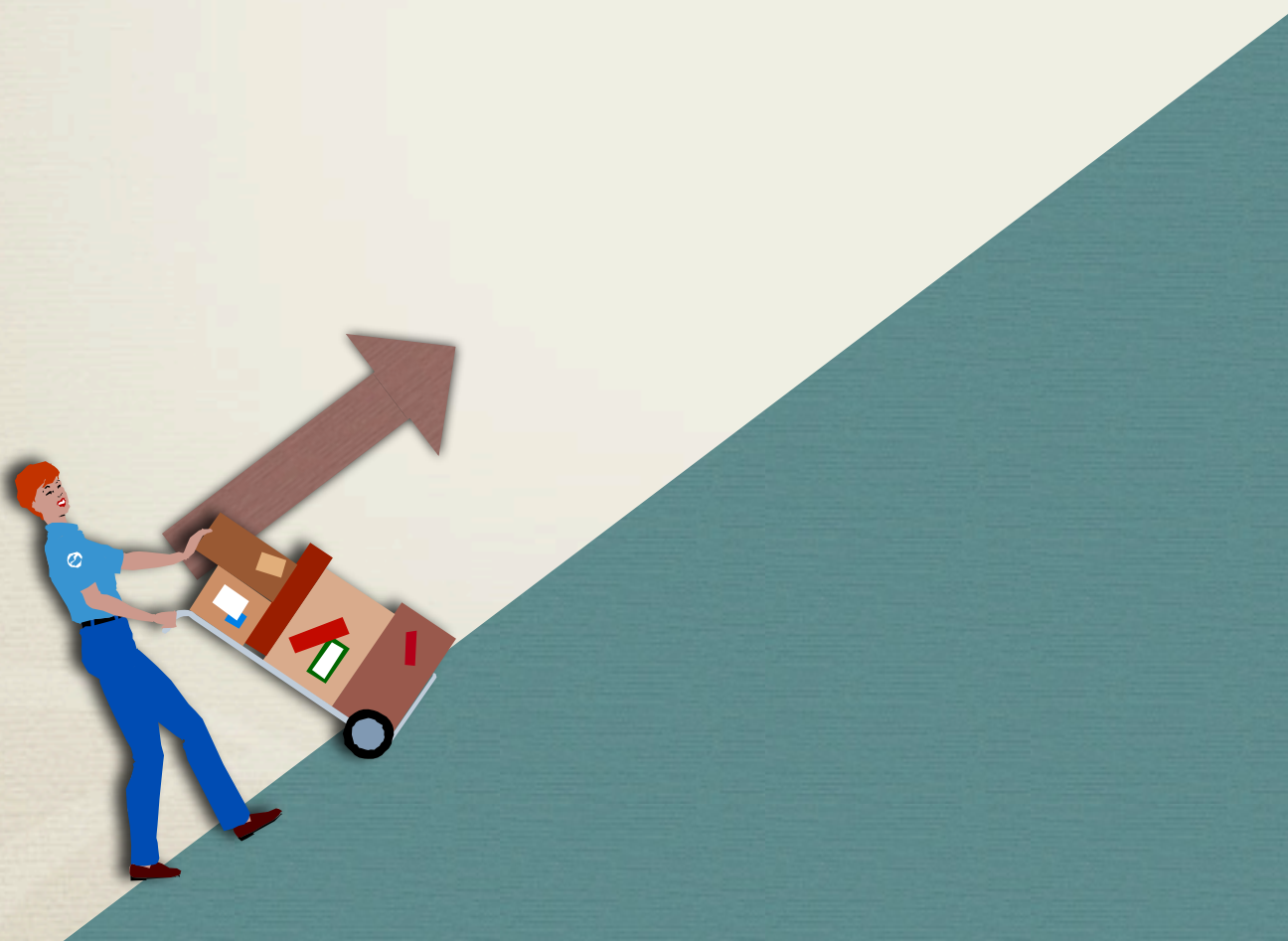
- ▶ IMA - the Ideal Mechanical Advantage
 - ▶ based on the geometry of the system
- ▶ AMA - the Actual Mechanical Advantage
 - ▶ based on the real forces used

Simple Machines

- ▶ IMA - the Ideal Mechanical Advantage
 - ▶ based on the geometry of the system
- ▶ AMA - the Actual Mechanical Advantage
 - ▶ based on the real forces used
- ▶ Efficiency = Work Output / Work Input
 - ▶ Efficiency = $W_o / W_i = AMA / IMA$

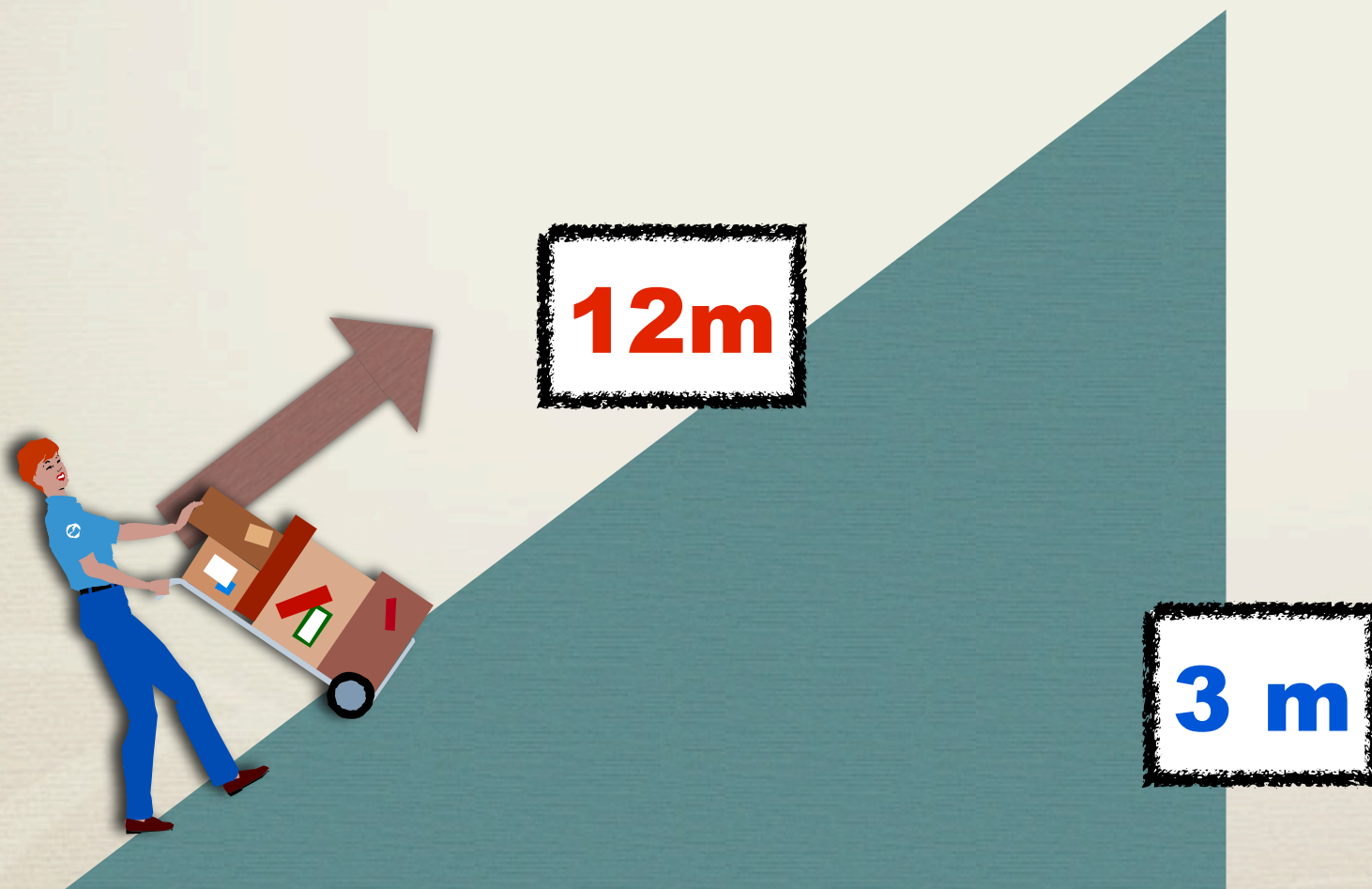
Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



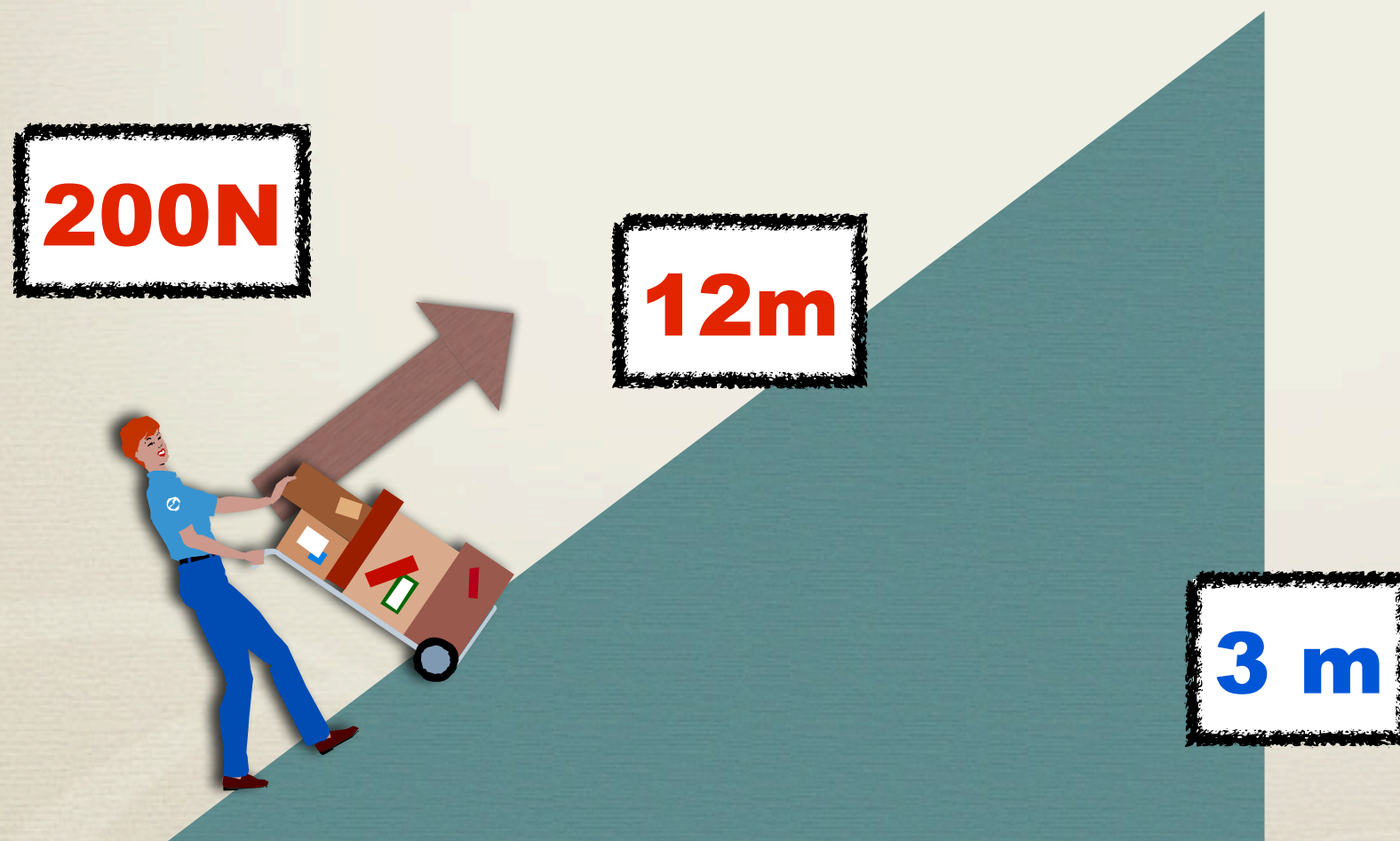
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Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



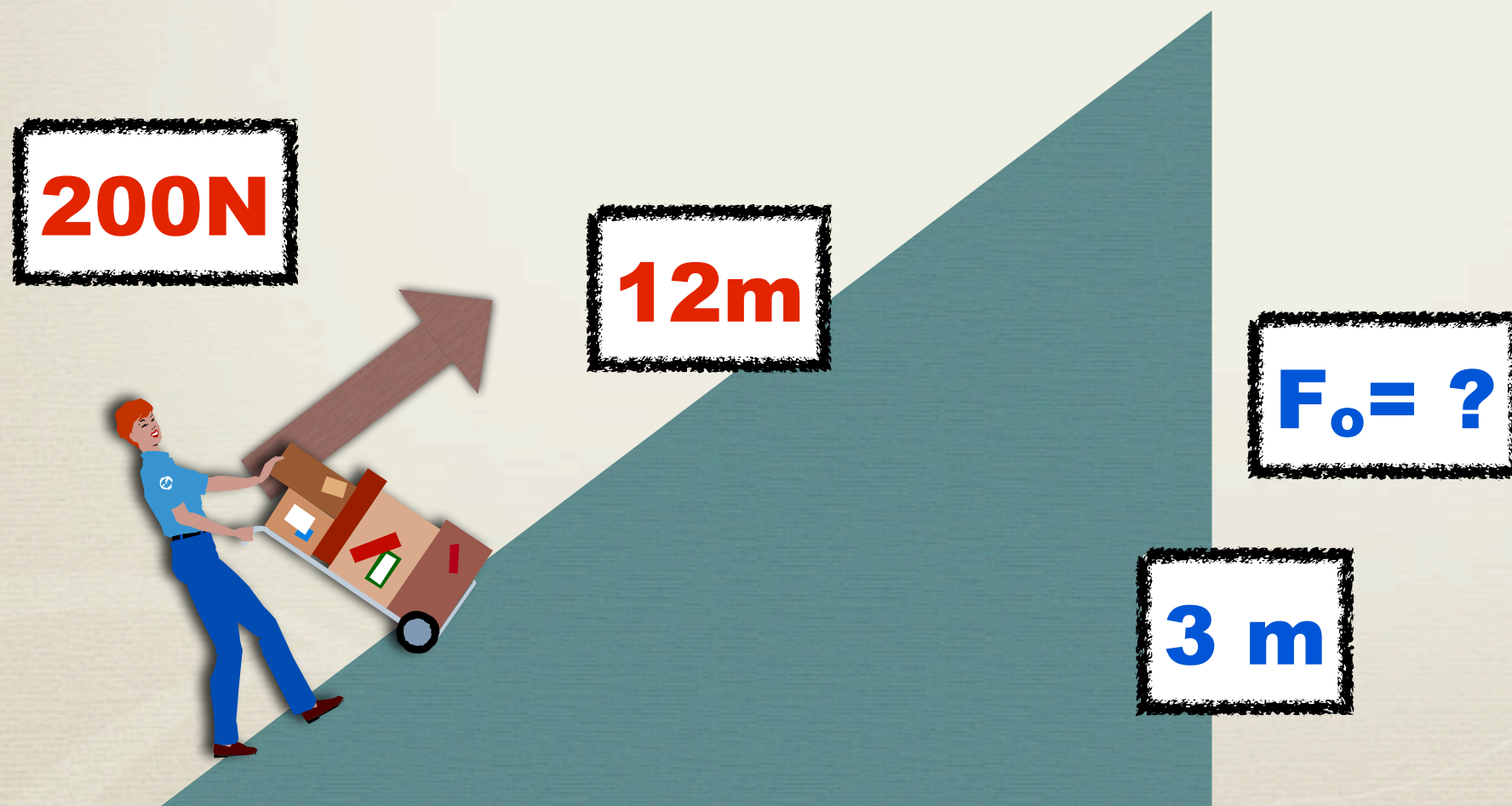
Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



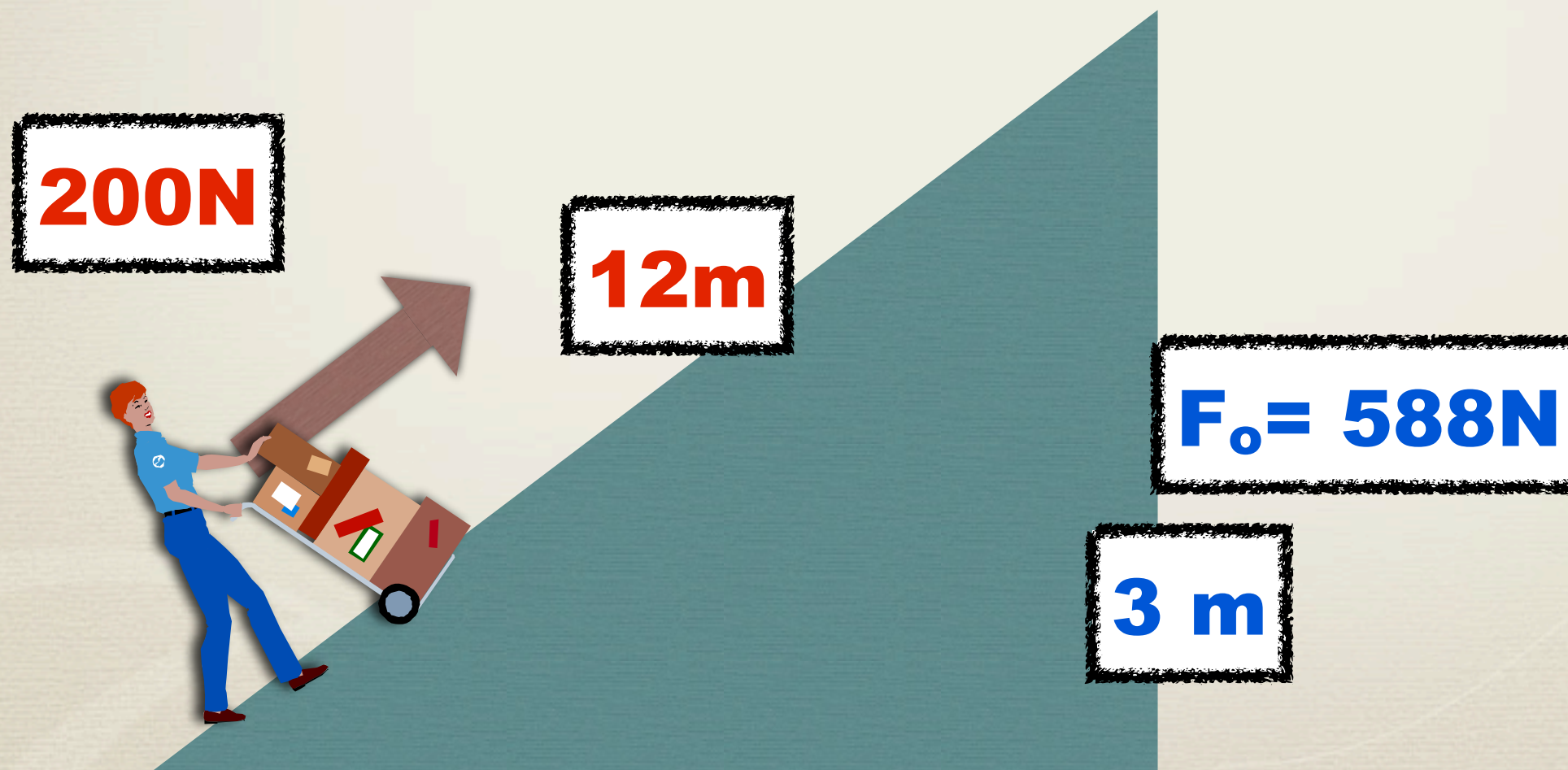
Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



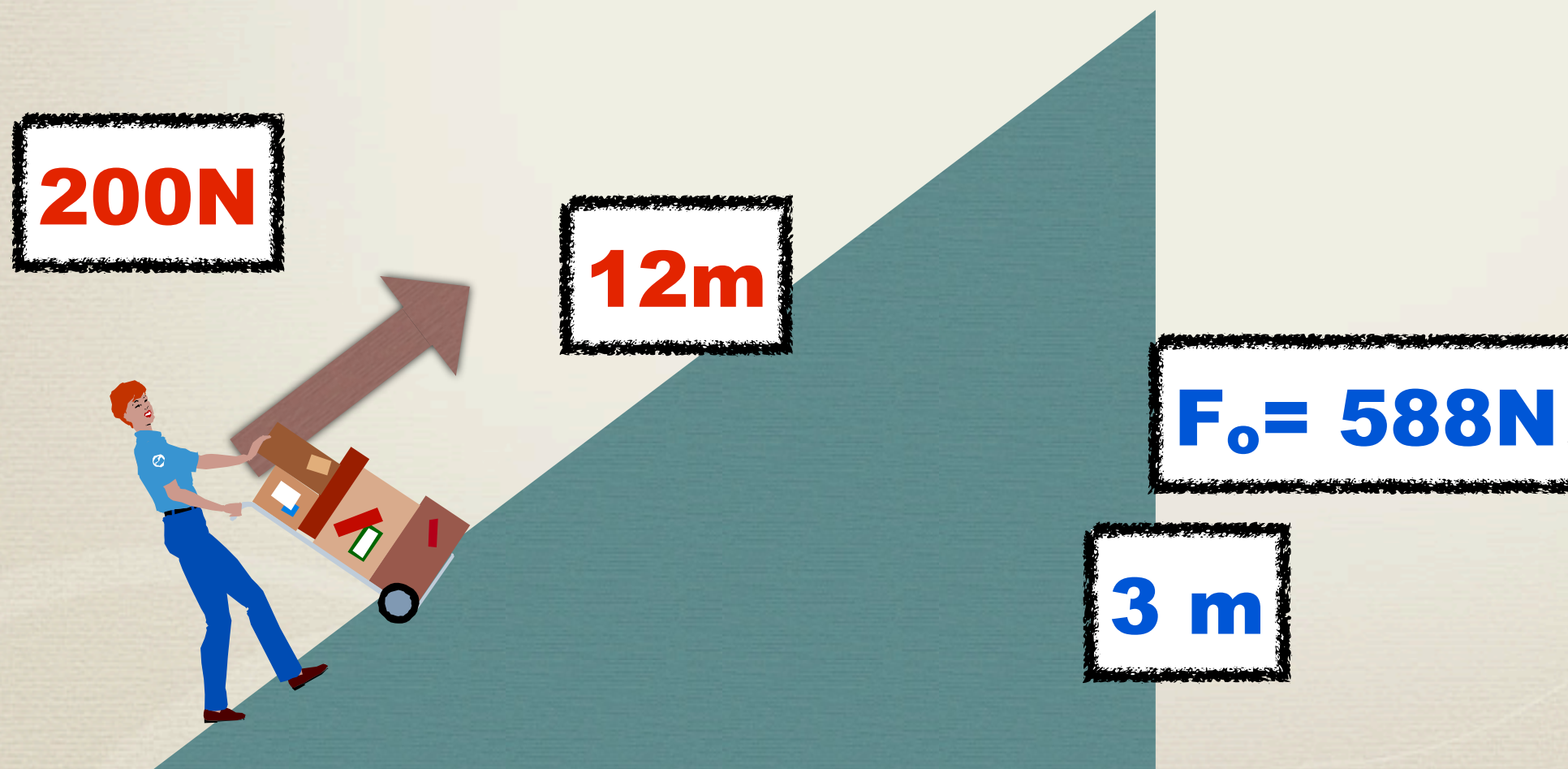
Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

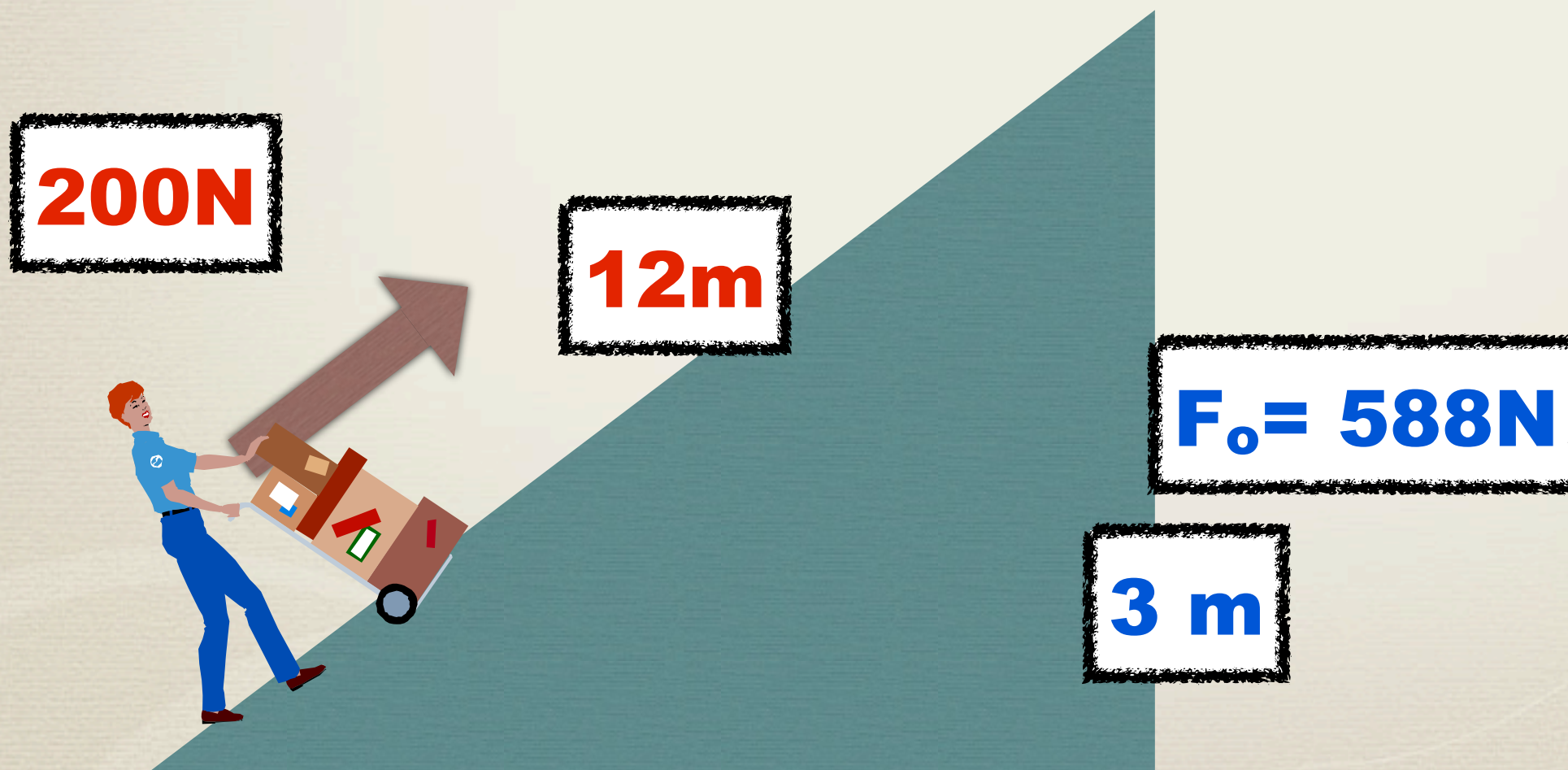
Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



$$W_i = F d$$

Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

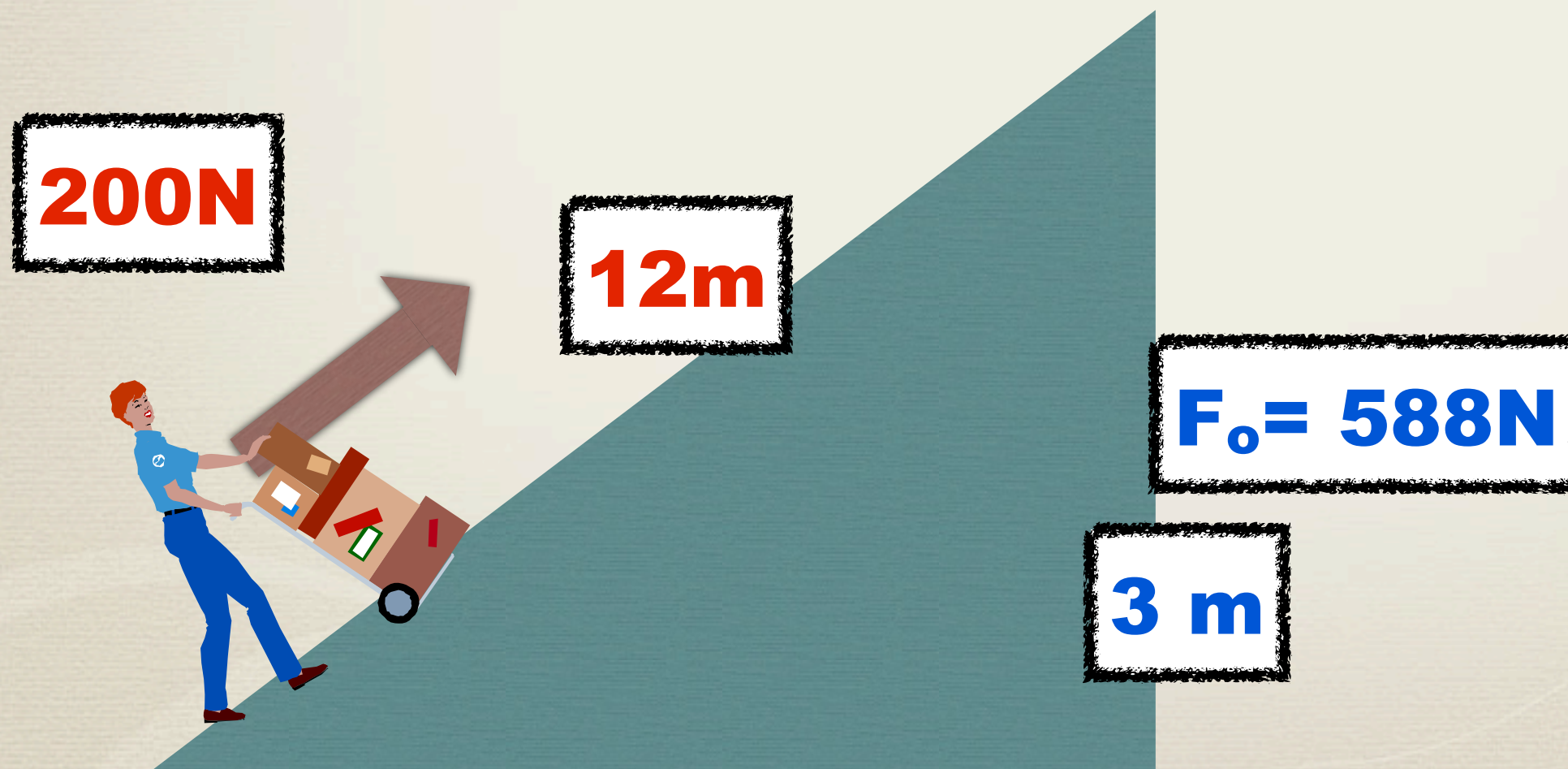
Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

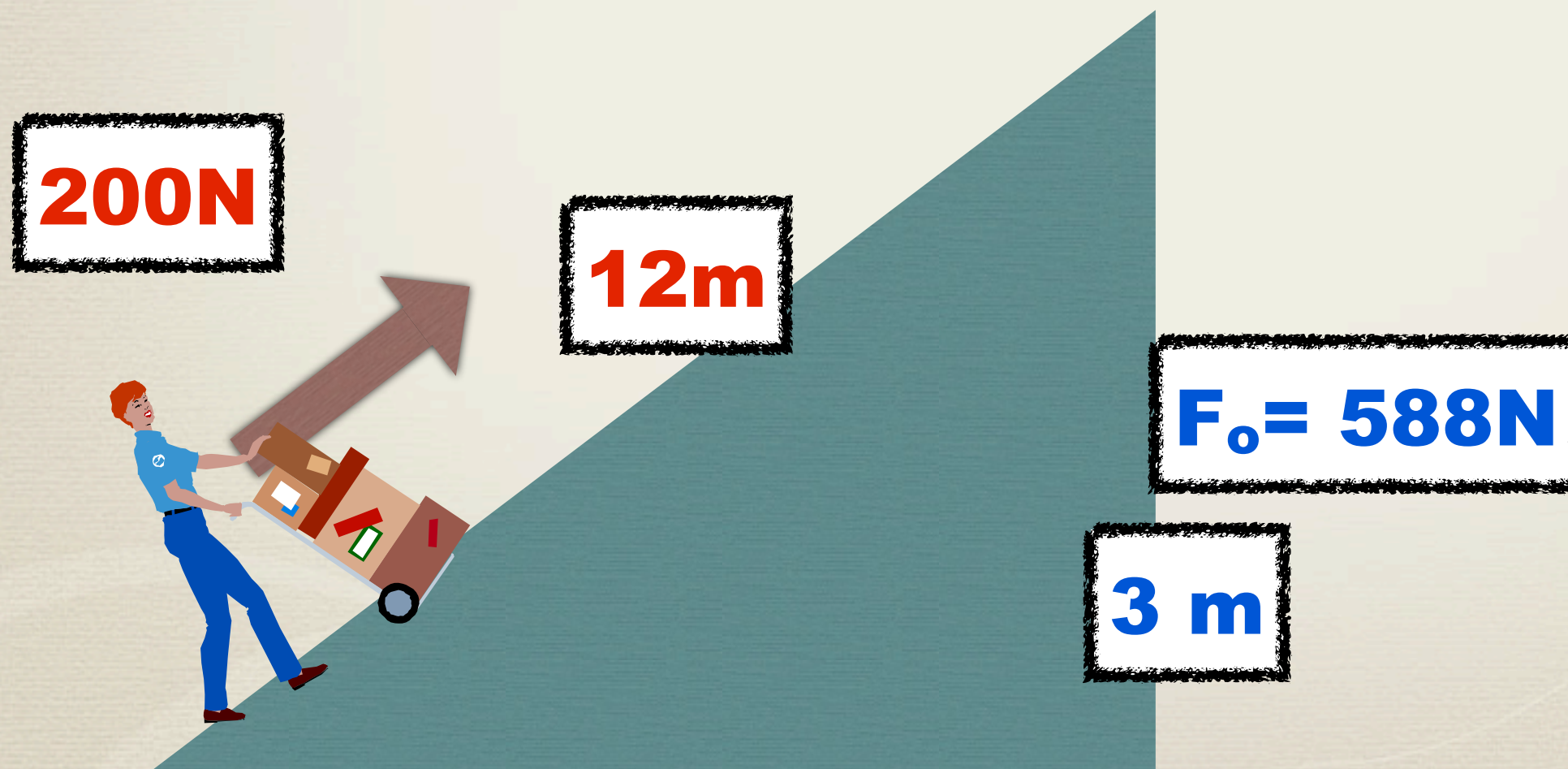
$$W_i = F d$$
$$W_i = (200 \text{ N}) (12 \text{ m})$$



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$W_i = F d$$
$$W_i = (200 \text{ N}) (12\text{m})$$
$$W_i = 2400 \text{ J}$$



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$W_i = F d$$
$$W_i = (200 \text{ N}) (12\text{m})$$
$$W_i = 2400 \text{ J}$$

$$W_o = F d$$

200N

12m

$F_o = 588\text{N}$

3 m

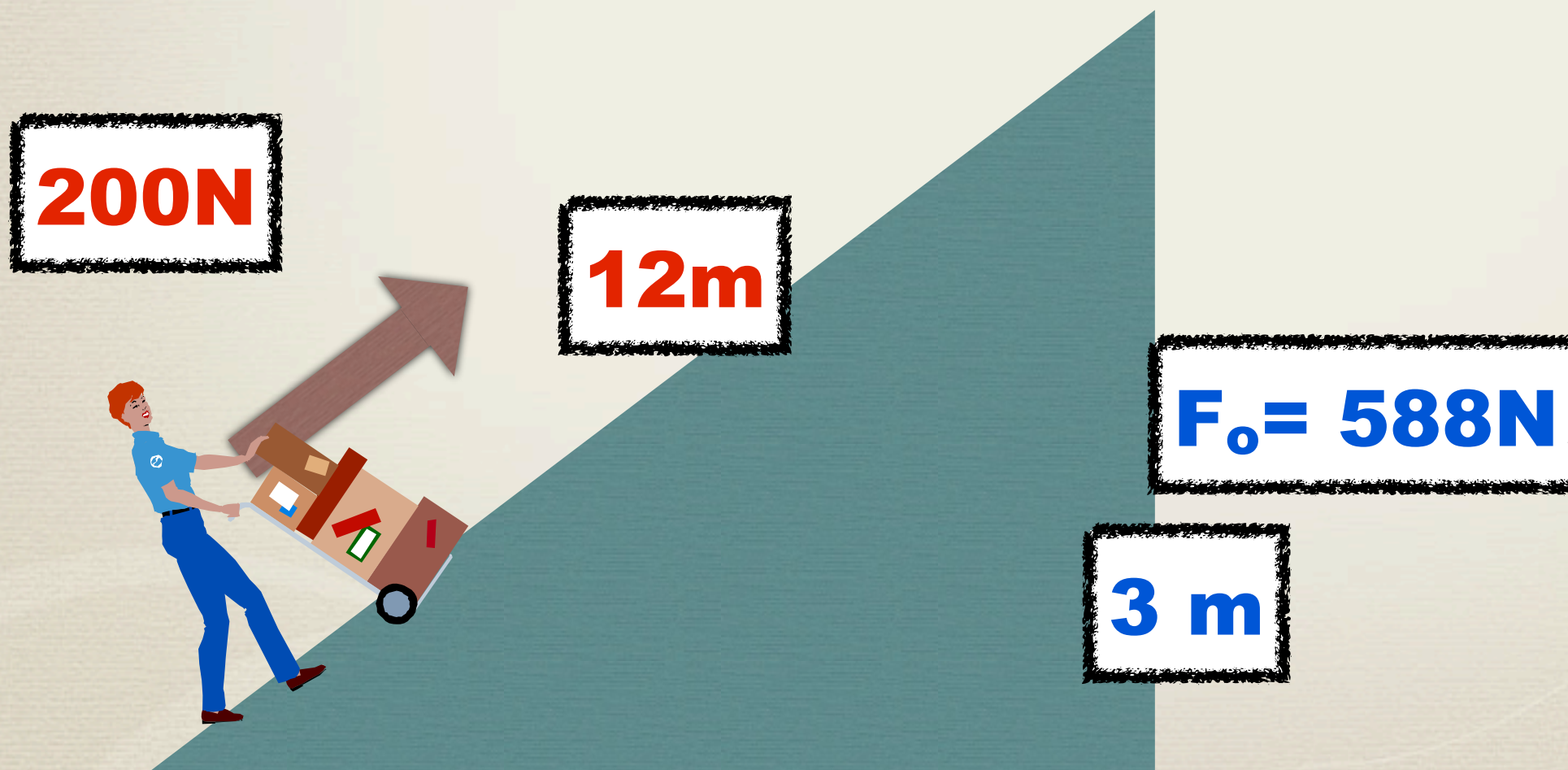


Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$W_i = F d$$
$$W_i = (200 \text{ N}) (12\text{m})$$
$$W_i = 2400 \text{ J}$$

$$W_o = F d$$
$$W_o = (588 \text{ N}) (3\text{m})$$



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$W_i = F d$$
$$W_i = (200 \text{ N}) (12\text{m})$$
$$W_i = 2400 \text{ J}$$

$$W_o = F d$$
$$W_o = (588 \text{ N}) (3\text{m})$$
$$W_o = 1764 \text{ J}$$

200N

12m

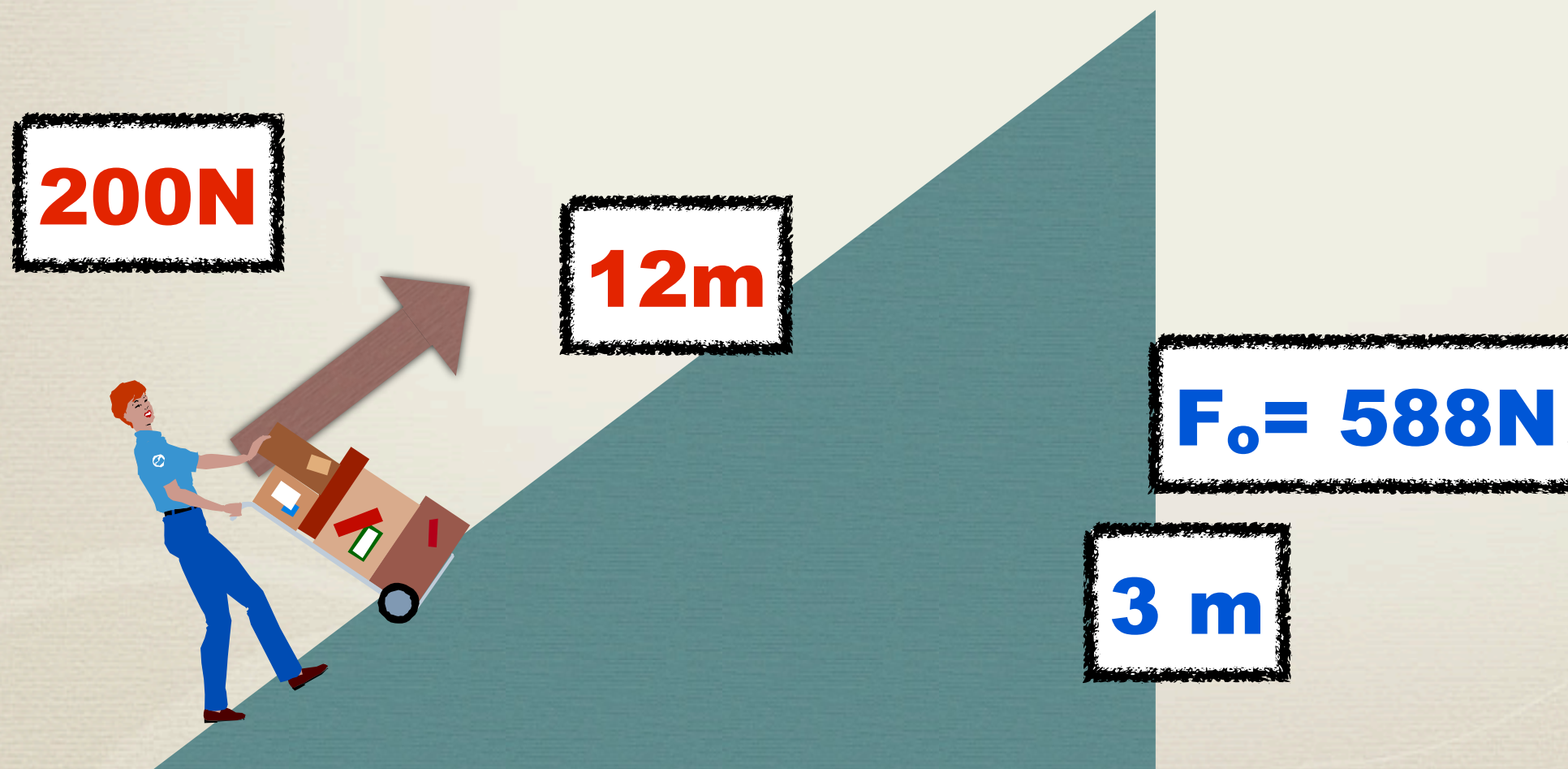
$F_o = 588\text{N}$

3 m



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

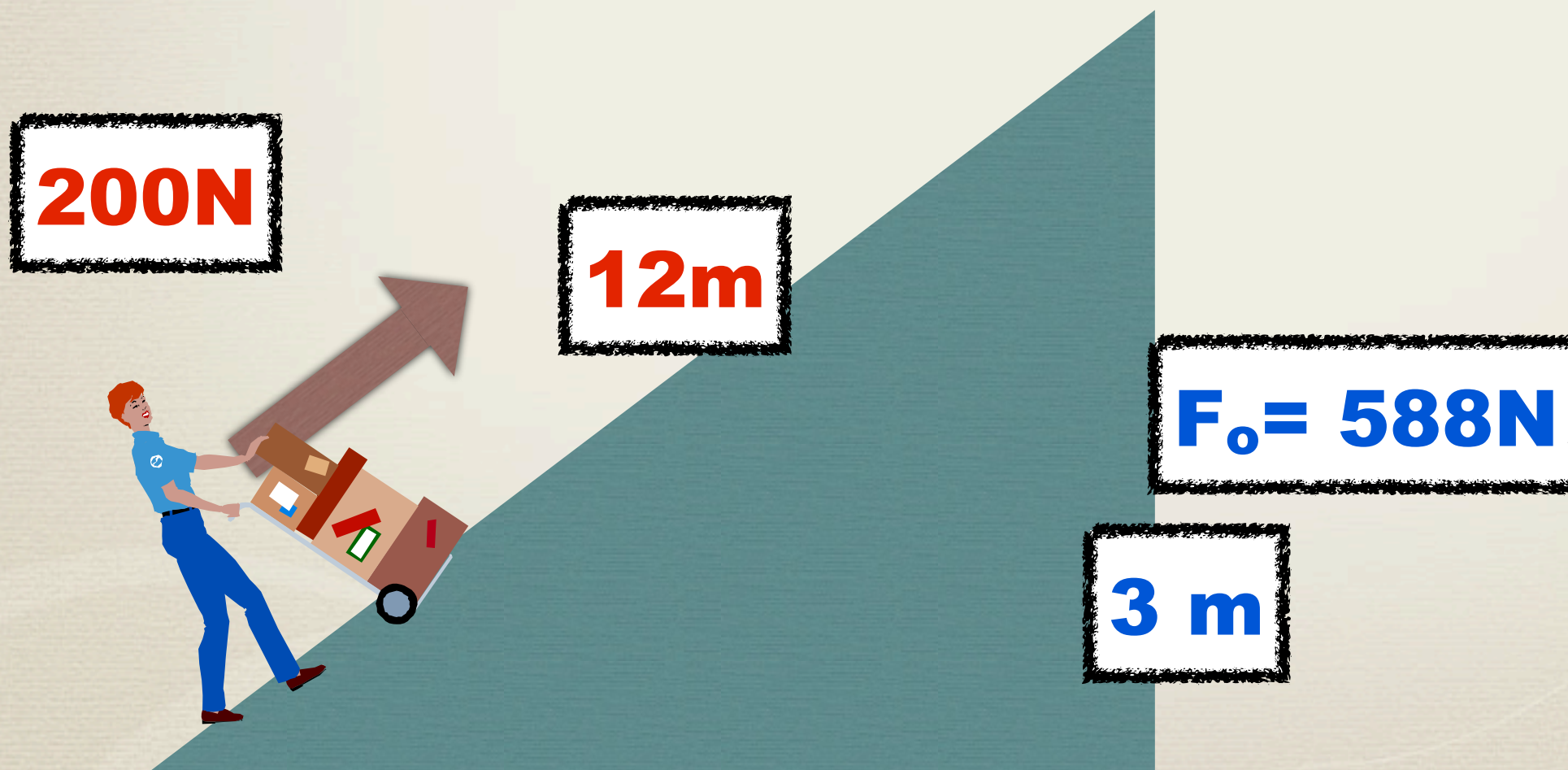
Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

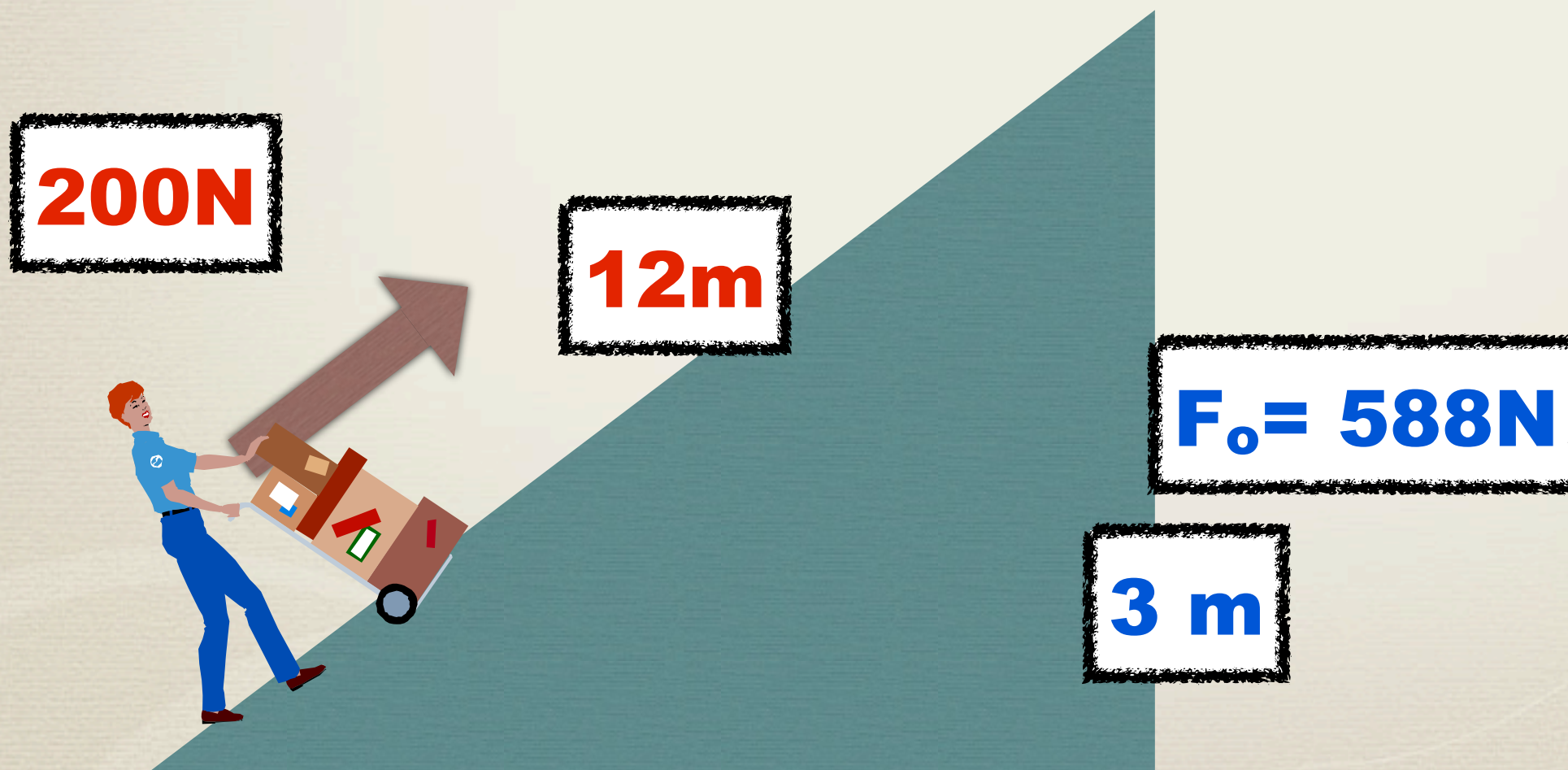
$$\text{IMA} = D_i / D_o$$



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$\text{IMA} = D_i / D_o$$
$$\text{IMA} = 12 / 3 = 4$$

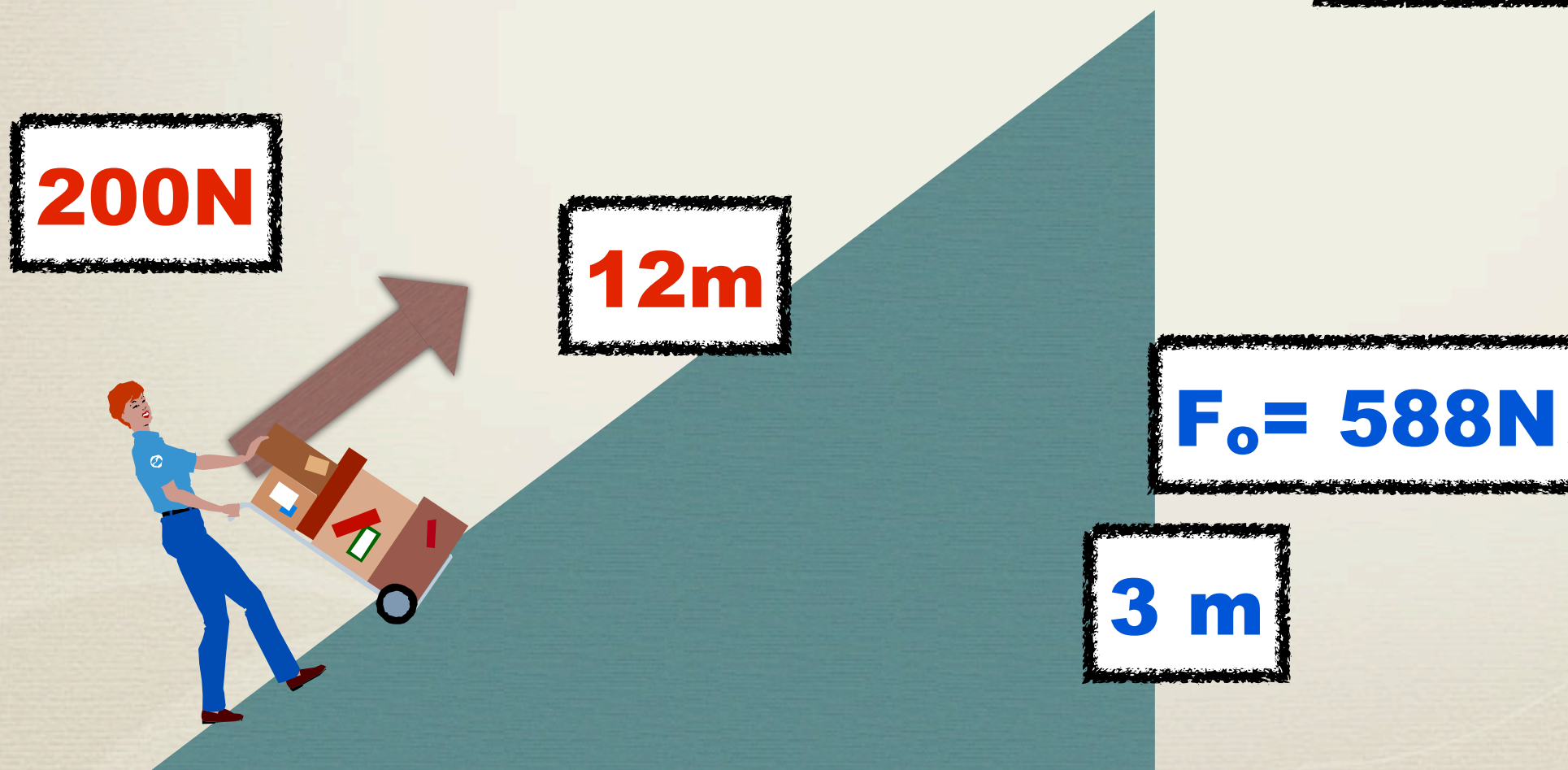


Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$\text{IMA} = D_i / D_o$$
$$\text{IMA} = 12 / 3 = 4$$

$$\text{AMA} = F_o / F_i$$

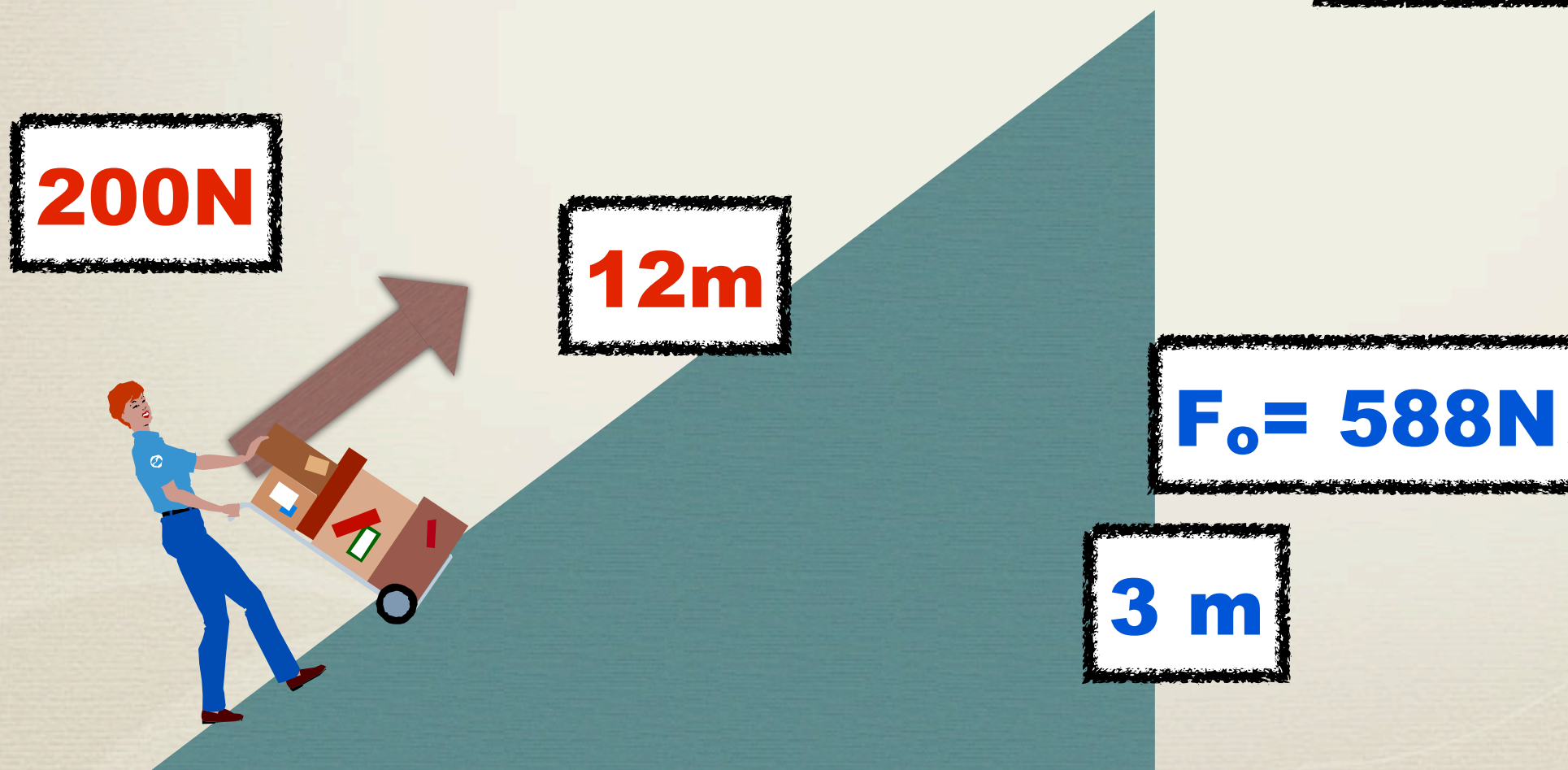


Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$\text{IMA} = D_i / D_o$$
$$\text{IMA} = 12 / 3 = 4$$

$$\text{AMA} = F_o / F_i$$
$$\text{AMA} = 588 / 200$$

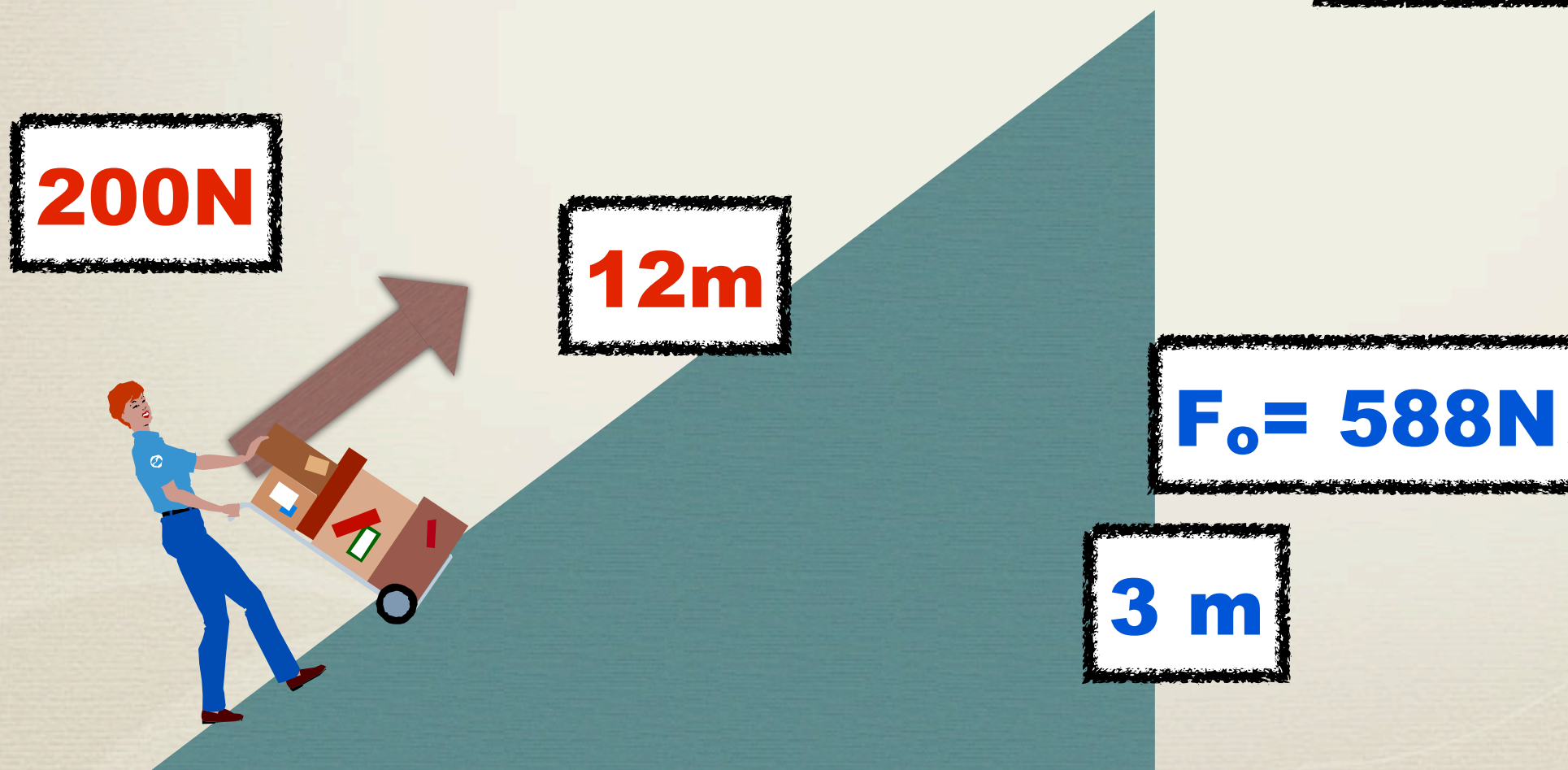


Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

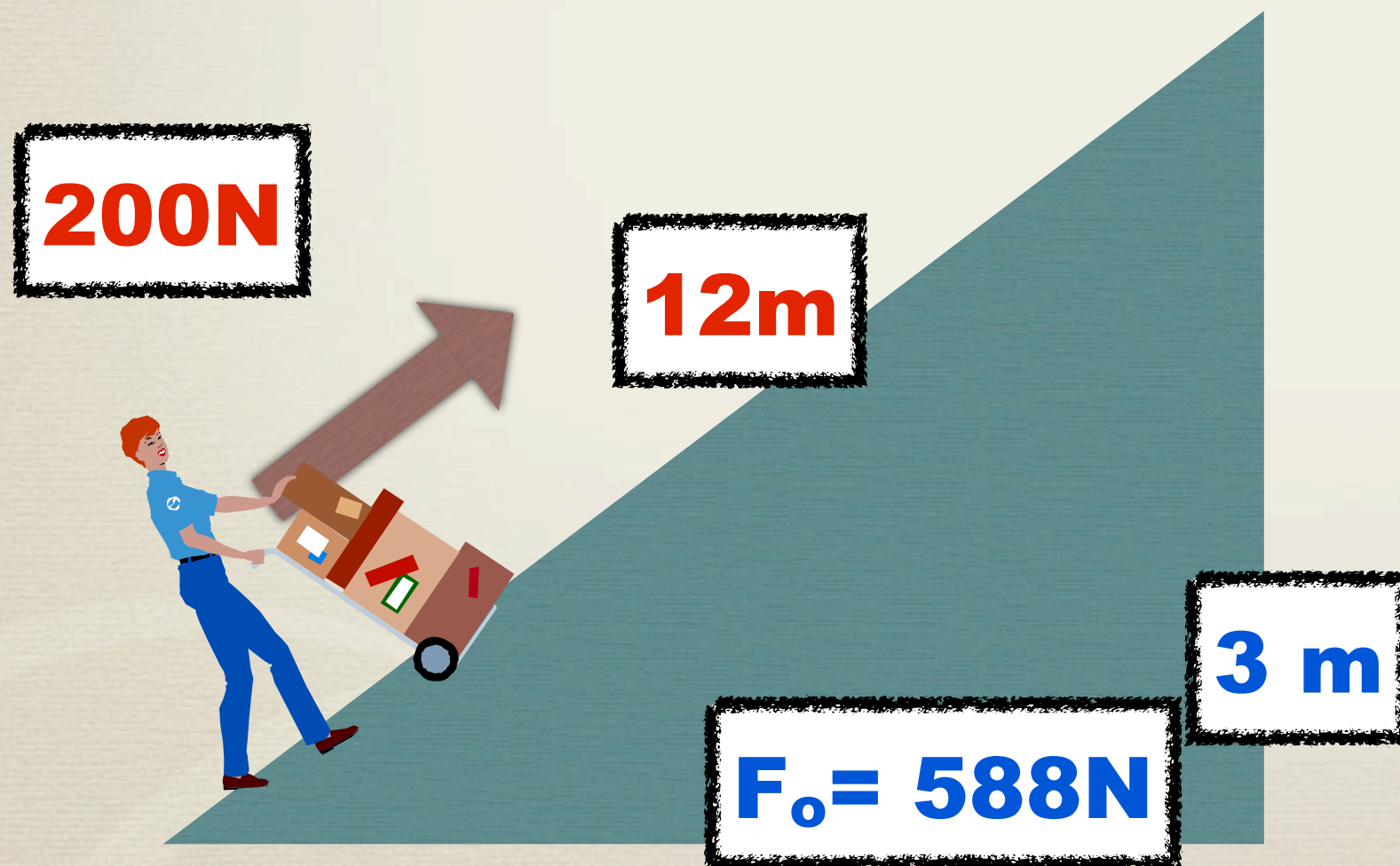
$$\text{IMA} = D_i / D_o$$
$$\text{IMA} = 12 / 3 = 4$$

$$\text{AMA} = F_o / F_i$$
$$\text{AMA} = 588 / 200$$
$$\text{AMA} = 2.94$$



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

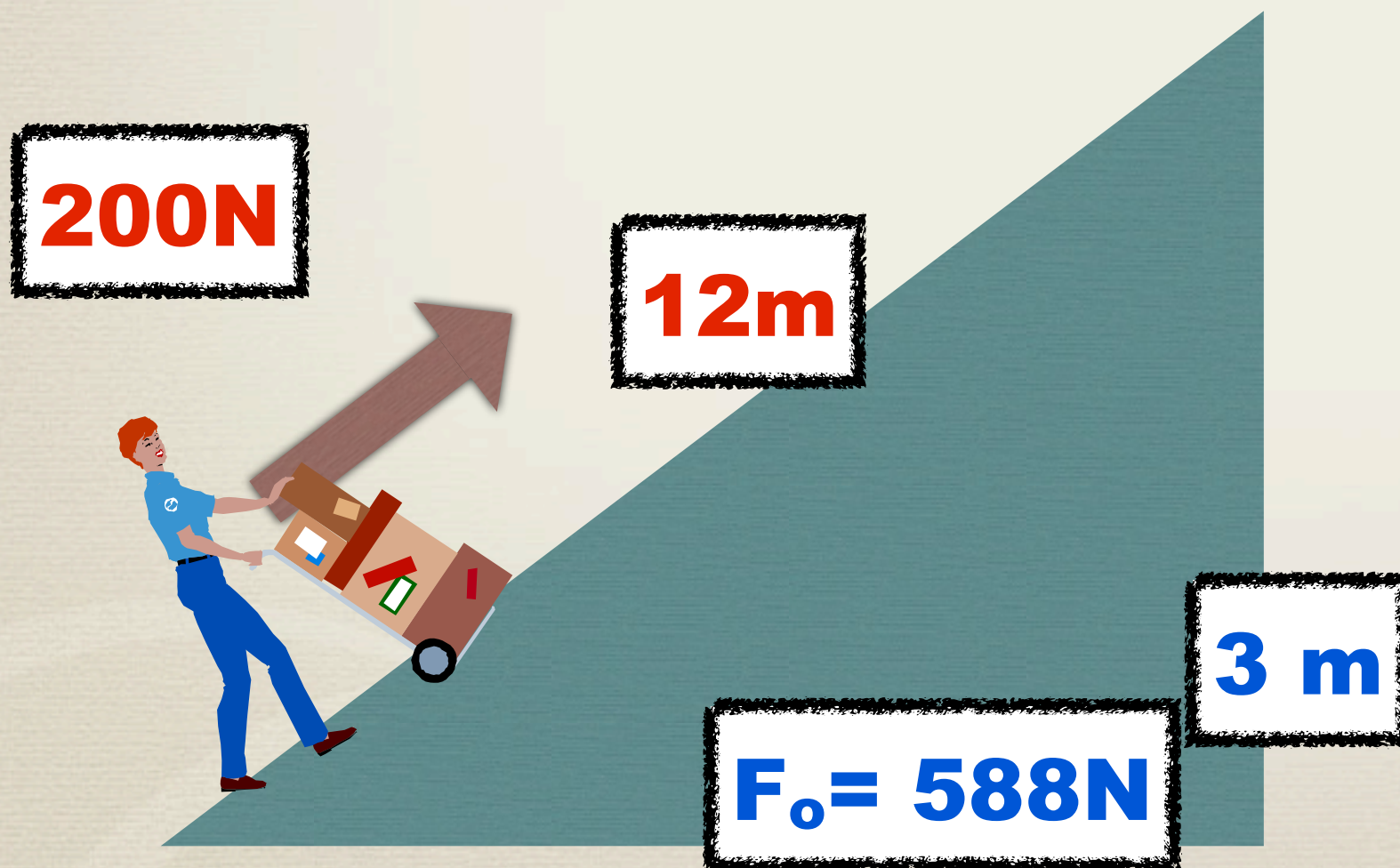
Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



Efficiency

Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

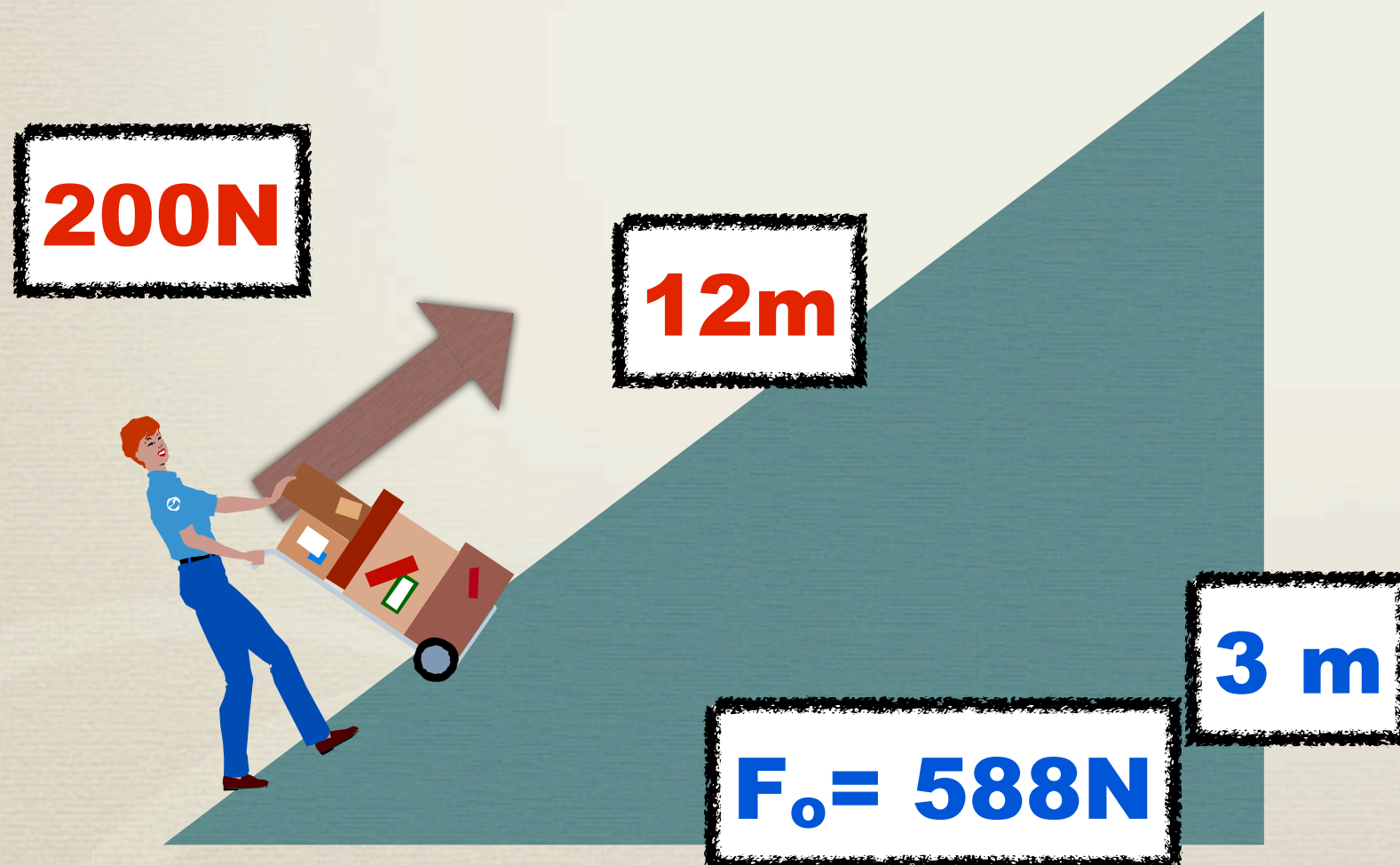
Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

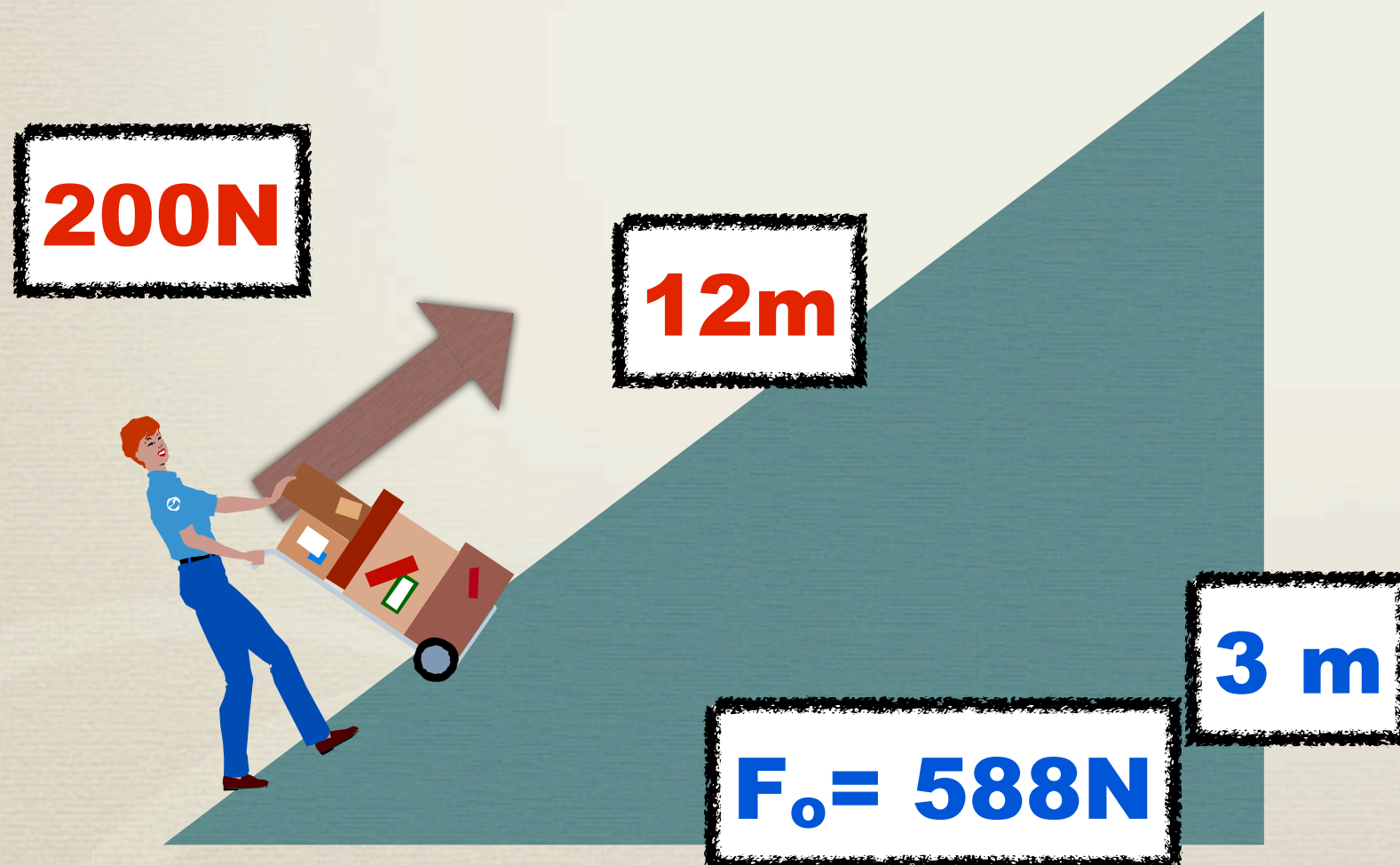
$$\text{Efficiency} = W_o / W_i$$



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

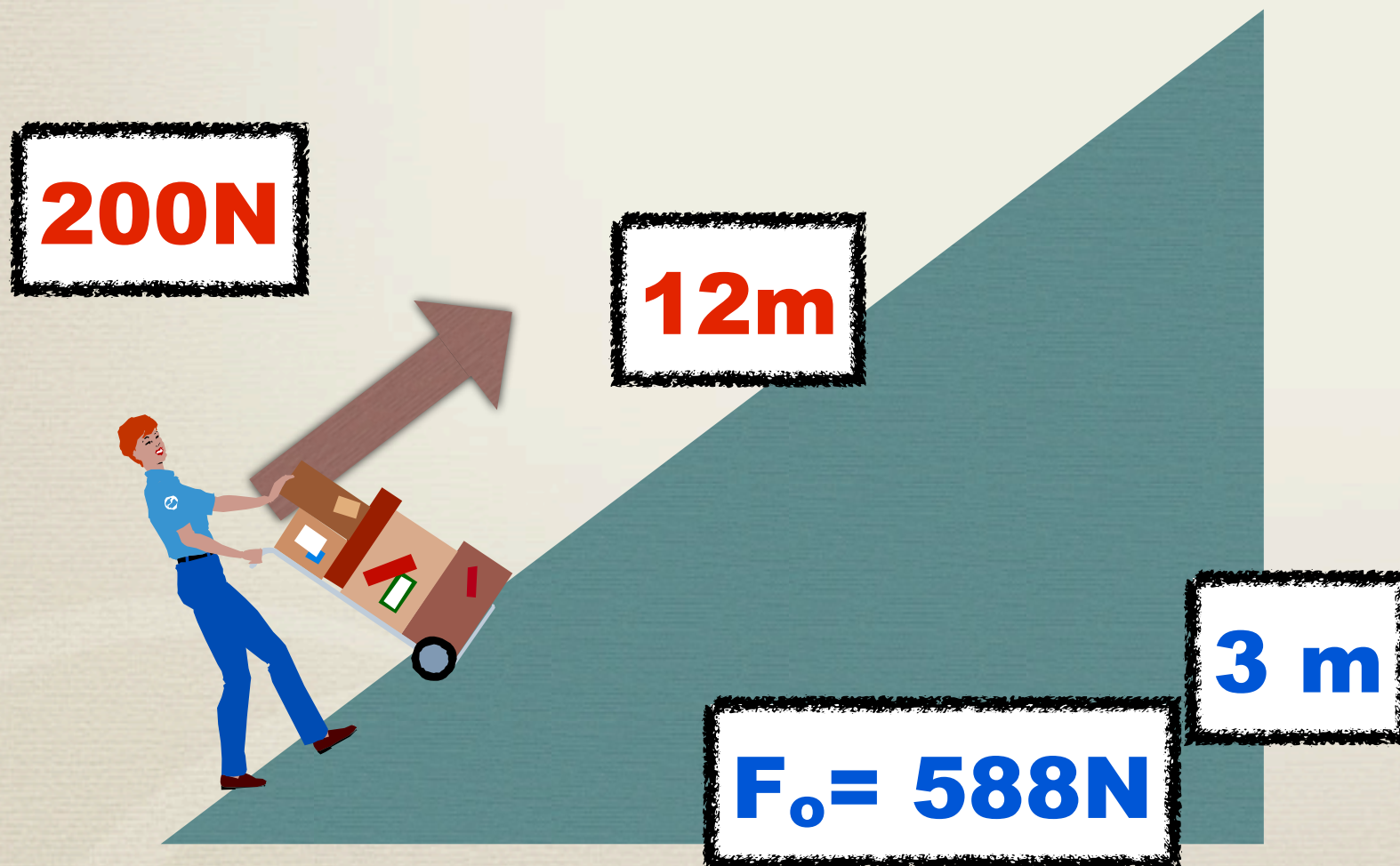
$$\begin{aligned}\text{Efficiency} &= W_o / W_i \\ &= AMA / IMA\end{aligned}$$



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$\begin{aligned}\text{Efficiency} &= W_o / W_i \\ &= AMA / IMA \\ \text{Eff} &= 73.5\%\end{aligned}$$

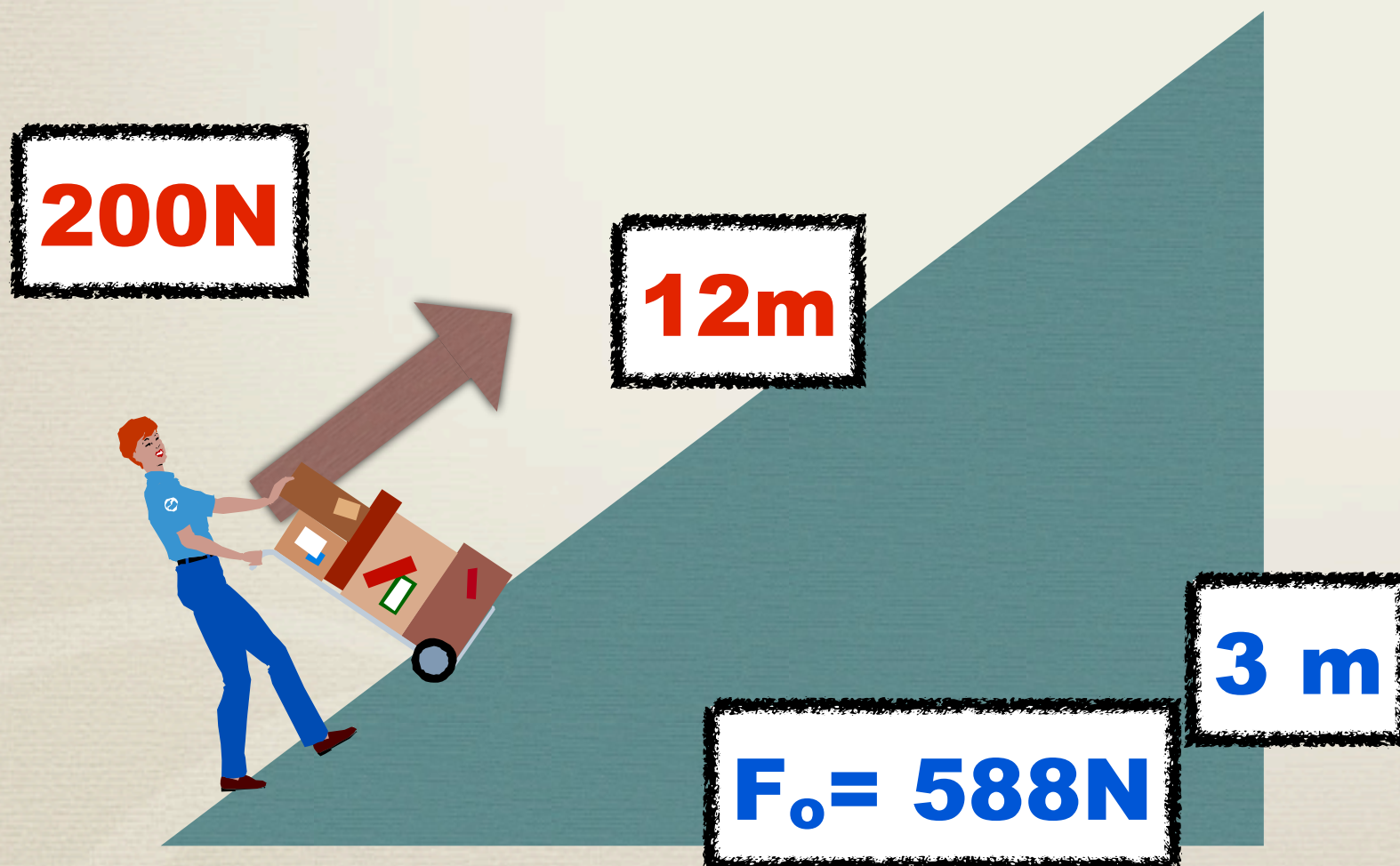


Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$\begin{aligned}\text{Efficiency} &= W_o / W_i \\ &= AMA / IMA \\ \text{Eff} &= 73.5\%\end{aligned}$$

Lost Energy to Friction

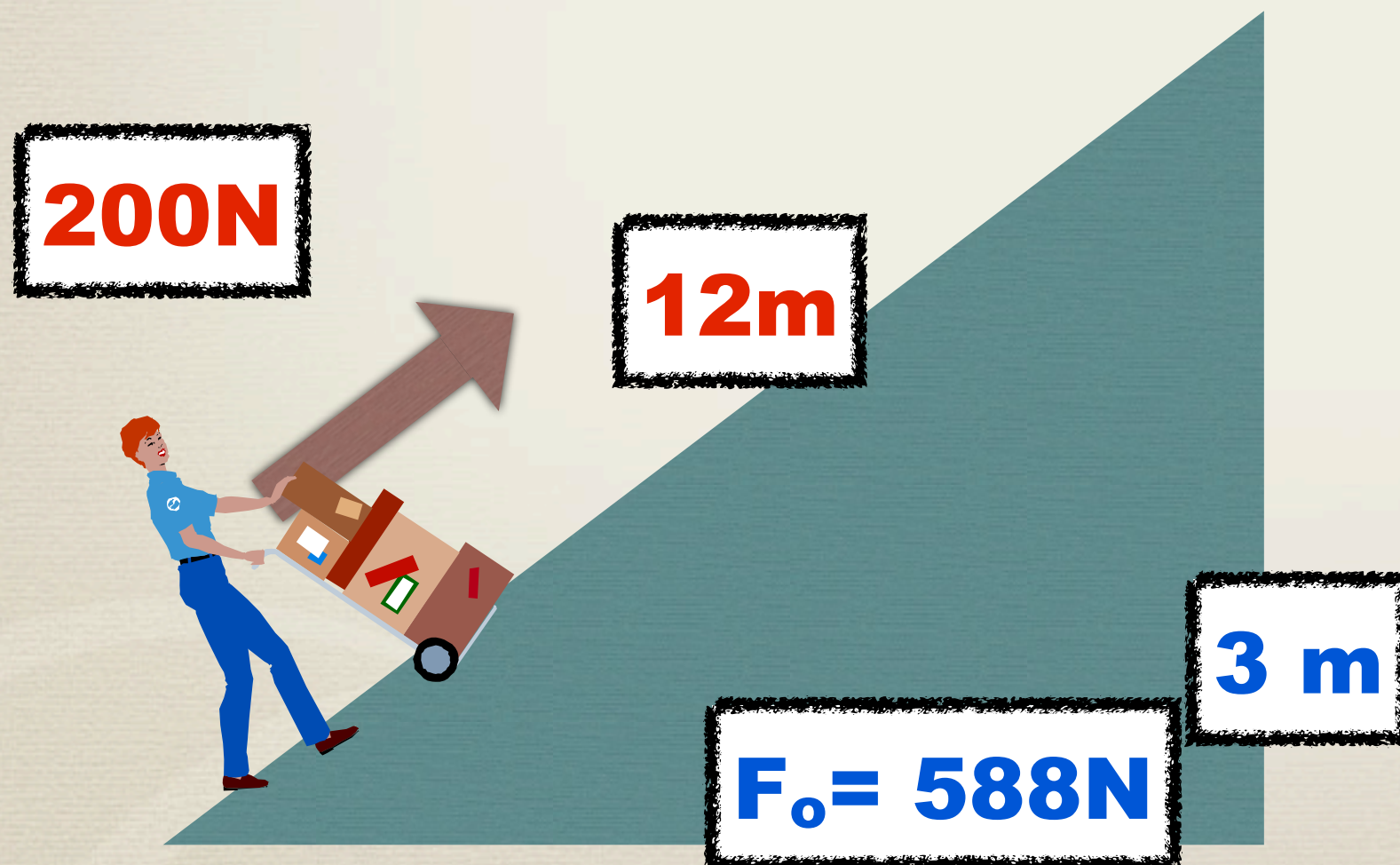


Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

$$\begin{aligned}\text{Efficiency} &= W_o / W_i \\ &= AMA / IMA \\ \text{Eff} &= 73.5\%\end{aligned}$$

$$\begin{aligned}\text{Lost Energy to Friction} \\ 2400\text{J} - 1764\text{J}\end{aligned}$$

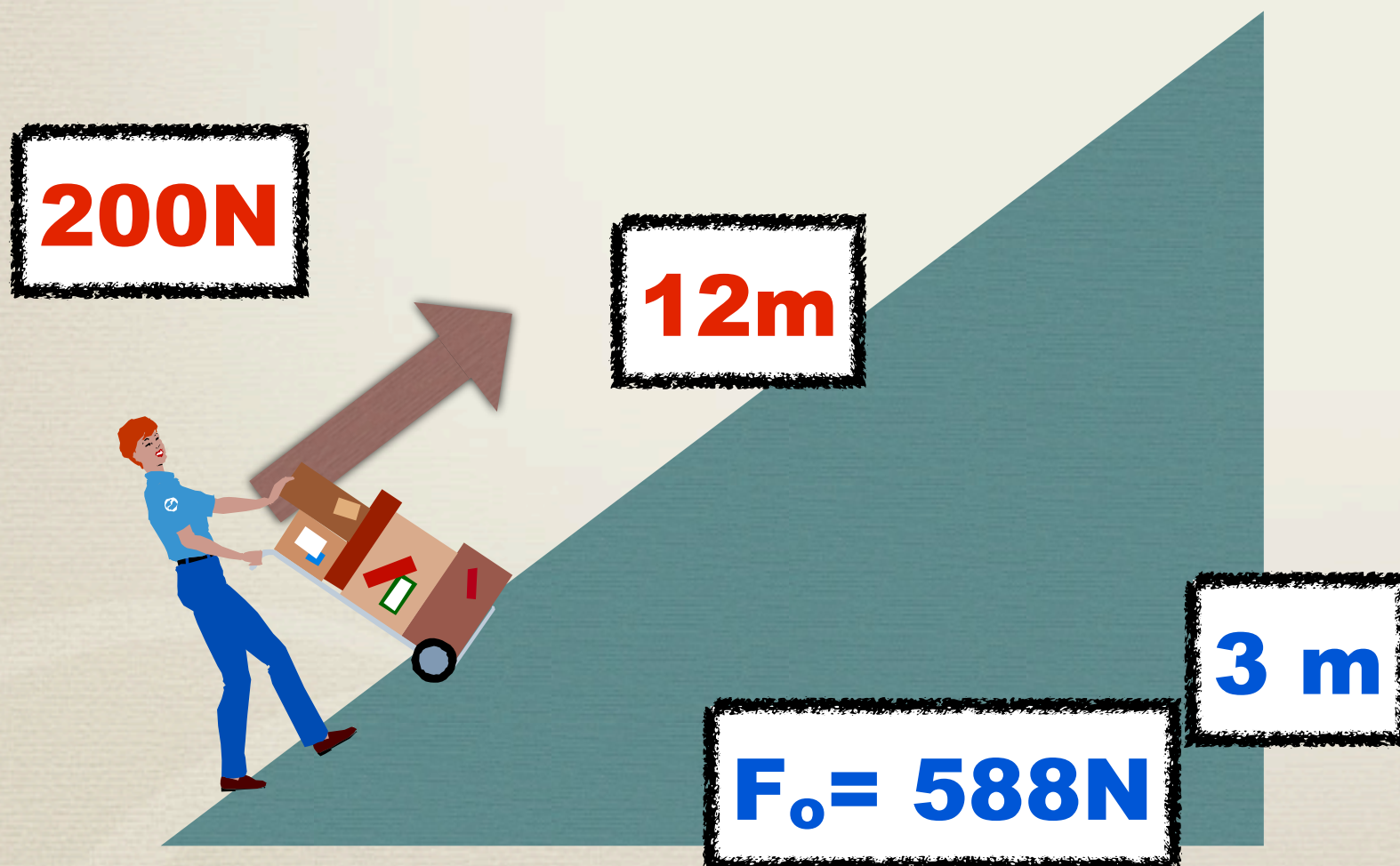


Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

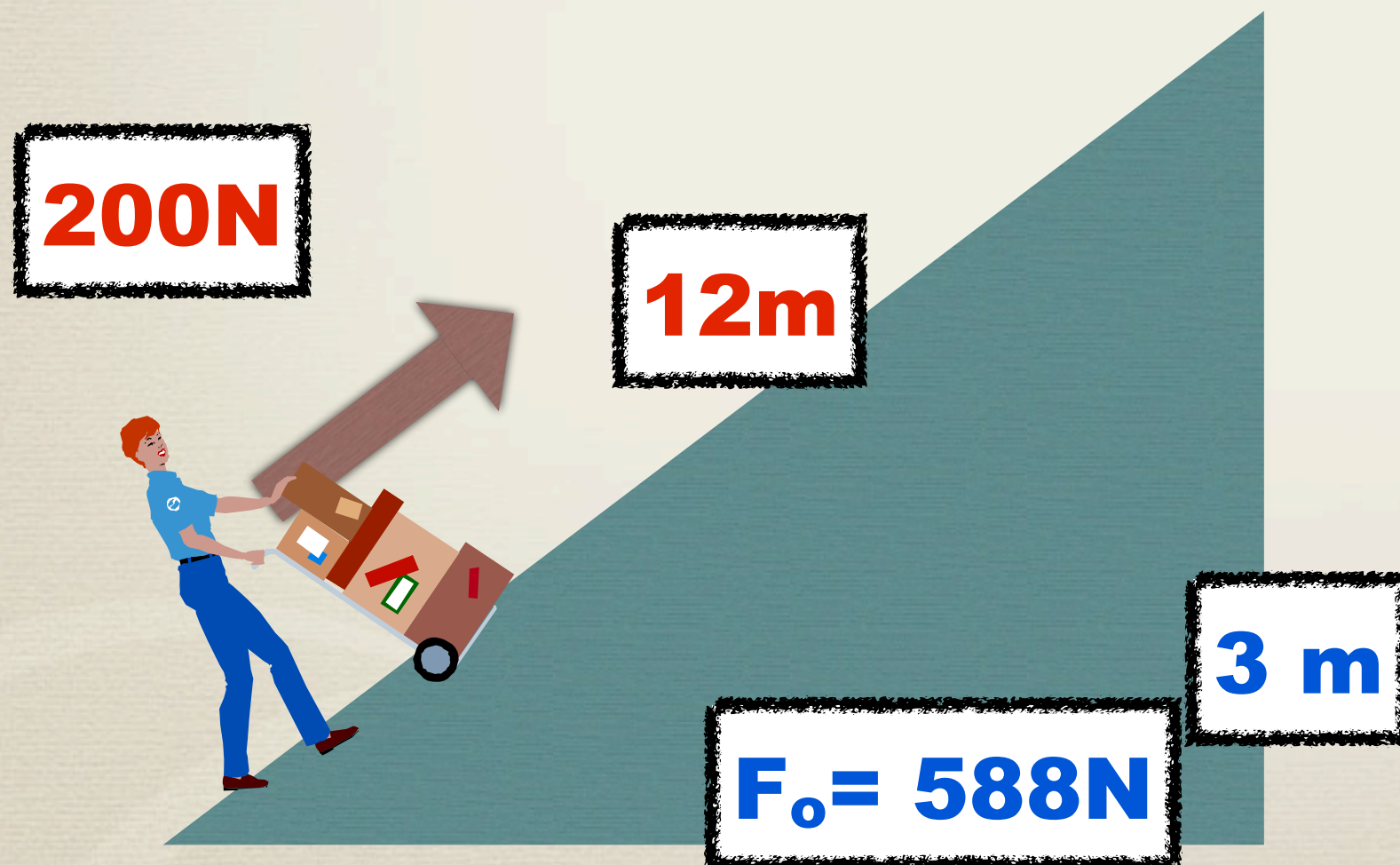
$$\begin{aligned}\text{Efficiency} &= W_o / W_i \\ &= AMA / IMA \\ \text{Eff} &= 73.5\%\end{aligned}$$

$$\begin{aligned}\text{Lost Energy to Friction} \\ 2400\text{J} - 1764\text{J} \\ 636\text{J}\end{aligned}$$



Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



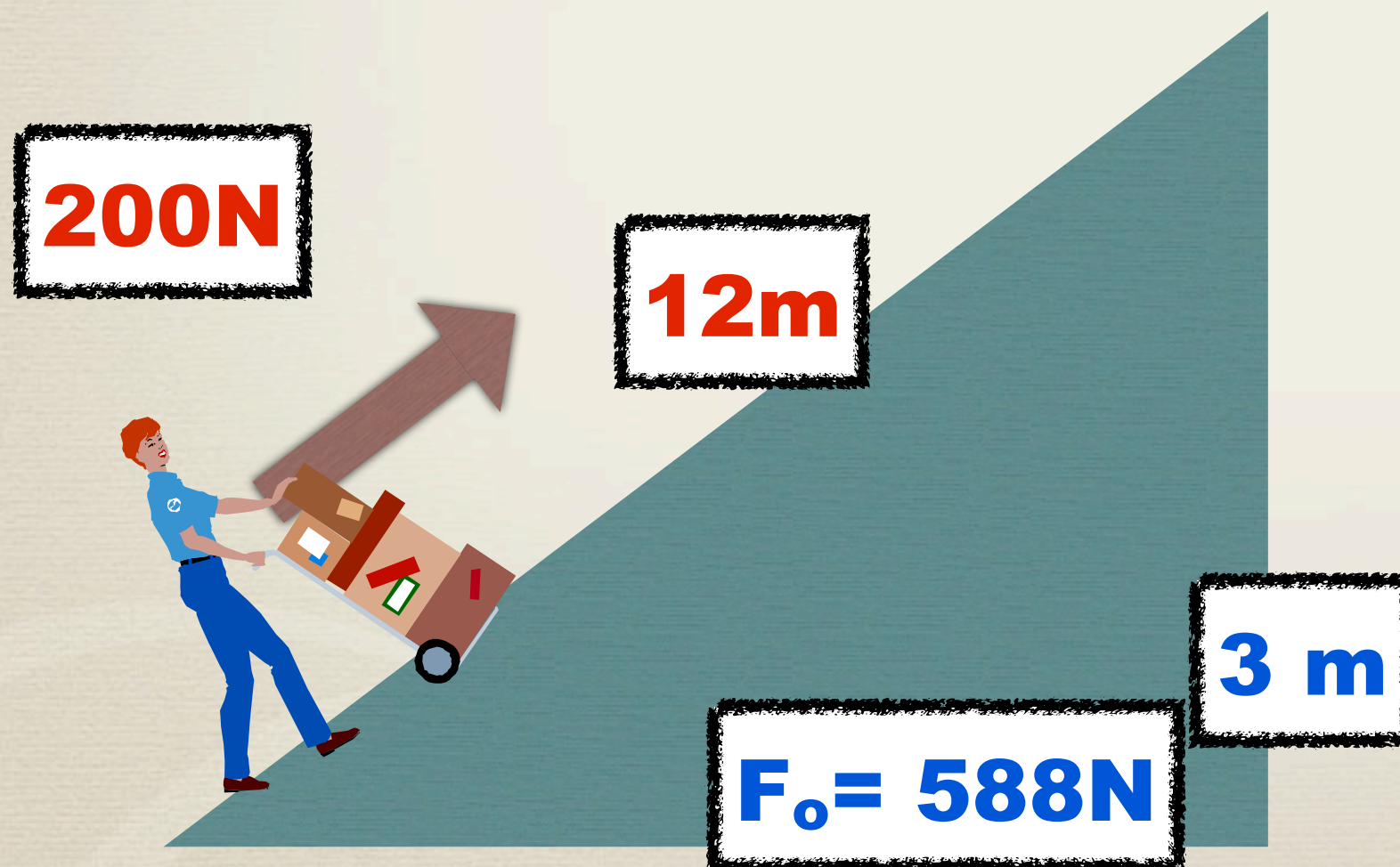
$$\begin{aligned}\text{Efficiency} &= W_o / W_i \\ &= AMA / IMA \\ \text{Eff} &= 73.5\%\end{aligned}$$

$$\begin{aligned}\text{Lost Energy to Friction} \\ 2400\text{J} - 1764\text{J} \\ 636\text{J}\end{aligned}$$

$$\text{Power} = W / t$$

Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power



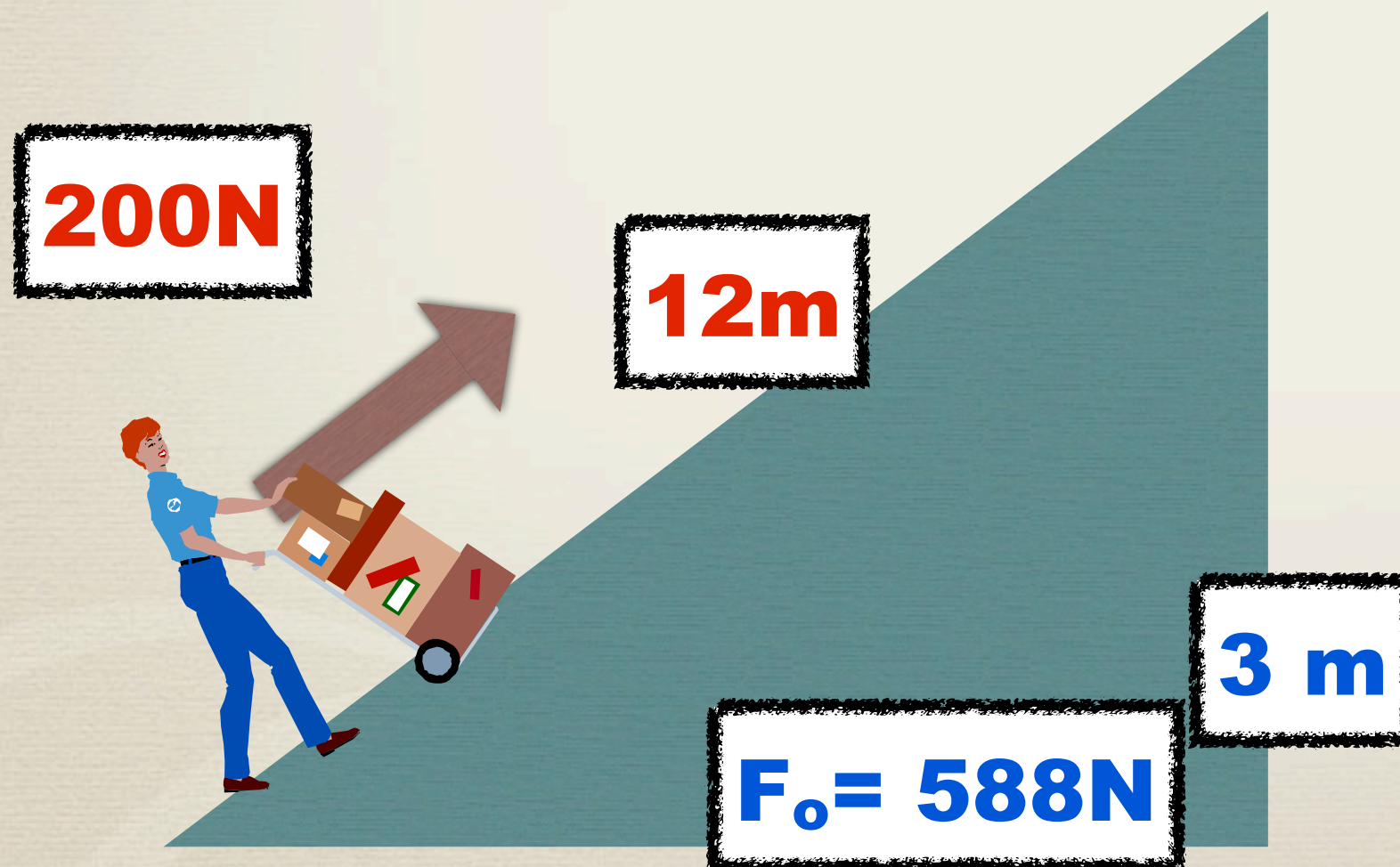
$$\begin{aligned}\text{Efficiency} &= W_o / W_i \\ &= AMA / IMA \\ \text{Eff} &= 73.5\%\end{aligned}$$

$$\begin{aligned}\text{Lost Energy to Friction} \\ 2400\text{J} - 1764\text{J} \\ 636\text{J}\end{aligned}$$

$$\begin{aligned}\text{Power} &= W / t \\ P &= 2400\text{J} / 30\text{s}\end{aligned}$$

Laura lifts some boxes up 3m by pushing the 60 kg cart up a 12 m ramp. She uses a force of 200 N and takes 30 seconds to travel.

Find; the work input, the work output, the IMA and AMA, the efficiency of the ramp, energy wasted by friction, her power

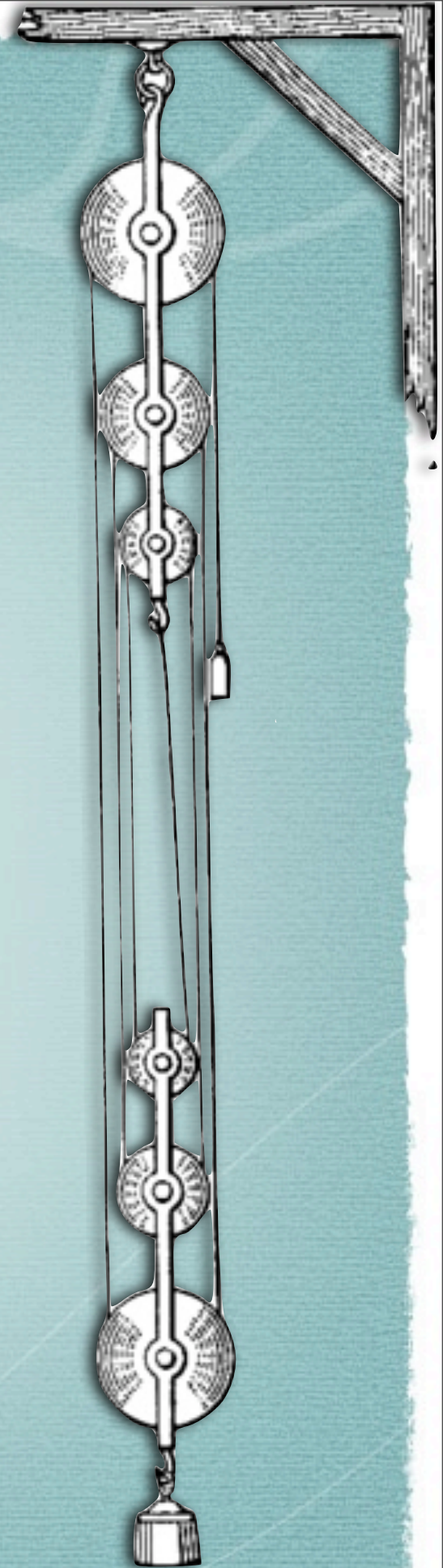


$$\begin{aligned}\text{Efficiency} &= W_o / W_i \\ &= AMA / IMA \\ \text{Eff} &= 73.5\%\end{aligned}$$

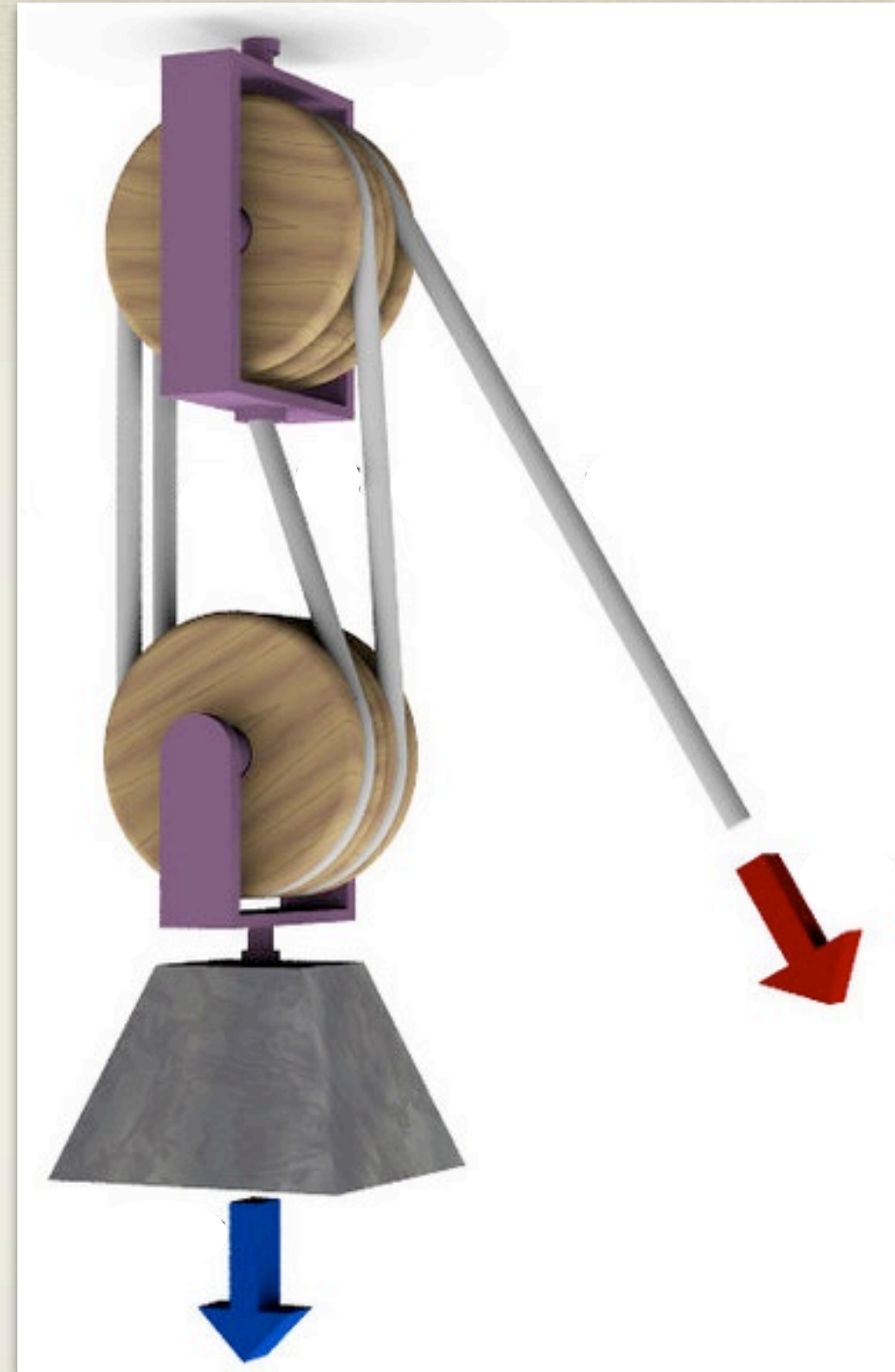
$$\begin{aligned}\text{Lost Energy to Friction} \\ 2400\text{J} - 1764\text{J} \\ 636\text{J}\end{aligned}$$

$$\begin{aligned}\text{Power} &= W / t \\ P &= 2400\text{J} / 30\text{s} \\ P &= 80\text{ W}\end{aligned}$$

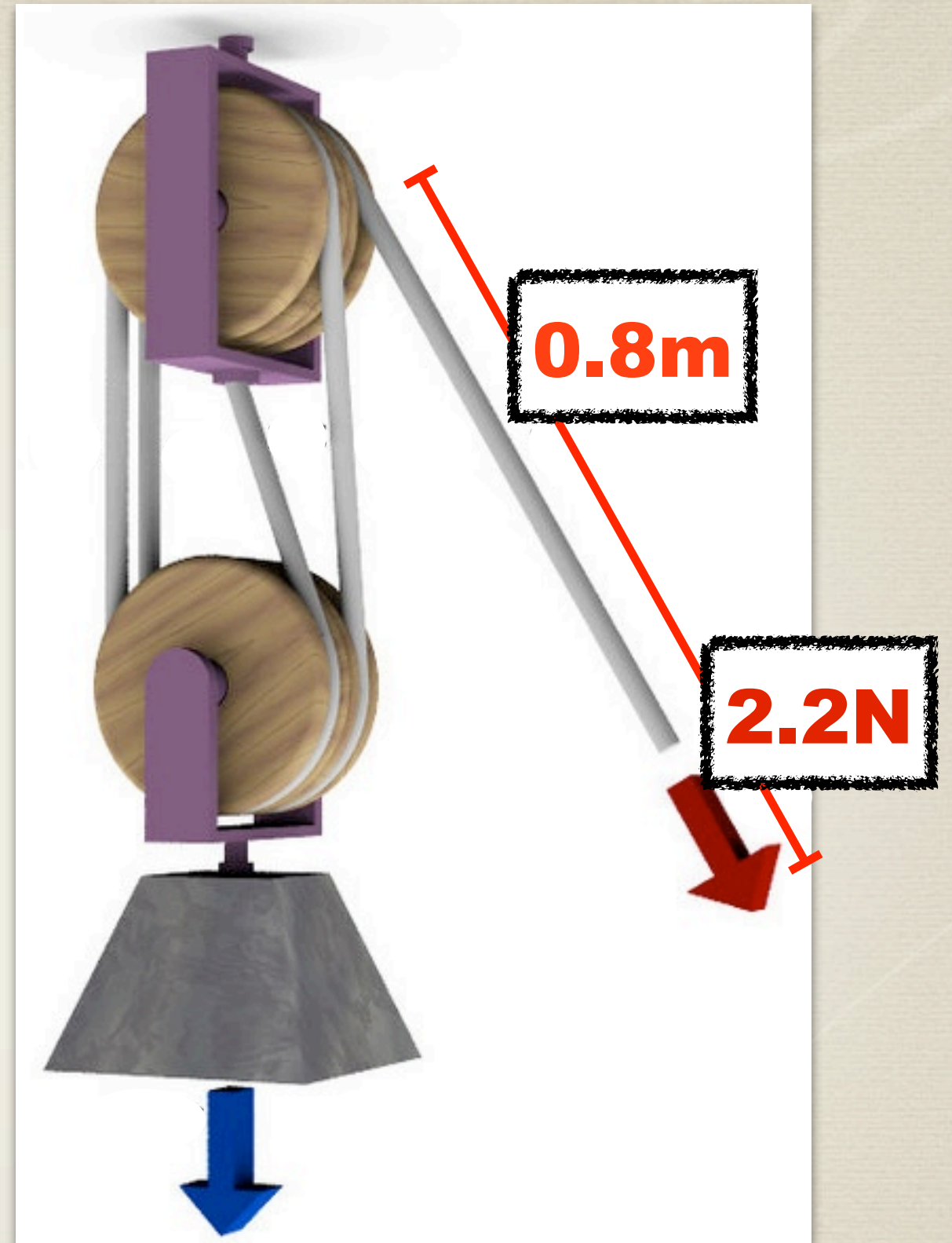
Pulley Arrangements



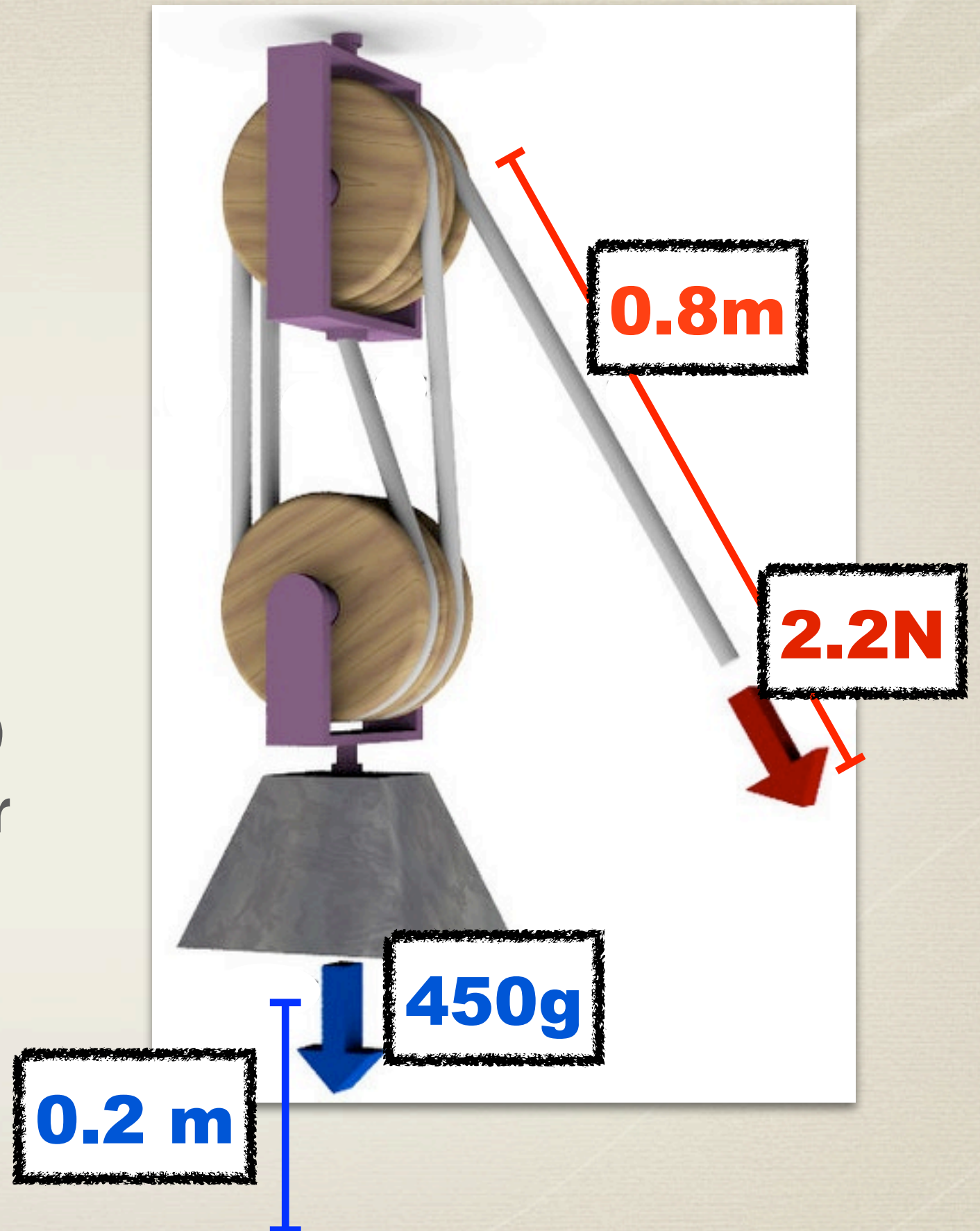
- In the Pulley arrangement shown, A force of 2.2 N is used to lift a 450 g Mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift.



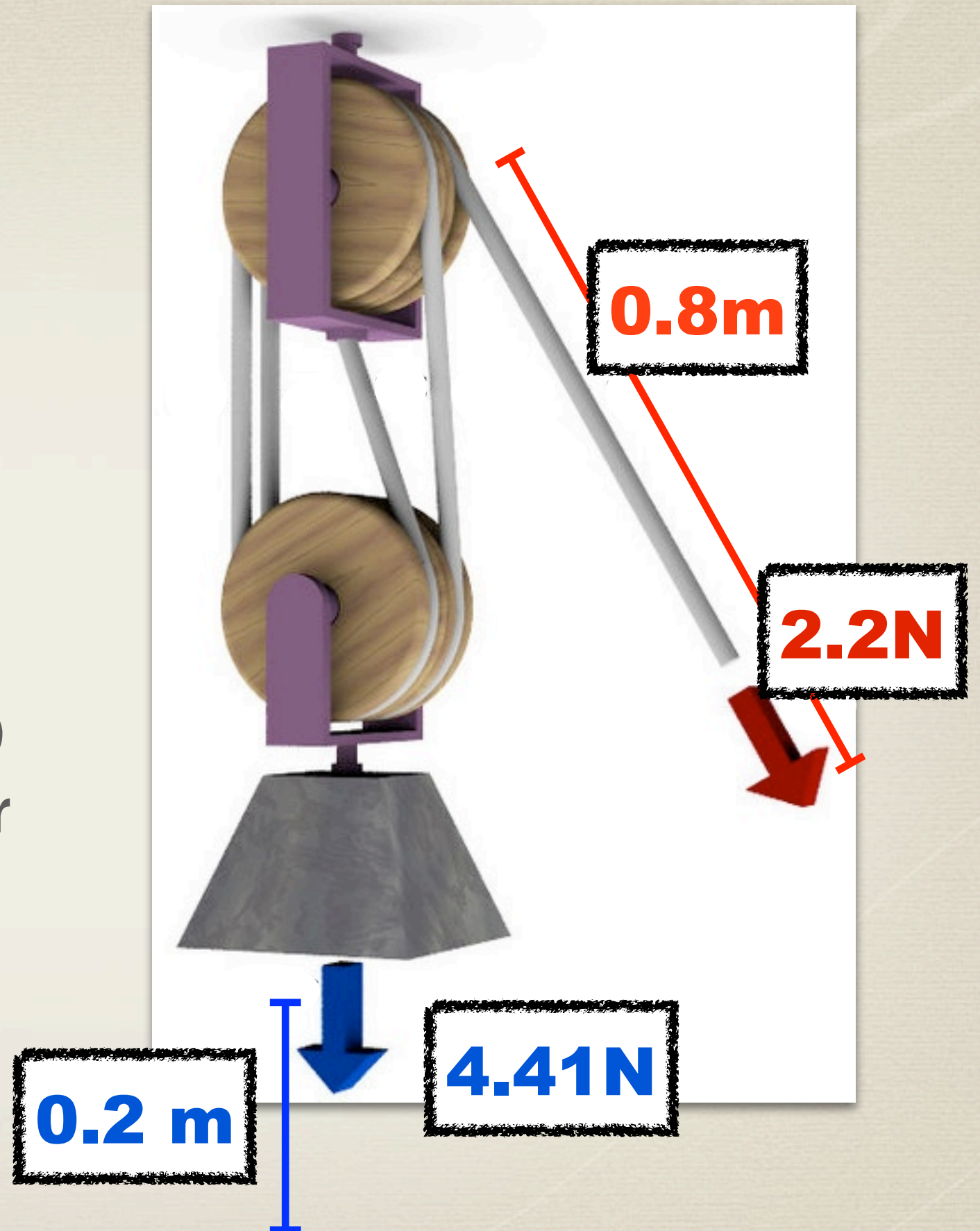
- In the Pulley arrangement shown, A force of 2.2 N is used to lift a 450 g Mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift.



- In the Pulley arrangement shown, A force of 2.2 N is used to lift a 450 g Mass. While the mass goes up 20 cm , a student pulls in 80 cm of string. It takes her 5 seconds to lift.

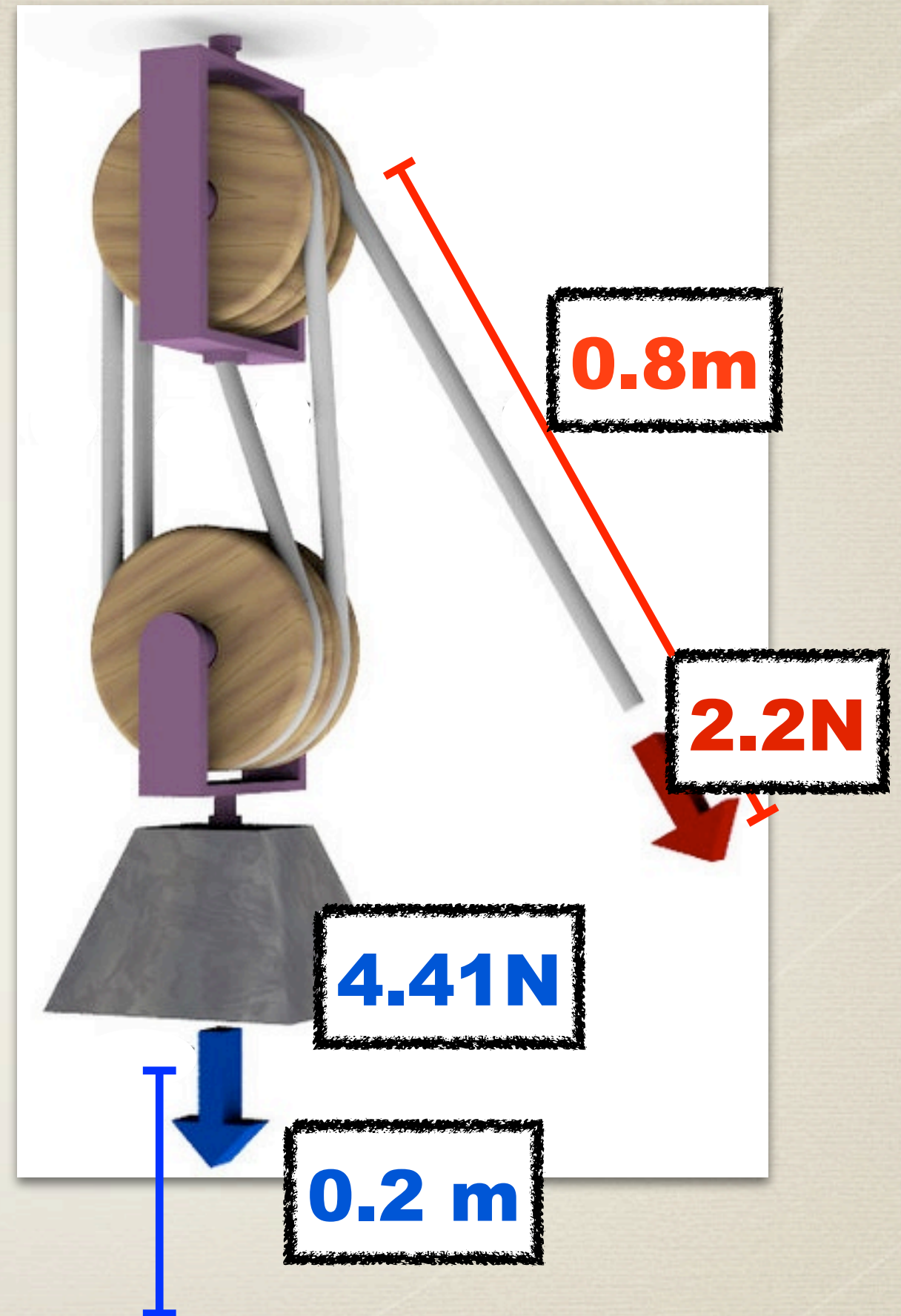


- In the Pulley arrangement shown, A force of 2.2 N is used to lift a 450 g Mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift.



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

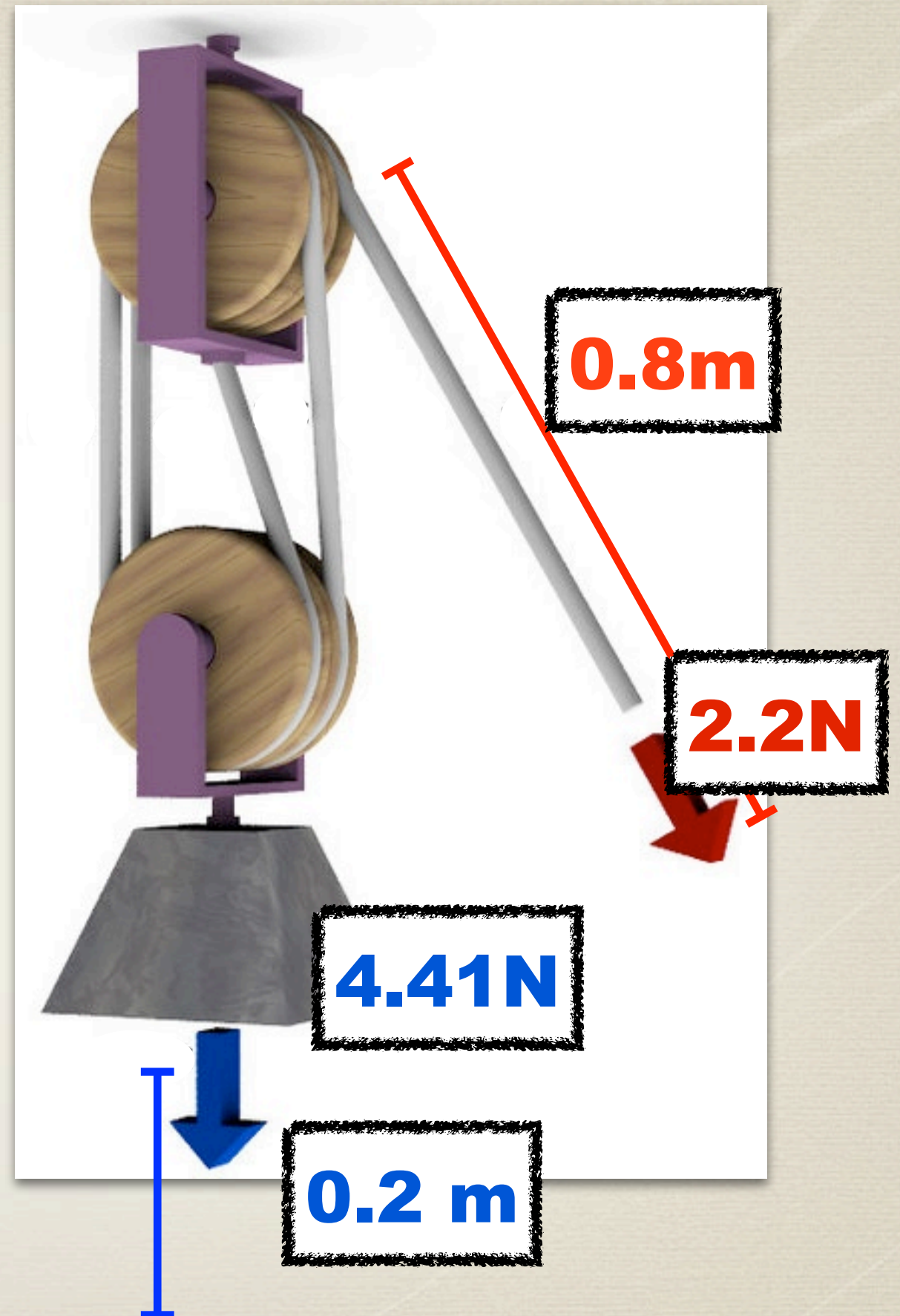
Find the work input,
the work output,
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input,
the work output,
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

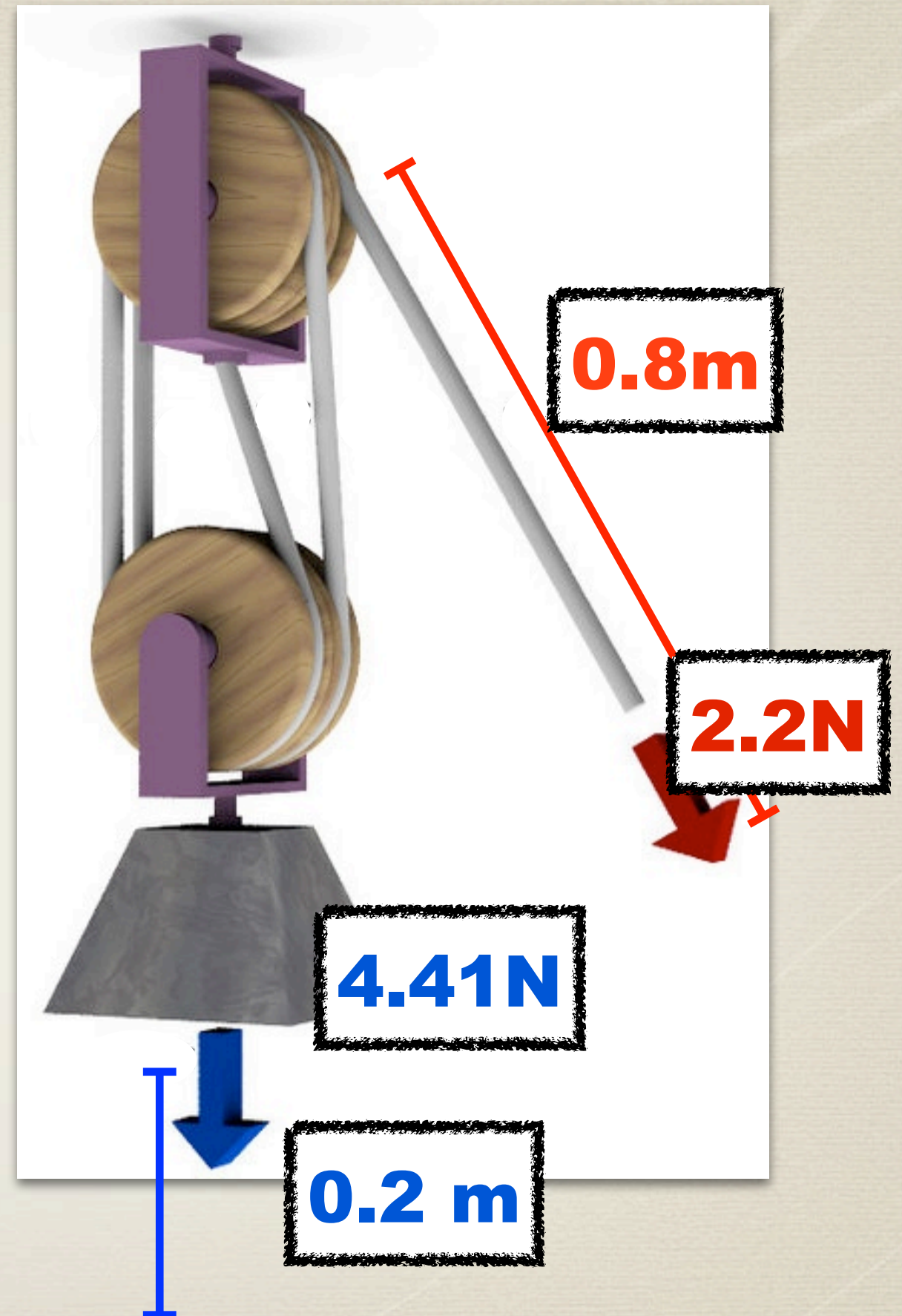
$$W_i = FD$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input,
the work output,
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

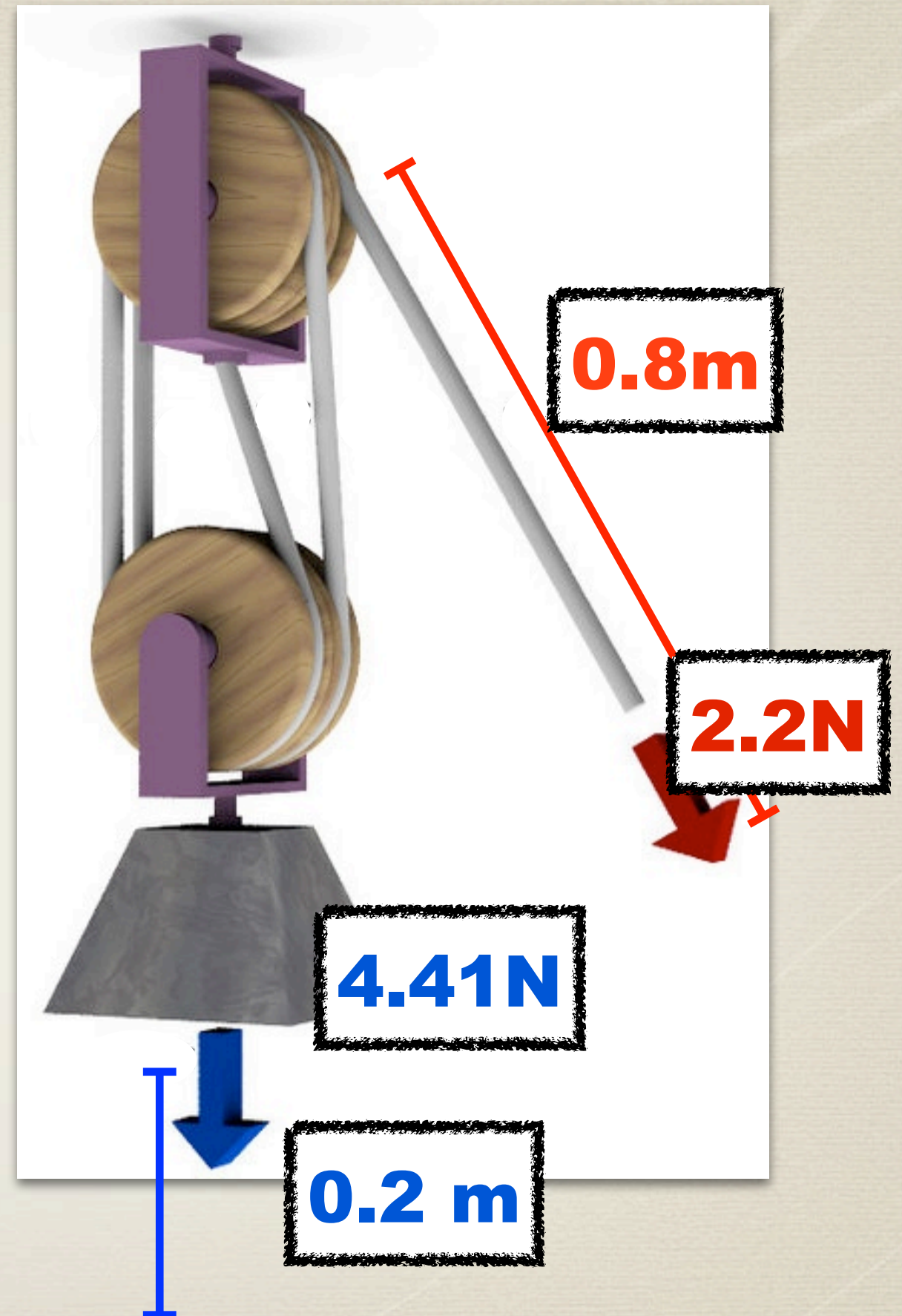
$$W_i = FD$$
$$W_i = (2.2\text{N})(0.8\text{m})$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input,
the work output,
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

$$W_i = FD$$
$$W_i = (2.2\text{N})(0.8\text{m})$$
$$W_i = 1.76 \text{ J}$$

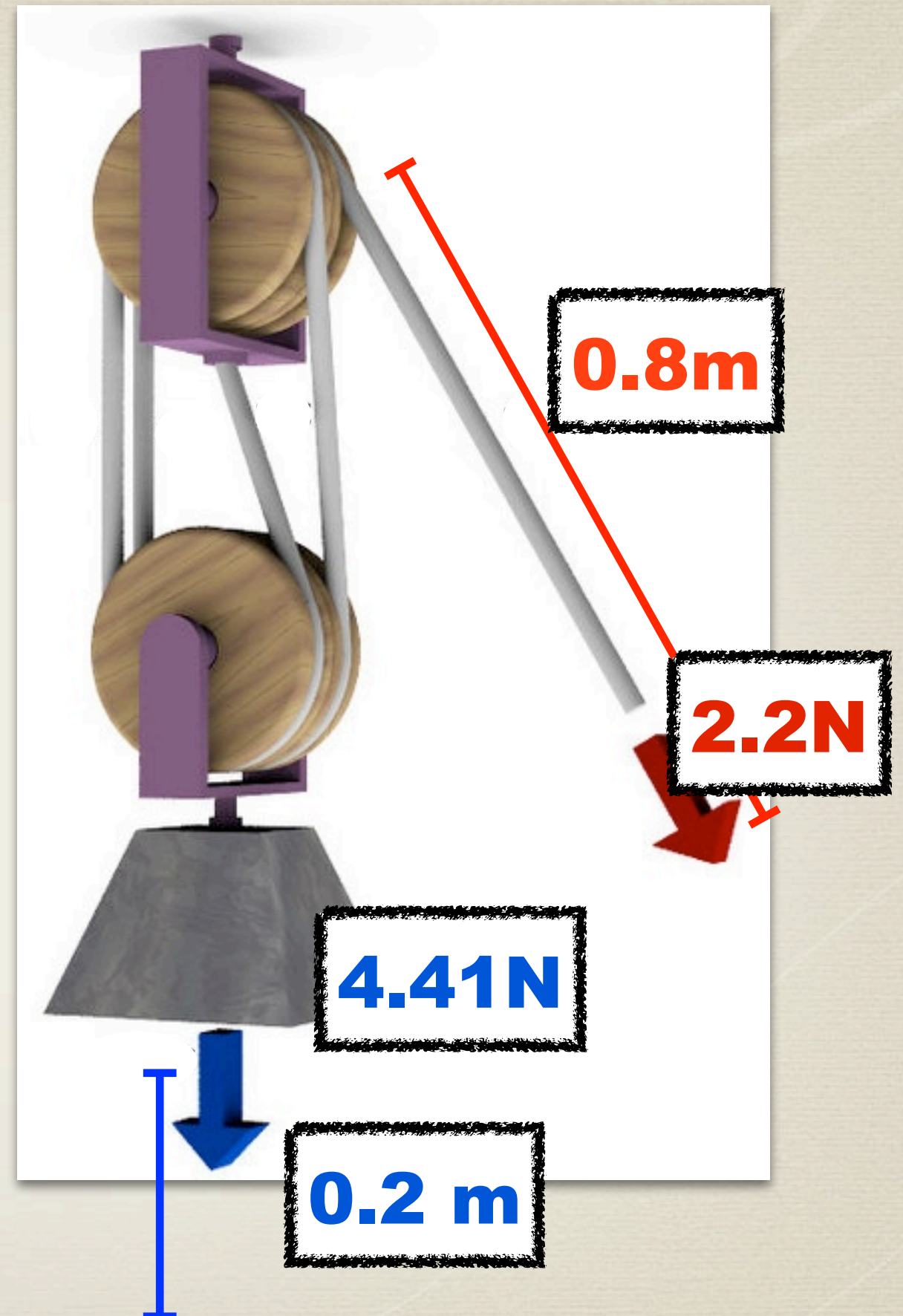


► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input,
the work output,
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

$$W_i = FD$$
$$W_i = (2.2\text{N})(0.8\text{m})$$
$$W_i = 1.76 \text{ J}$$

$$W_o = FD$$

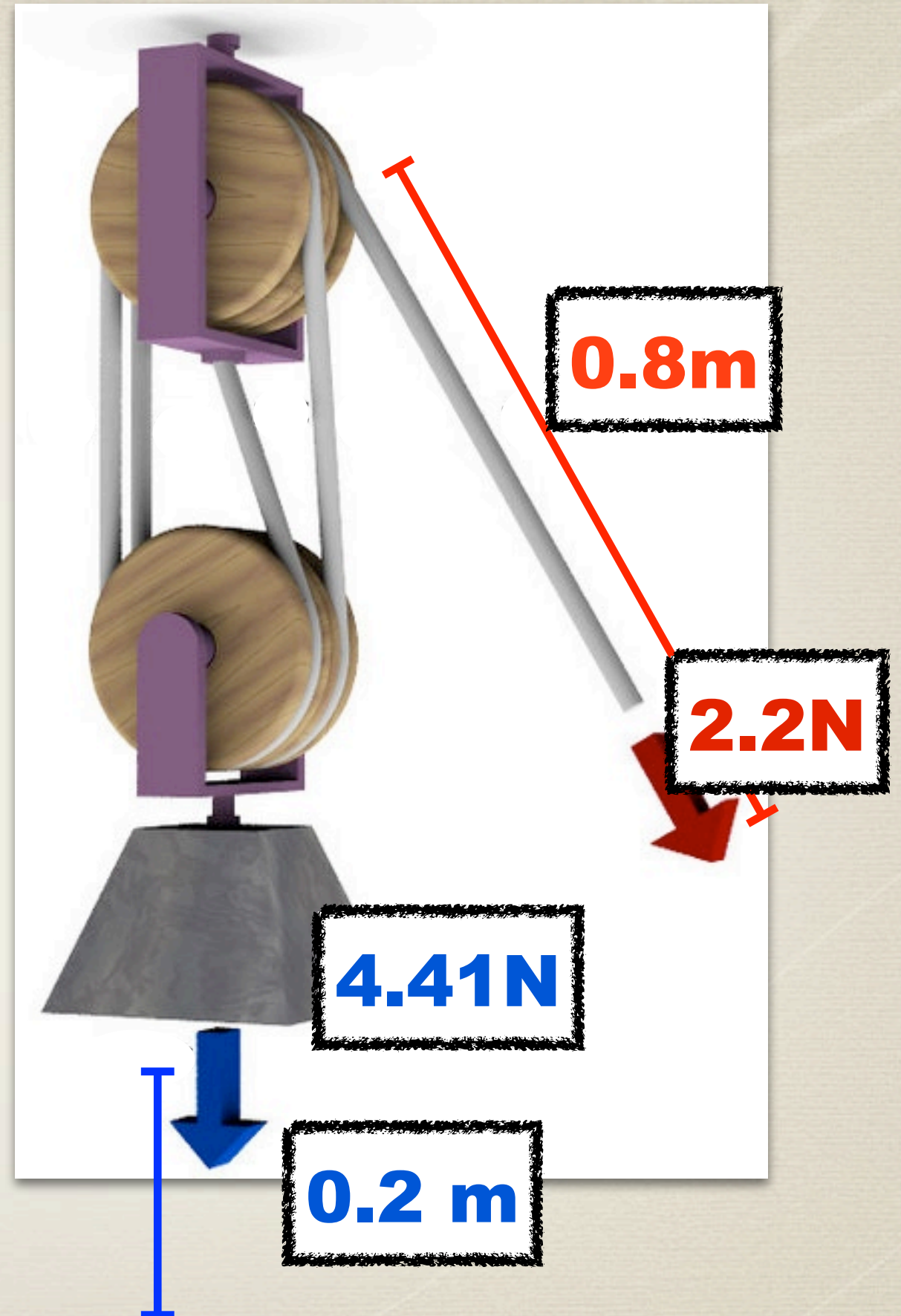


► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input,
the work output,
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

$$W_i = FD$$
$$W_i = (2.2\text{N})(0.8\text{m})$$
$$W_i = 1.76 \text{ J}$$

$$W_o = FD$$
$$W_o = 4.41\text{N}(0.2\text{m})$$

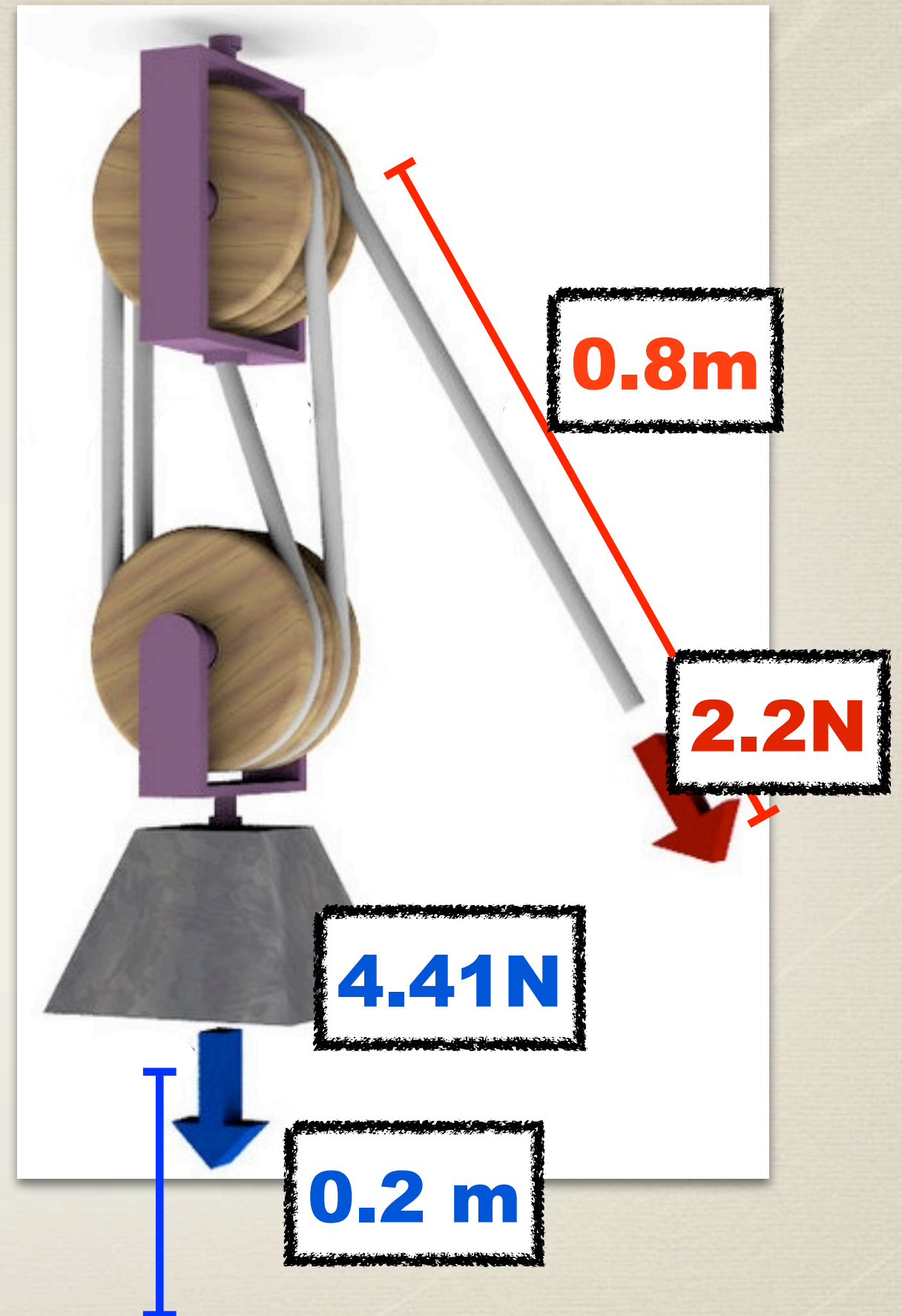


► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input,
the work output,
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

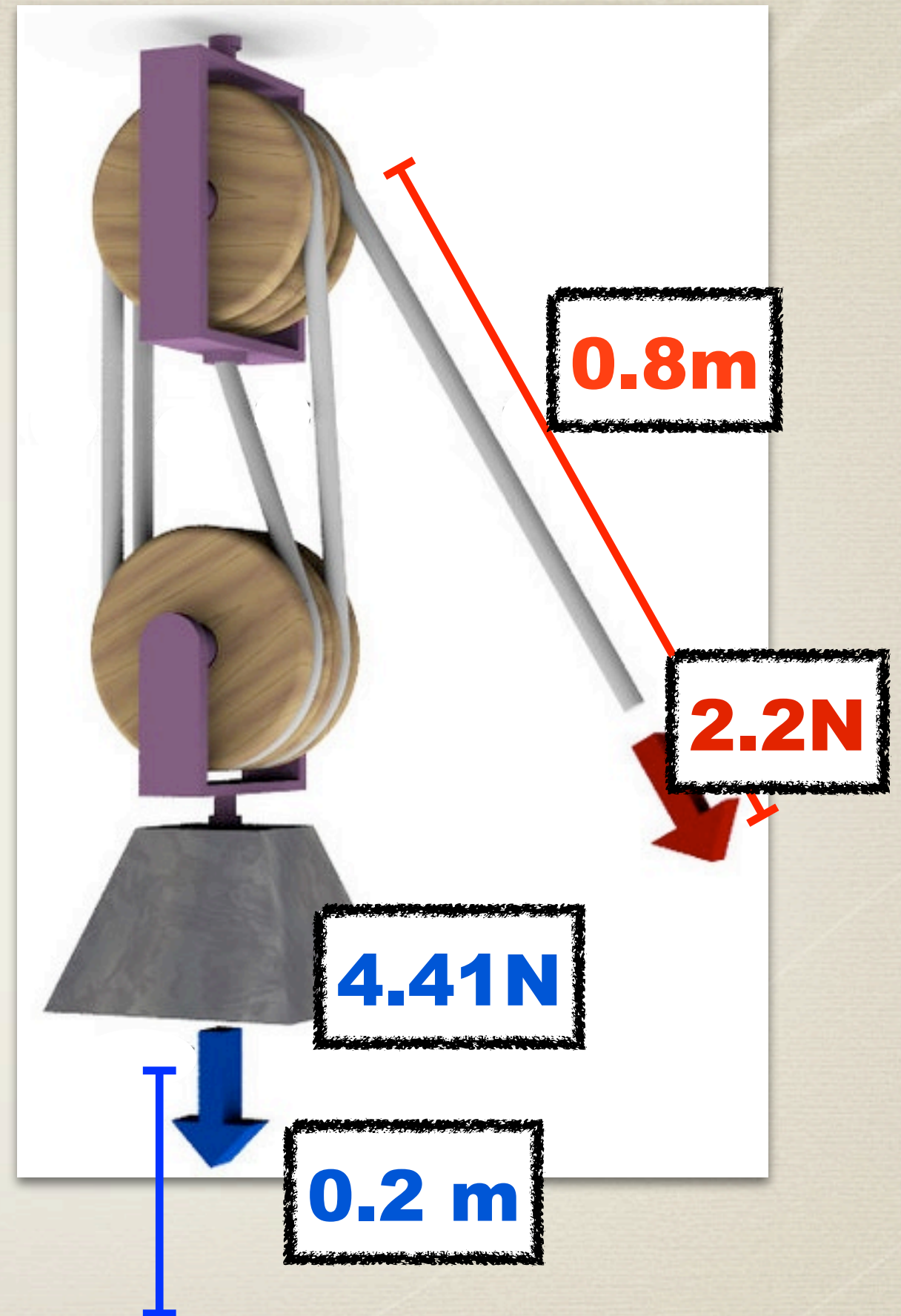
$$W_i = FD$$
$$W_i = (2.2\text{N})(0.8\text{m})$$
$$W_i = 1.76 \text{ J}$$

$$W_o = FD$$
$$W_o = 4.41\text{N}(0.2\text{m})$$
$$W_o = 0.882 \text{ J}$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

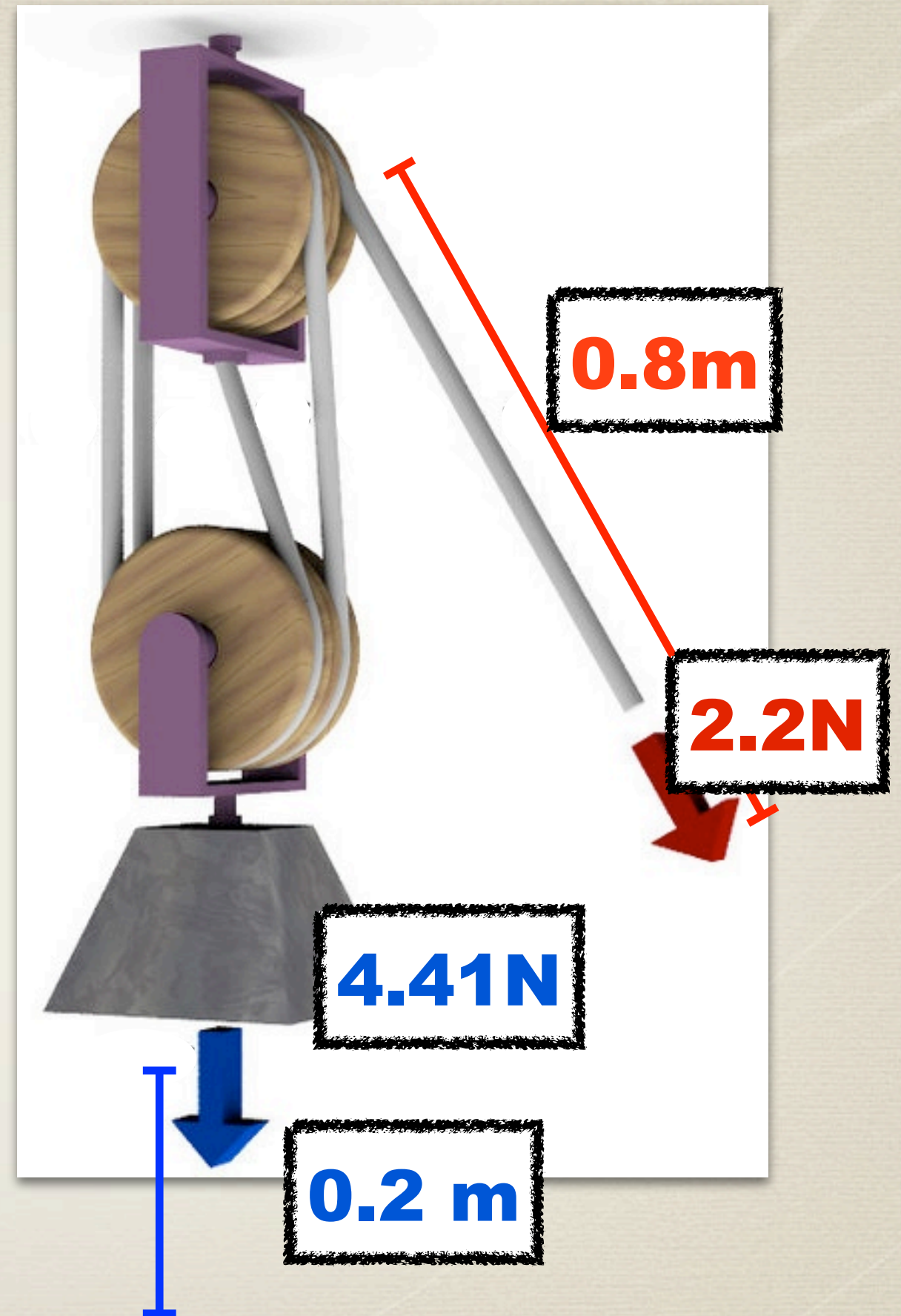
Find the work input $W_i = 1.76 \text{ J}$
the work output, $W_o = 0.882 \text{ J}$
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input $W_i = 1.76 \text{ J}$
the work output, $W_o = 0.882 \text{ J}$
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

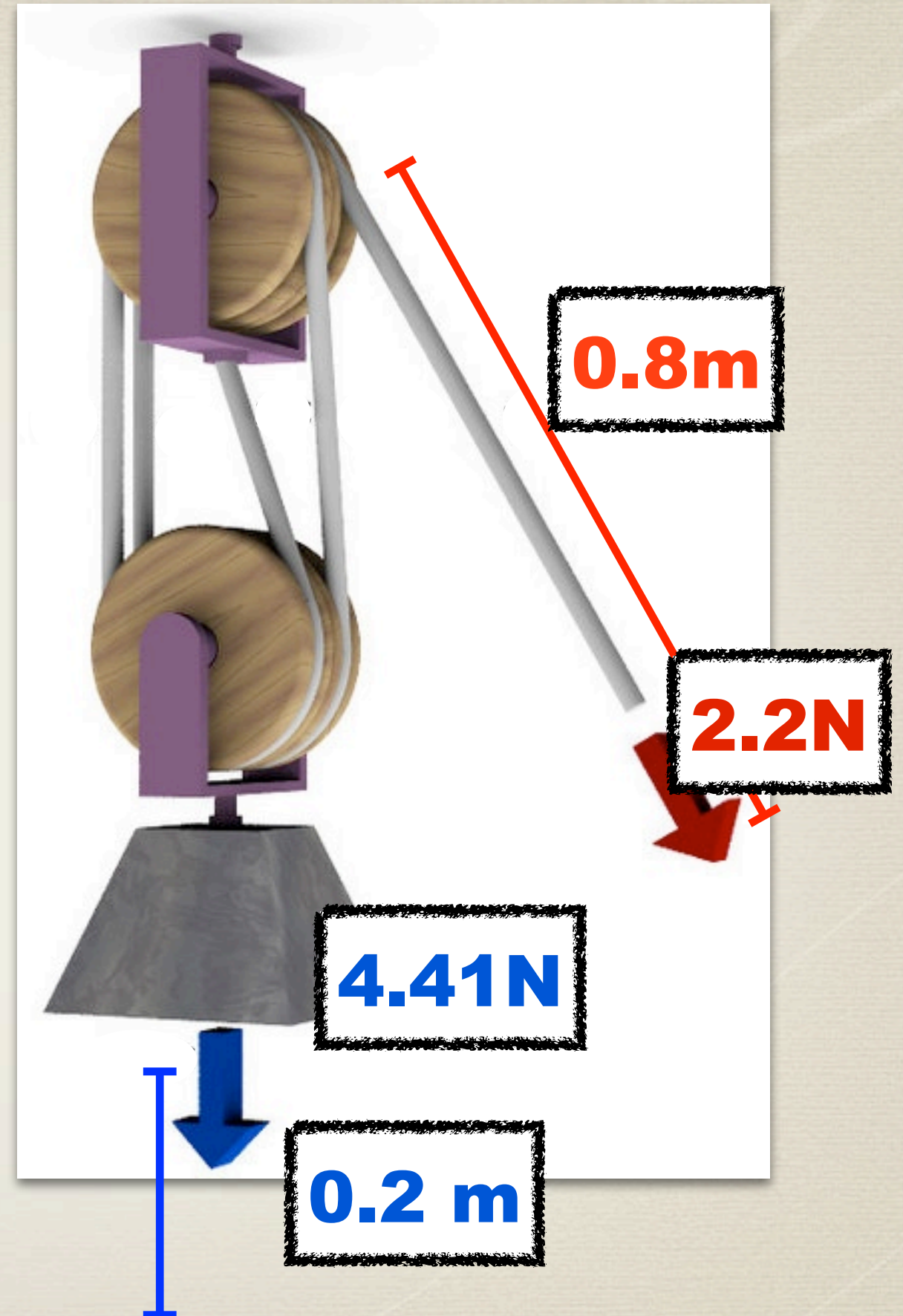
$$\text{IMA} = D_i / D_o$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input $W_i = 1.76 \text{ J}$
the work output, $W_o = 0.882 \text{ J}$
the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

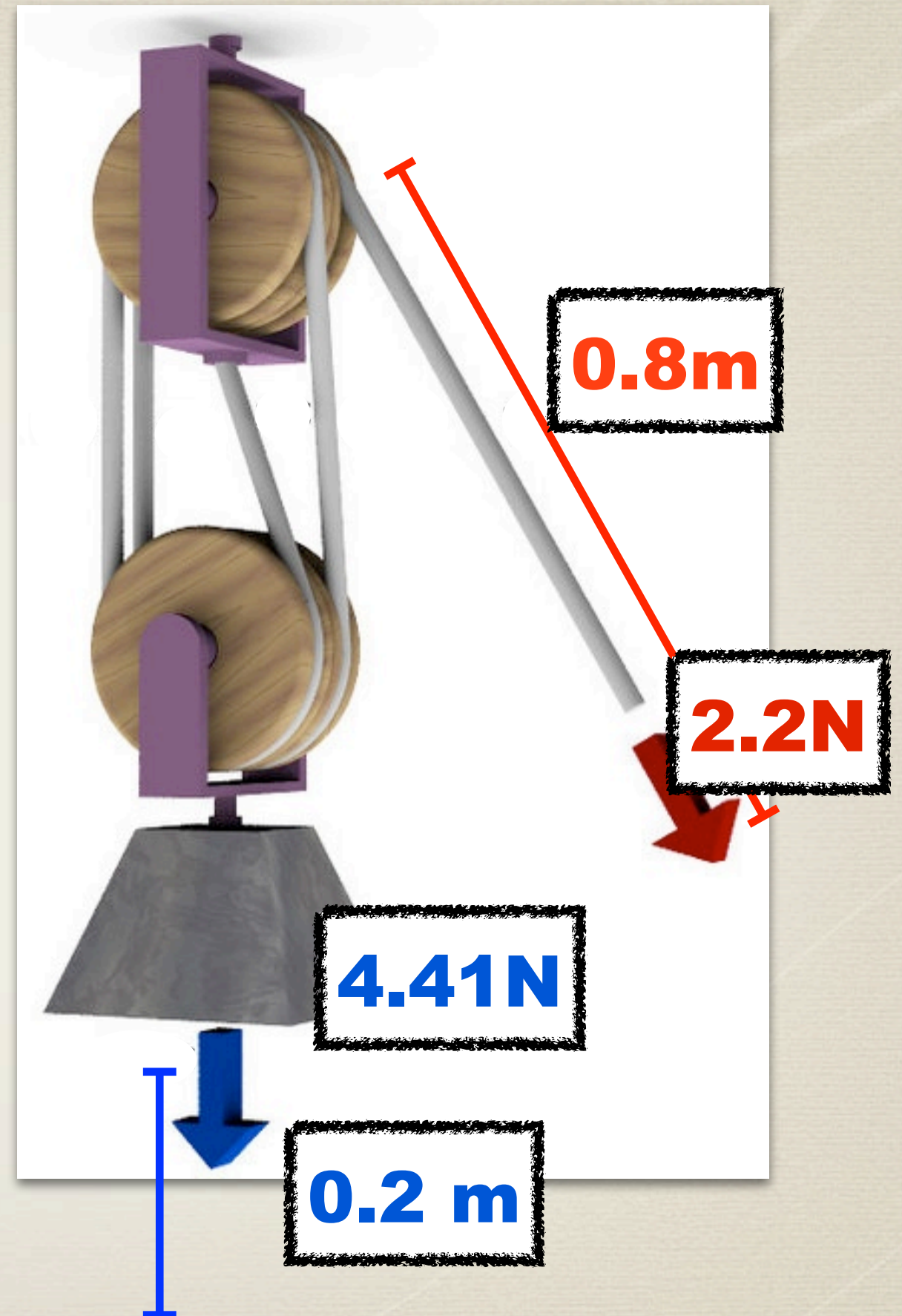
$$\text{IMA} = D_i / D_o$$
$$\text{IMA} = (0.8\text{m}) / (0.2\text{m})$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

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the IMA,
the AMA,
the efficiency of the pulley,
the energy wasted by friction,
her power

$$\text{IMA} = D_i / D_o$$
$$\text{IMA} = (0.8\text{m}) / (0.2\text{m})$$
$$\text{IMA} = 4$$

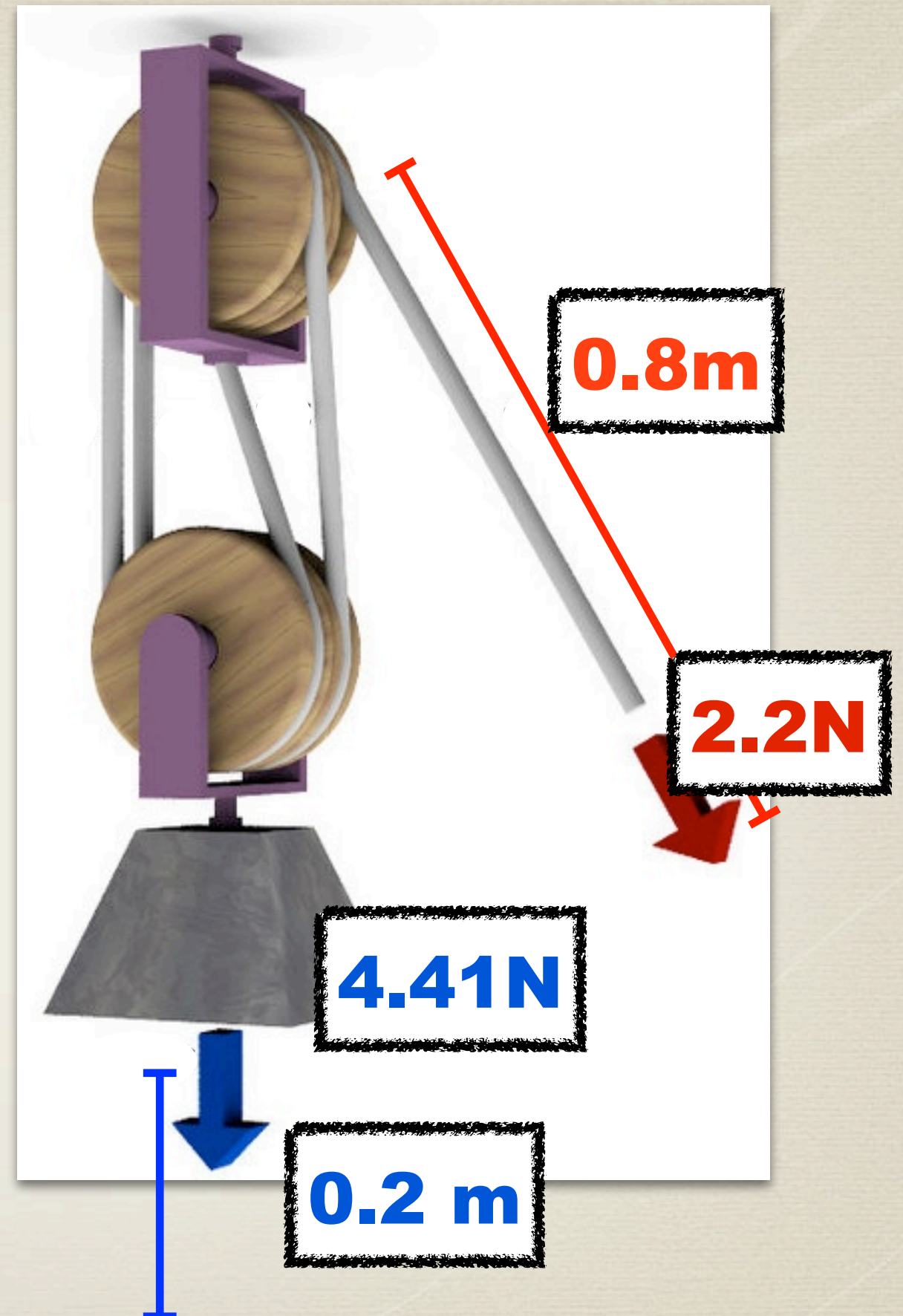


► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

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the AMA,
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$$\text{IMA} = D_i / D_o$$
$$\text{IMA} = (0.8\text{m}) / (0.2\text{m})$$
$$\text{IMA} = 4$$

$$\text{AMA} = F_o / F_i$$

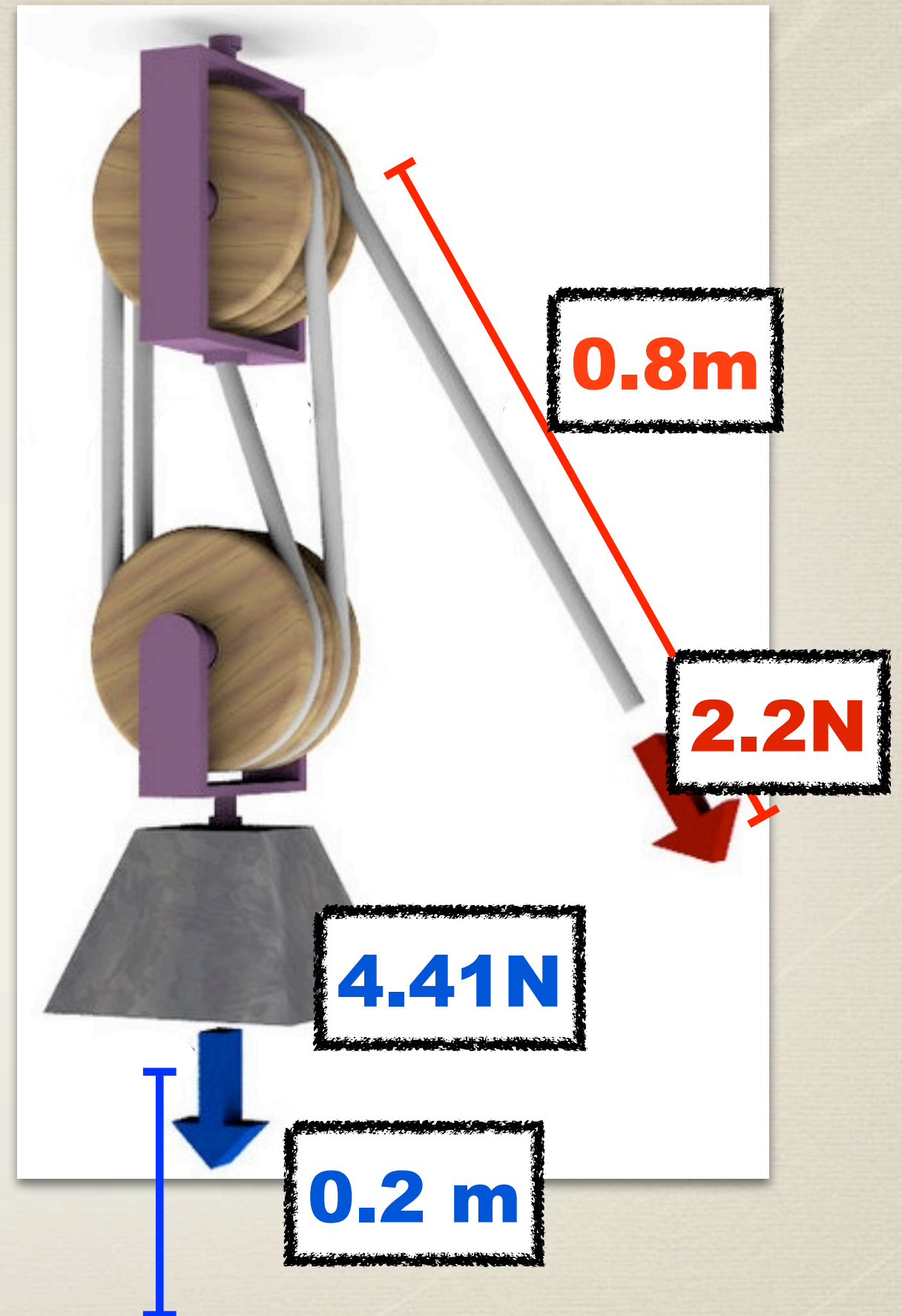


► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

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$$\text{IMA} = D_i / D_o$$
$$\text{IMA} = (0.8\text{m}) / (0.2\text{m})$$
$$\text{IMA} = 4$$

$$\text{AMA} = F_o / F_i$$
$$\text{AMA} = 4.41\text{N} / (2.2\text{N})$$

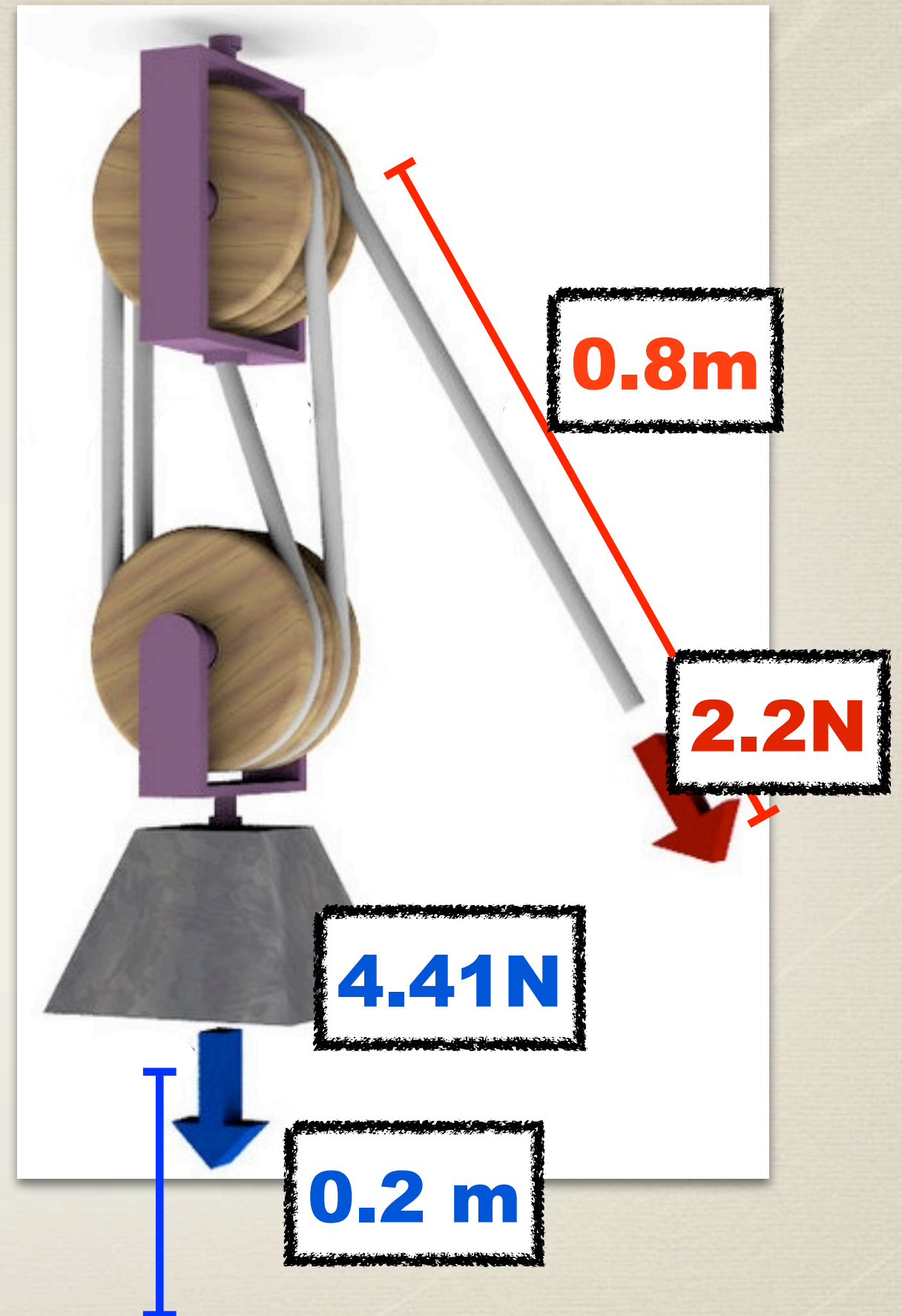


► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

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the IMA,
the AMA,
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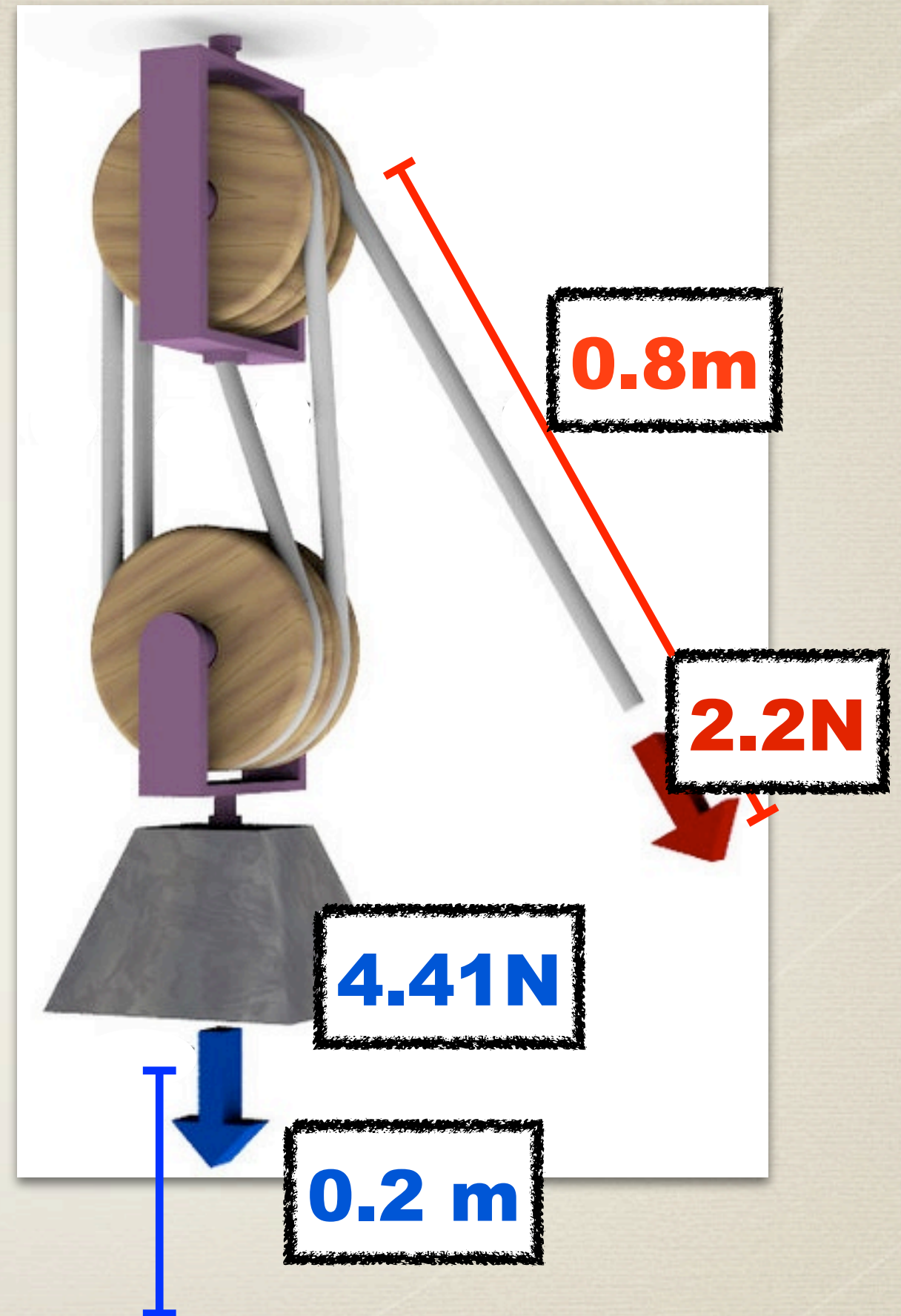
$$\begin{aligned} \text{IMA} &= D_i / D_o \\ \text{IMA} &= (0.8\text{m}) / (0.2\text{m}) \\ \text{IMA} &= 4 \end{aligned}$$

$$\begin{aligned} \text{AMA} &= F_o / F_i \\ \text{AMA} &= 4.41\text{N} / (2.2\text{N}) \\ \text{AMA} &= 2 \end{aligned}$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

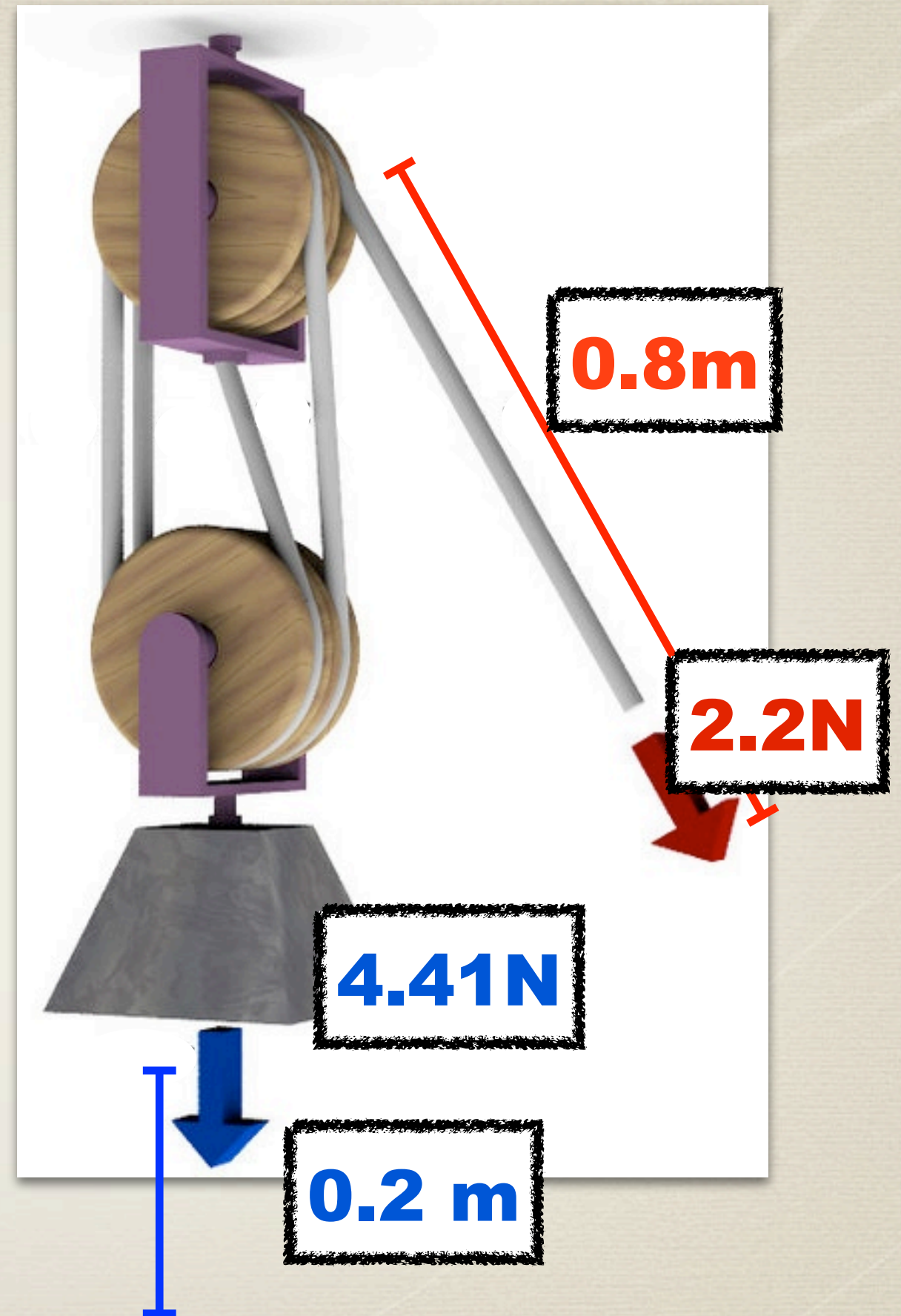
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the work output, $W_o = 0.882 \text{ J}$
the IMA, $IMA = 4$
the AMA, $AMA = 2$
the efficiency of the pulley,
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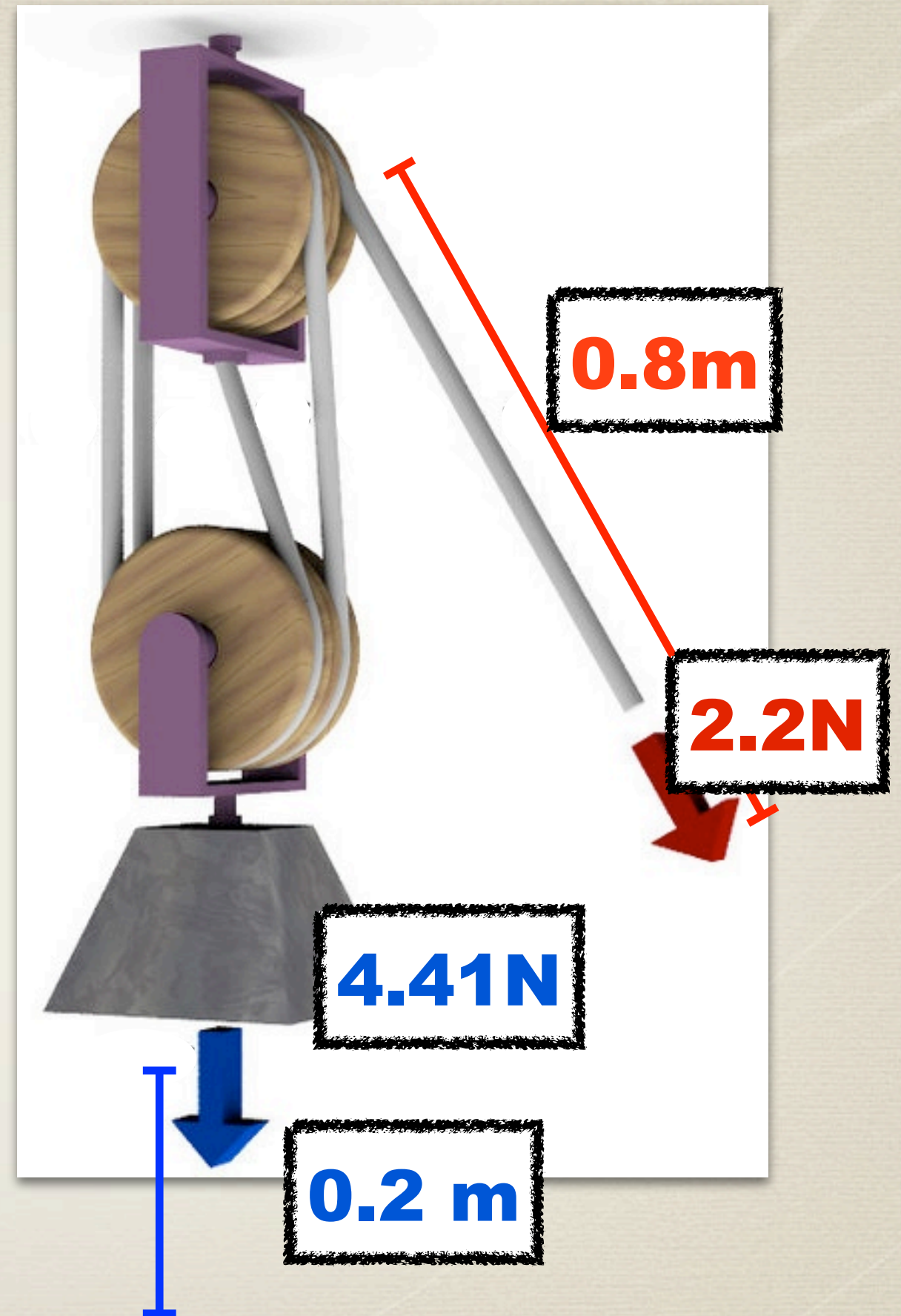
$$\text{Efficiency} = W_o / W_i$$



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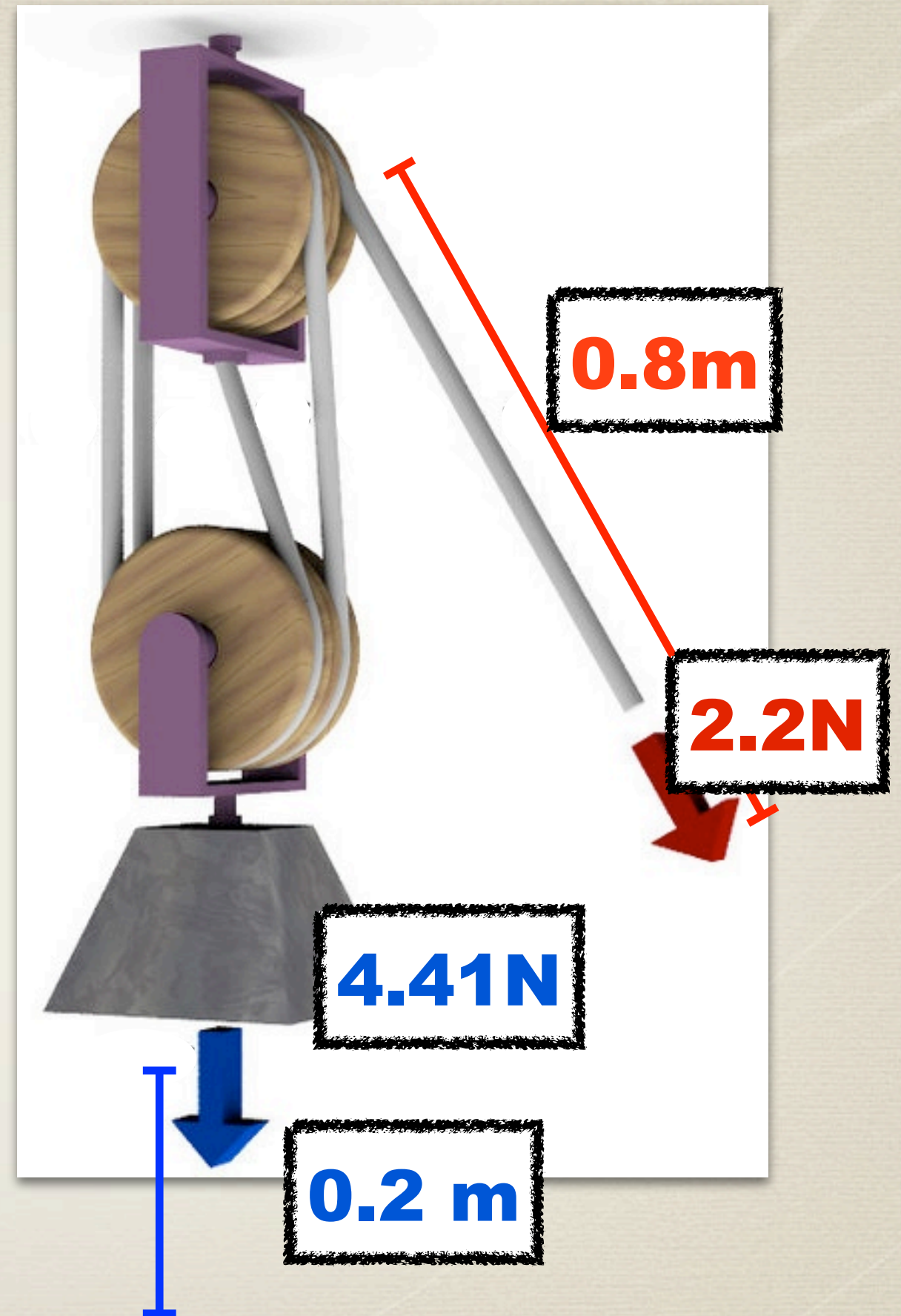
$$\text{Efficiency} = W_o / W_i$$
$$\text{Efficiency} = (0.882\text{J}) / (1.76\text{J})$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

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the work output, $W_o = 0.882 \text{ J}$
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the efficiency of the pulley,
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$$\text{Efficiency} = W_o / W_i$$
$$\text{Efficiency} = (0.882\text{J}) / (1.76\text{J})$$
$$\text{Efficiency} = 0.5 = 50\%$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

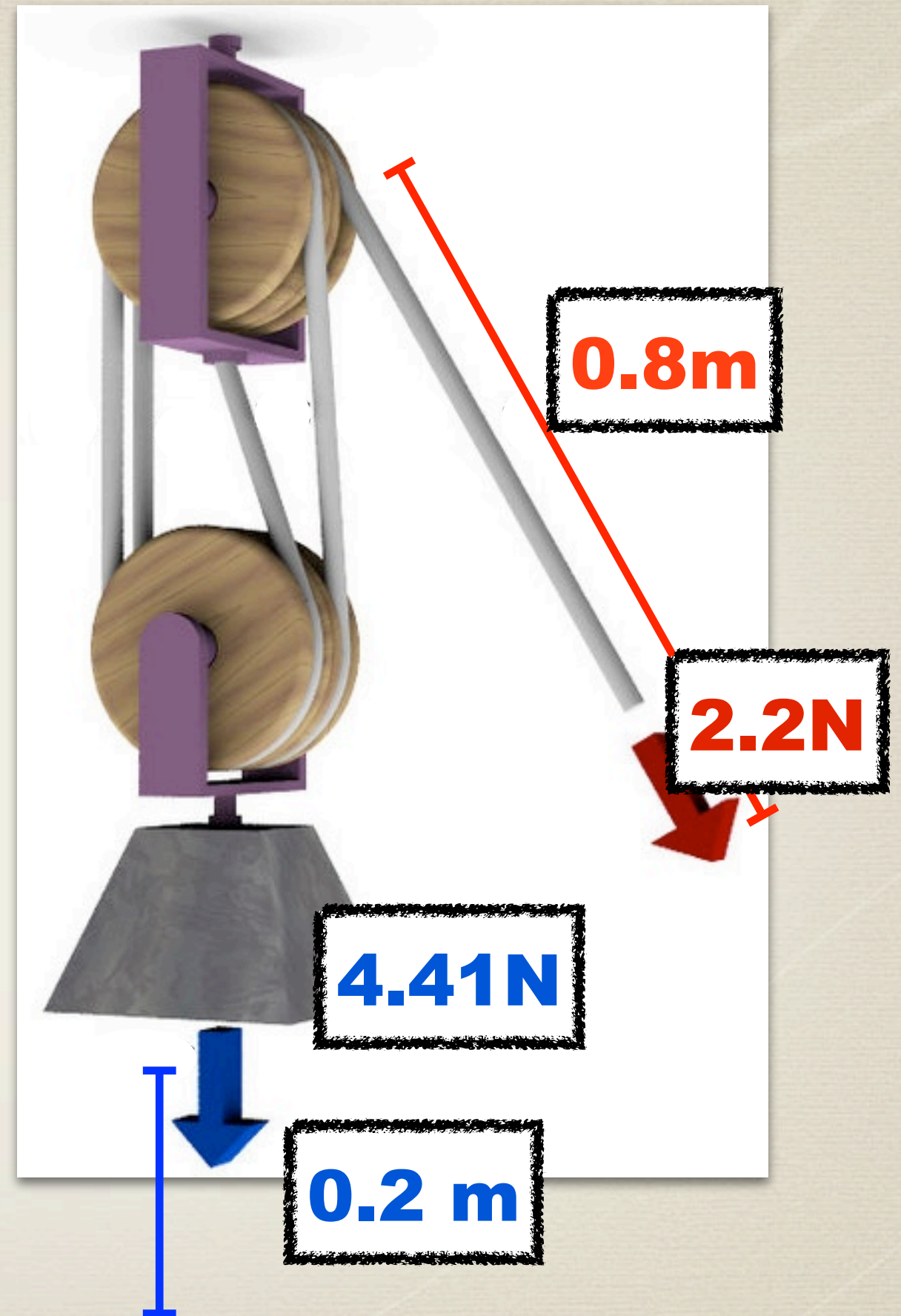
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$$\text{Efficiency} = W_o / W_i$$

$$\text{Efficiency} = (0.882\text{J}) / (1.76\text{J})$$

$$\text{Efficiency} = 0.5 = 50\%$$

Energy Lost

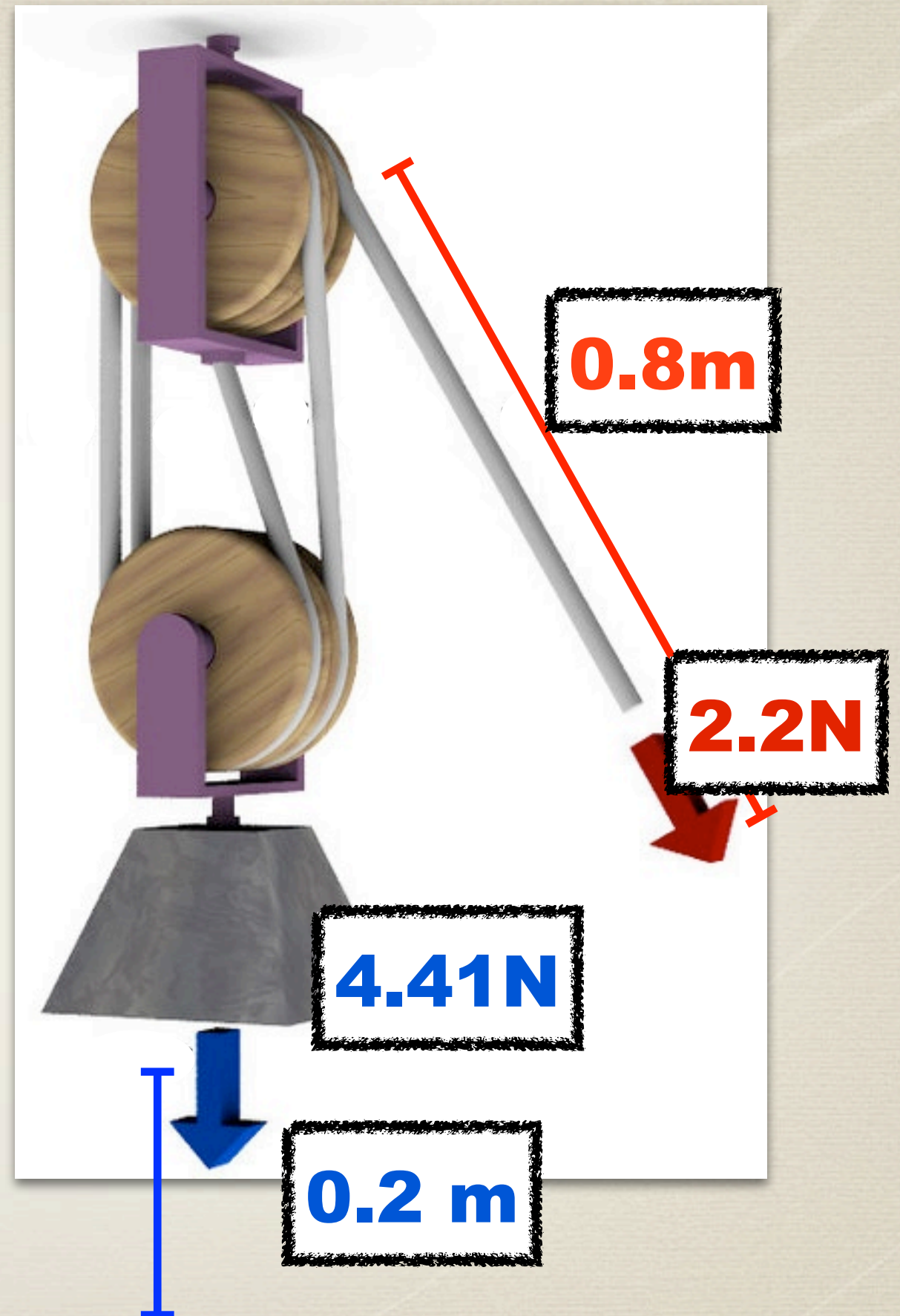


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$$\text{Efficiency} = W_o / W_i$$
$$\text{Efficiency} = (0.882\text{J}) / (1.76\text{J})$$
$$\text{Efficiency} = 0.5 = 50\%$$

$$\text{Energy Lost}$$
$$1.76 - 0.882 = 0.878\text{J}$$



► A force of 2.2 N is used to lift a 450 g mass. While the mass goes up 20 cm, a student pulls in 80 cm of string. It takes her 5 seconds to lift

Find the work input $W_i = 1.76 \text{ J}$
the work output, $W_o = 0.882 \text{ J}$
the IMA, $IMA = 4$
the AMA, $AMA = 2$
the efficiency of the pulley,
the energy wasted by friction,
her power

$$\text{Efficiency} = W_o / W_i$$

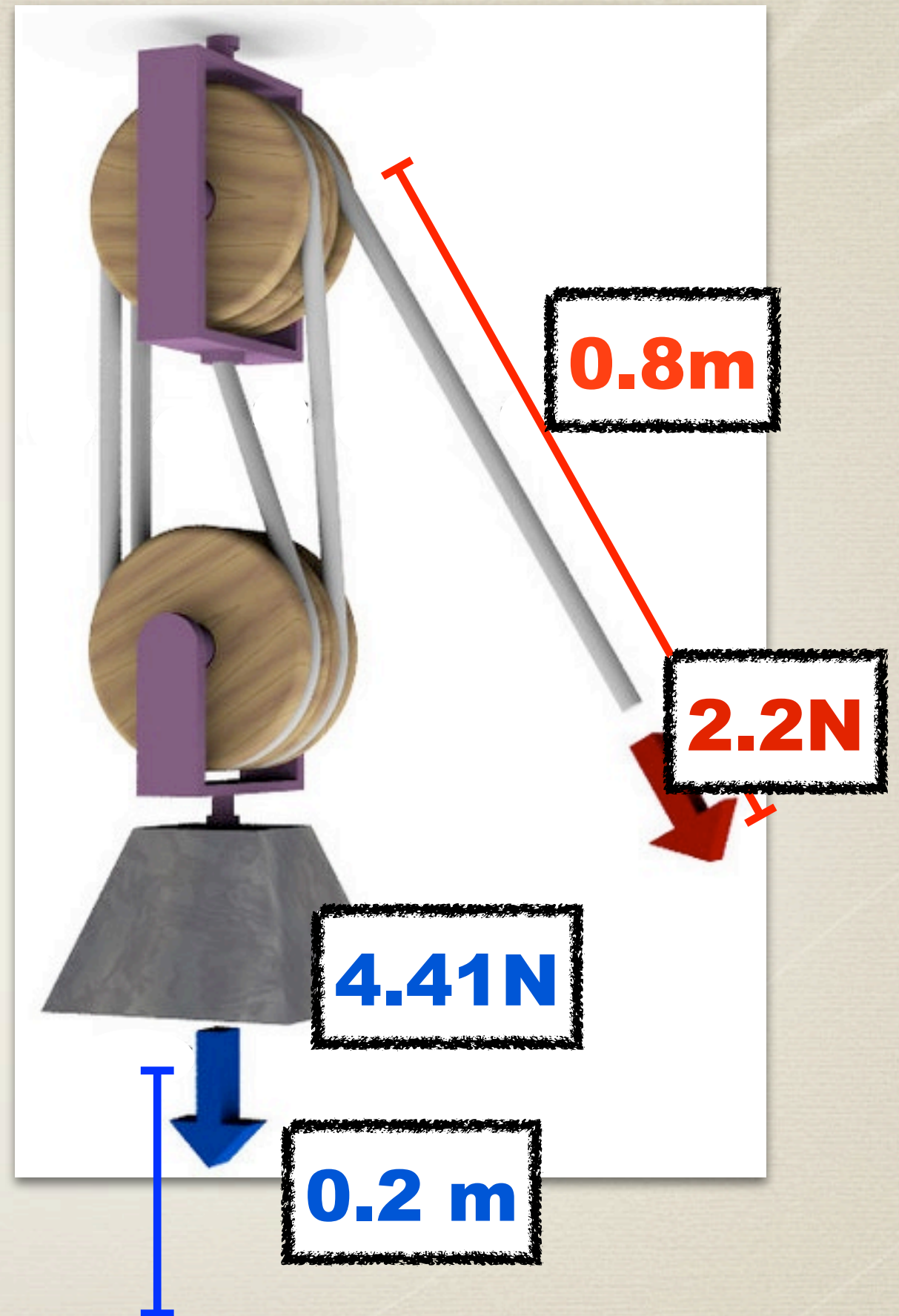
$$\text{Efficiency} = (0.882\text{J}) / (1.76\text{J})$$

$$\text{Efficiency} = 0.5 = 50\%$$

Energy Lost

$$1.76 - 0.882 = 0.878\text{J}$$

$$\text{Power} = W / t$$



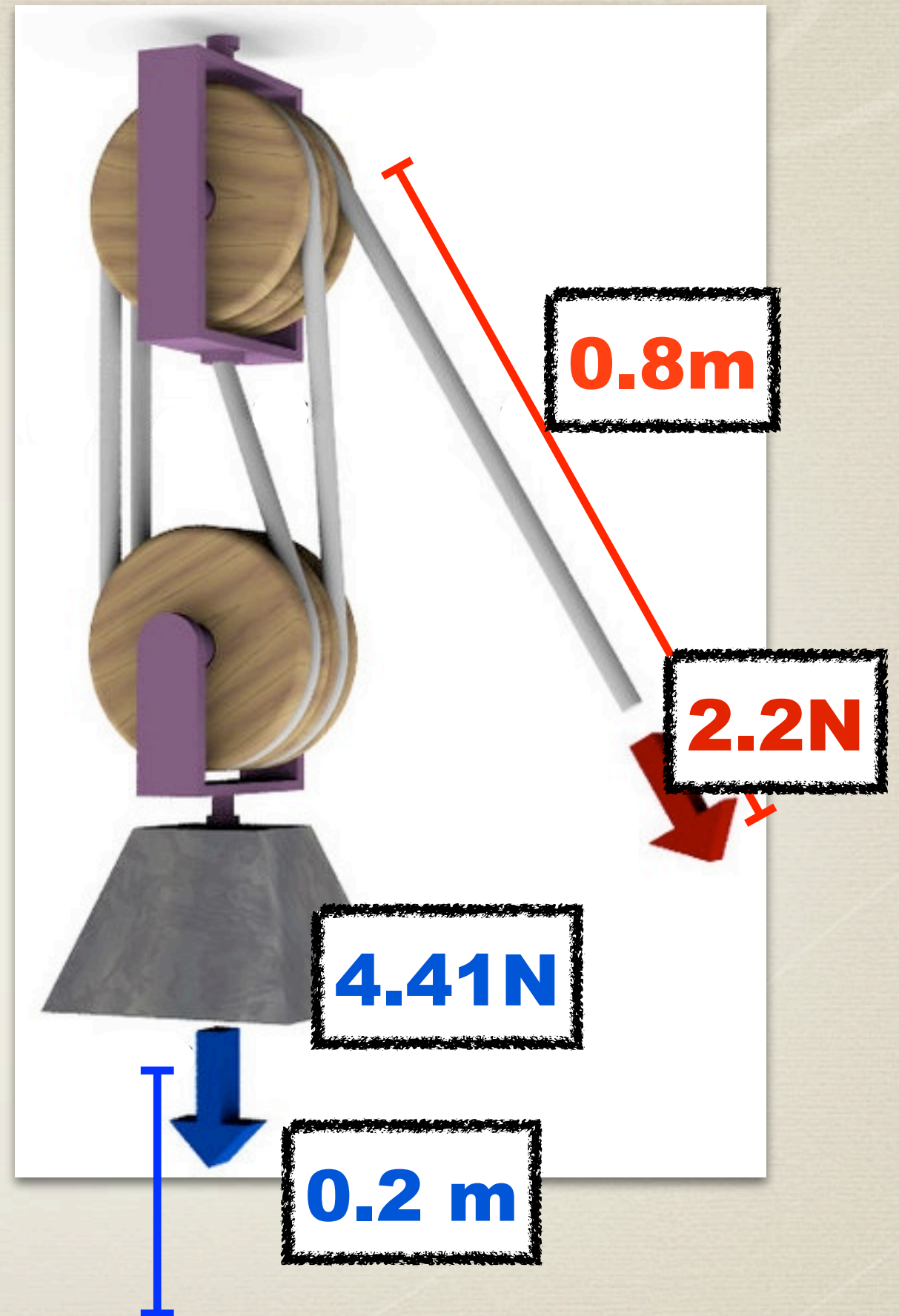
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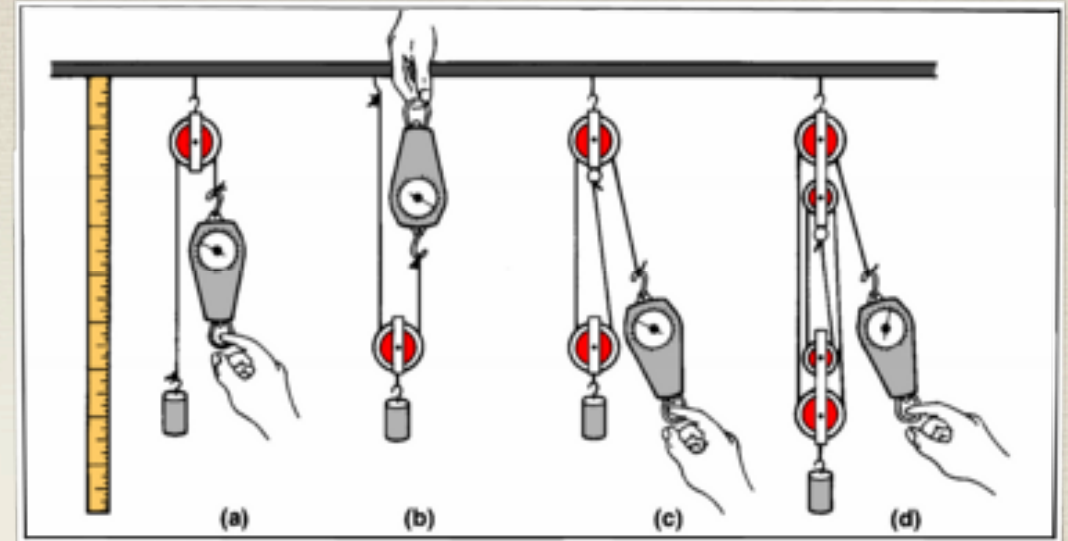
$$\text{Efficiency} = W_o / W_i$$
$$\text{Efficiency} = (0.882\text{J}) / (1.76\text{J})$$
$$\text{Efficiency} = 0.5 = 50\%$$

$$\text{Energy Lost}$$
$$1.76 - 0.882 = 0.878\text{J}$$

$$\text{Power} = W / t$$
$$\text{Power} = 1.76 / 5\text{s} = 0.352\text{W}$$



Pulley Lab



Data:		Draw the pulley arrangement	Calculations:	
mass lifted			Number of lifting strings	
Weight Lifted			Work input $F \times D$	
Height lifted			Work output $W \times H$	
mass needed			Efficiency W_o / W_i	
Force applied				
Distance				

Academic Assignment

Academic Physics

Set 1 - Chapter 10

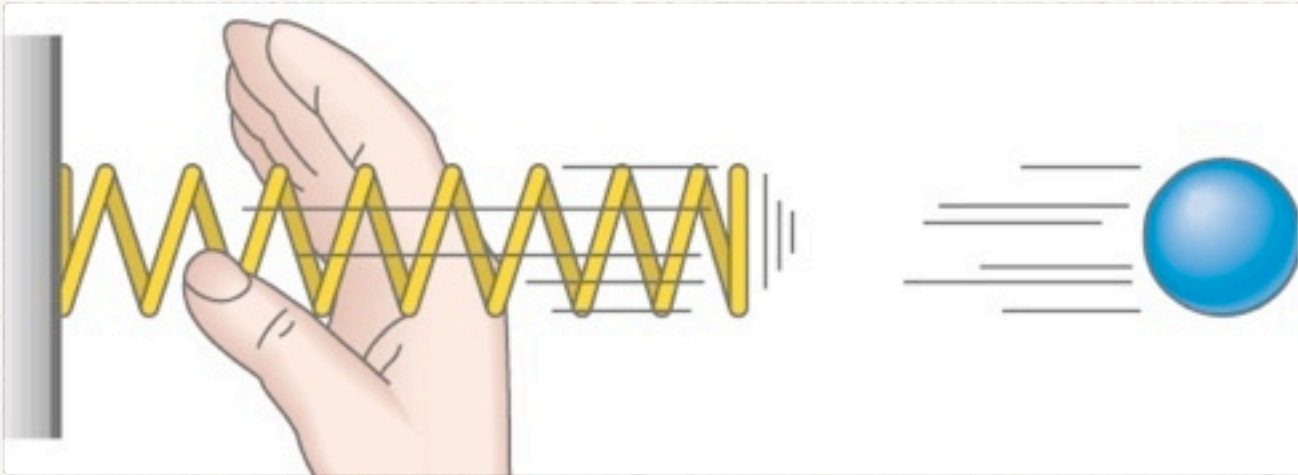
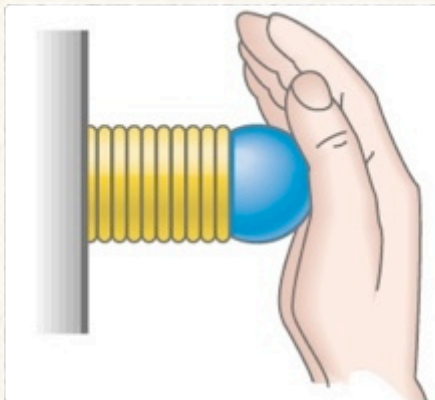
1, 2, 3, 5, 6, 7, 25, 26, 27, 28, 52, 53, 56, 57

Solving Problems with Energy

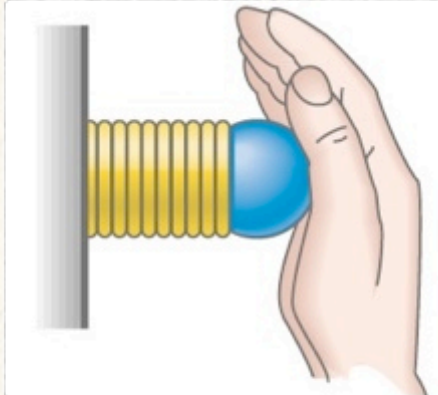
instead of old equations



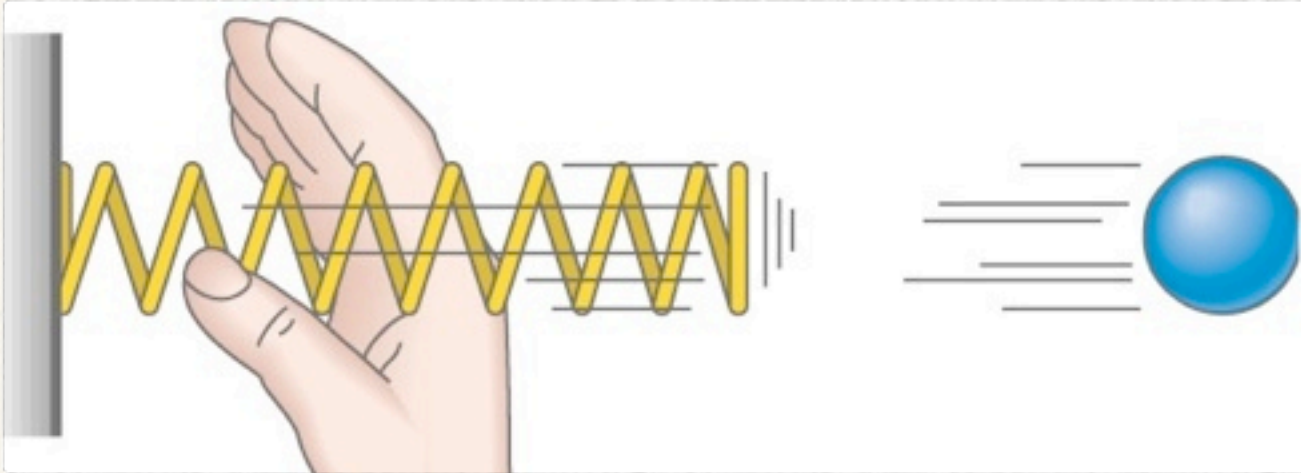
Elastic Potential Energy



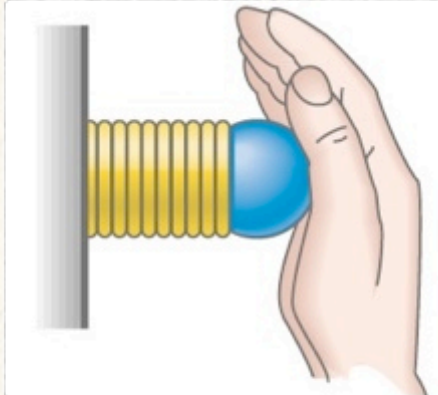
Elastic Potential Energy



► $W = F D$

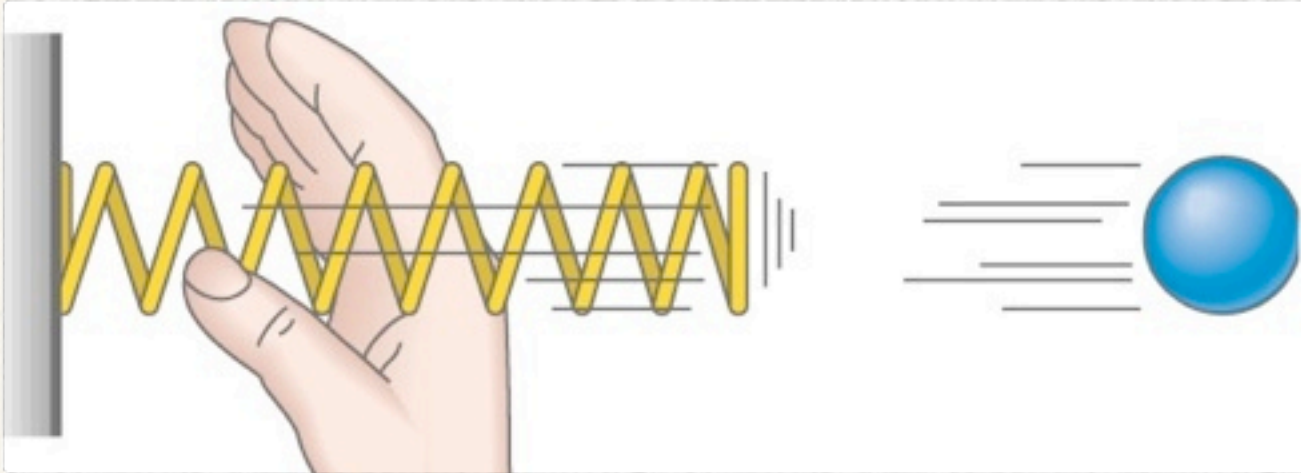


Elastic Potential Energy

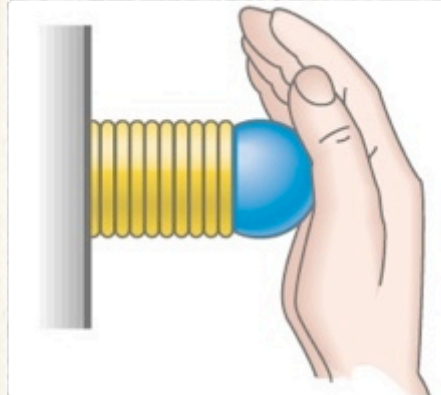


▶ $W = F D$

▶ $F = k x$



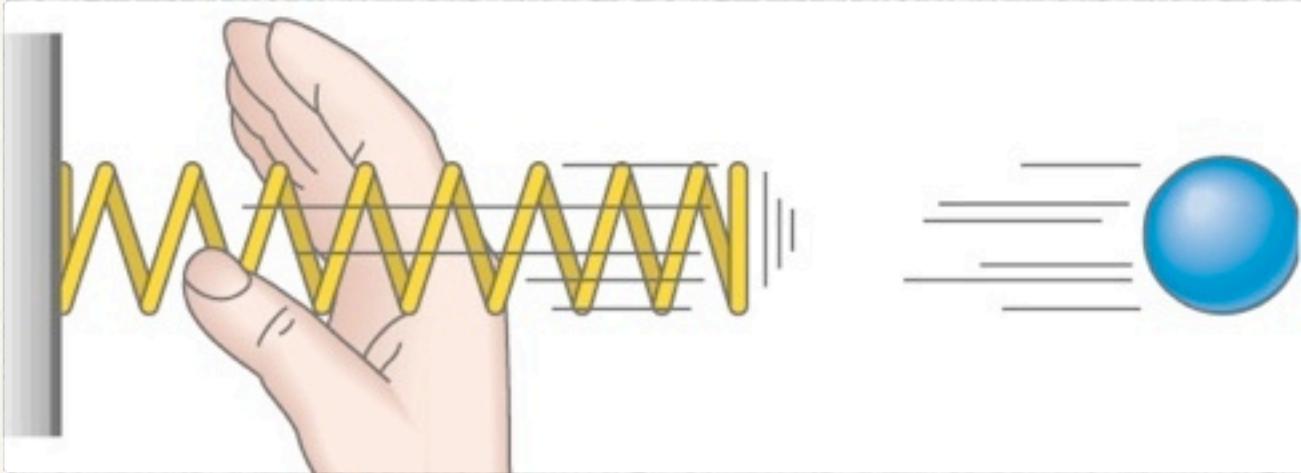
Elastic Potential Energy



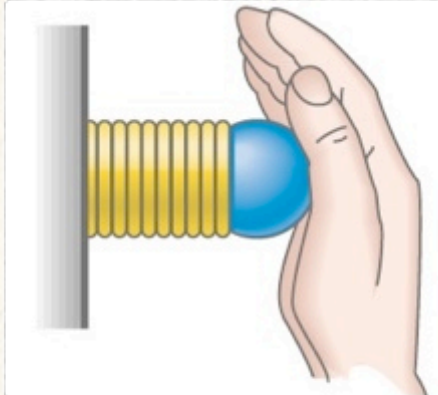
▶ $W = F D$

▶ $F = k x$

▶ $F_{\text{avg}} = \frac{1}{2} k x$



Elastic Potential Energy

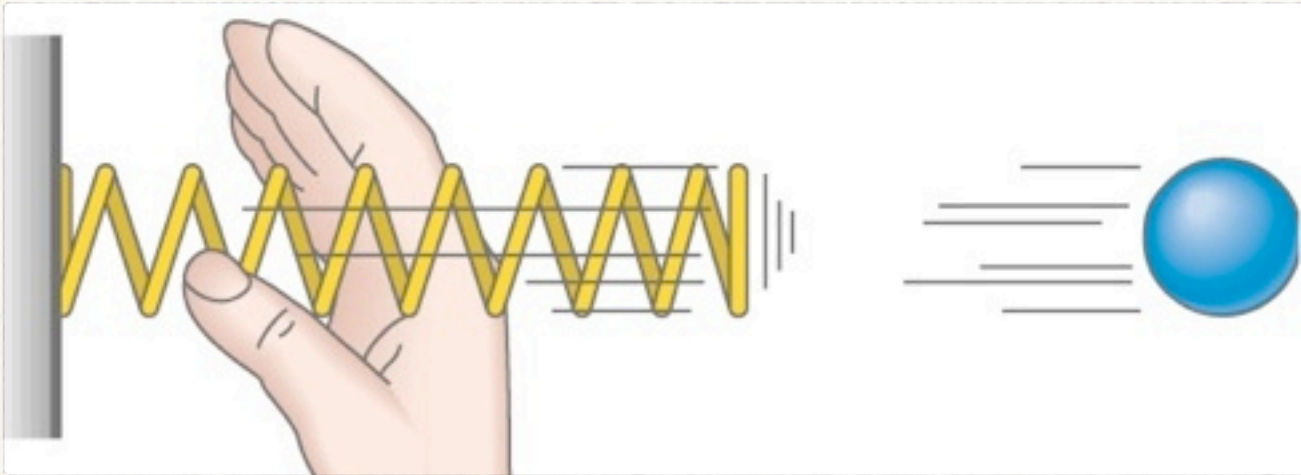


▶ $W = F D$

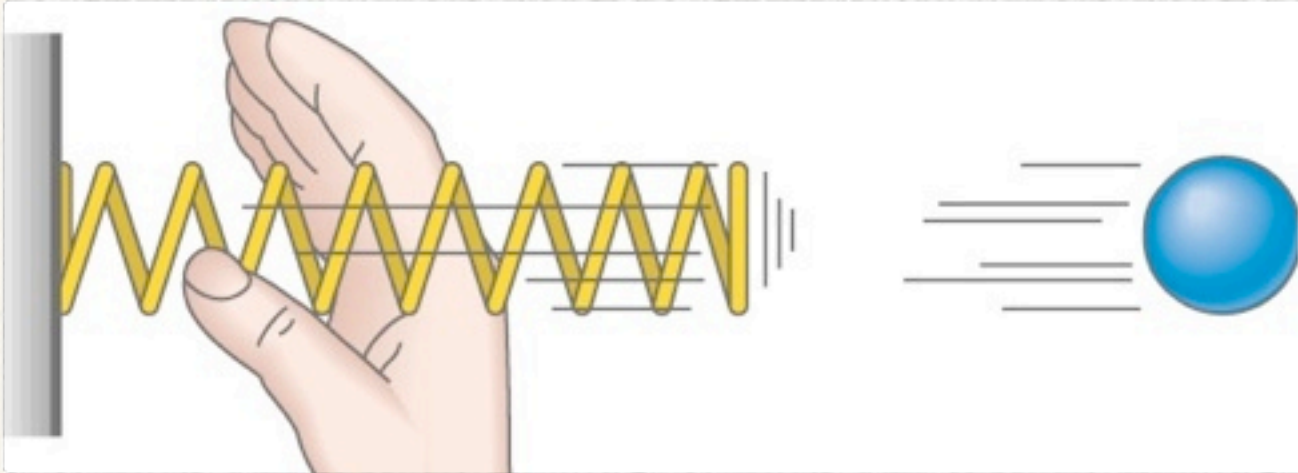
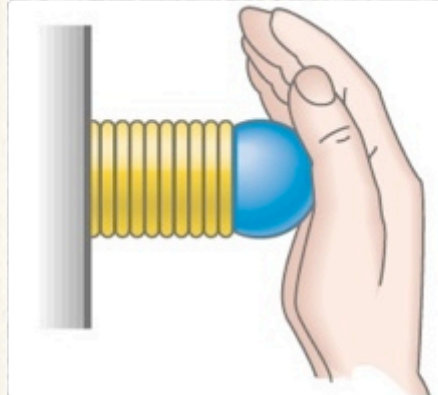
▶ $F = k x$

▶ $F_{\text{avg}} = \frac{1}{2} k x$

▶ $W = (\frac{1}{2} k x) (x)$



Elastic Potential Energy



▶ $W = F D$

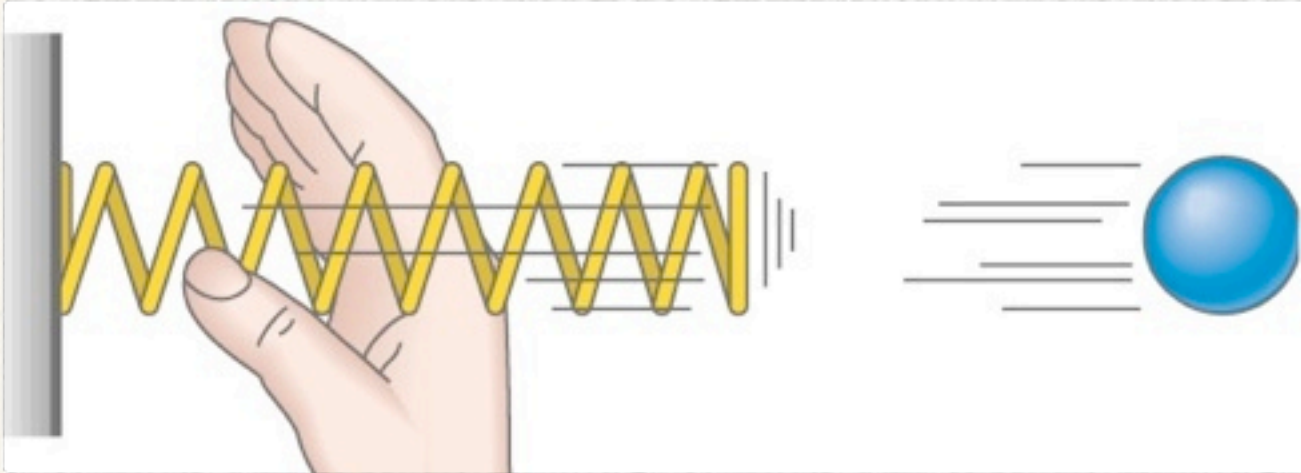
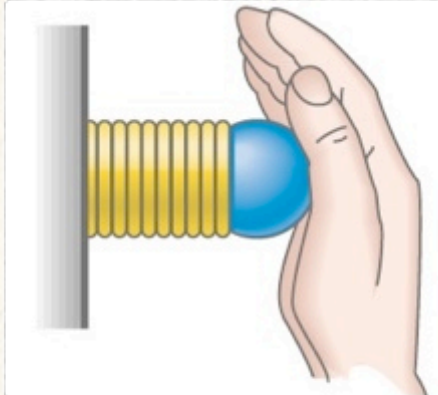
▶ $F = k x$

▶ $F_{\text{avg}} = \frac{1}{2} k x$

▶ $W = (\frac{1}{2} k x) (x)$

▶ $W = \frac{1}{2} k x^2$

Elastic Potential Energy



▶ $W = F D$

▶ $F = k x$

▶ $F_{\text{avg}} = \frac{1}{2} k x$

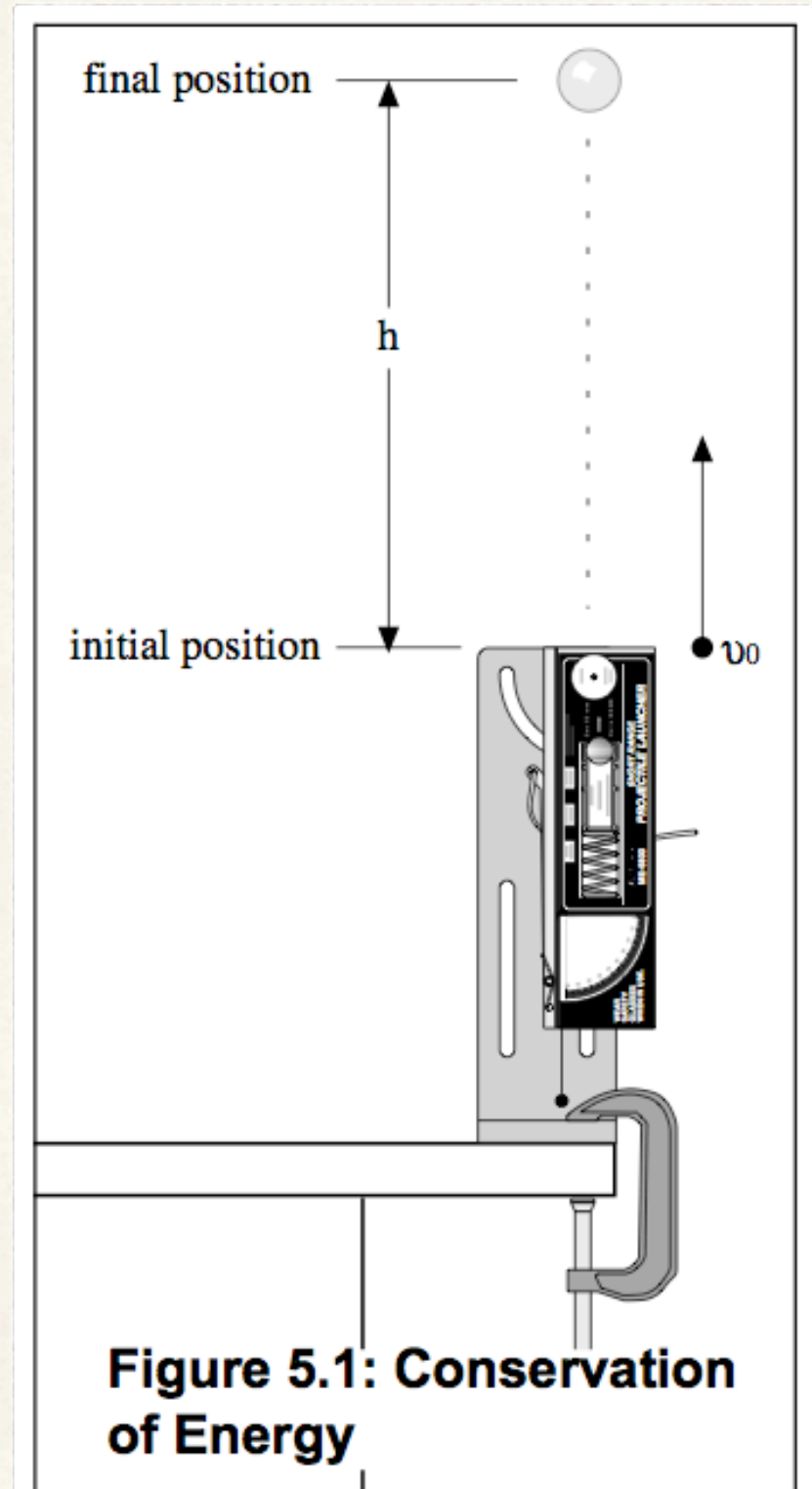
▶ $W = (\frac{1}{2} k x) (x)$

▶ $W = \frac{1}{2} k x^2$

▶ $PE = \frac{1}{2} k x^2$

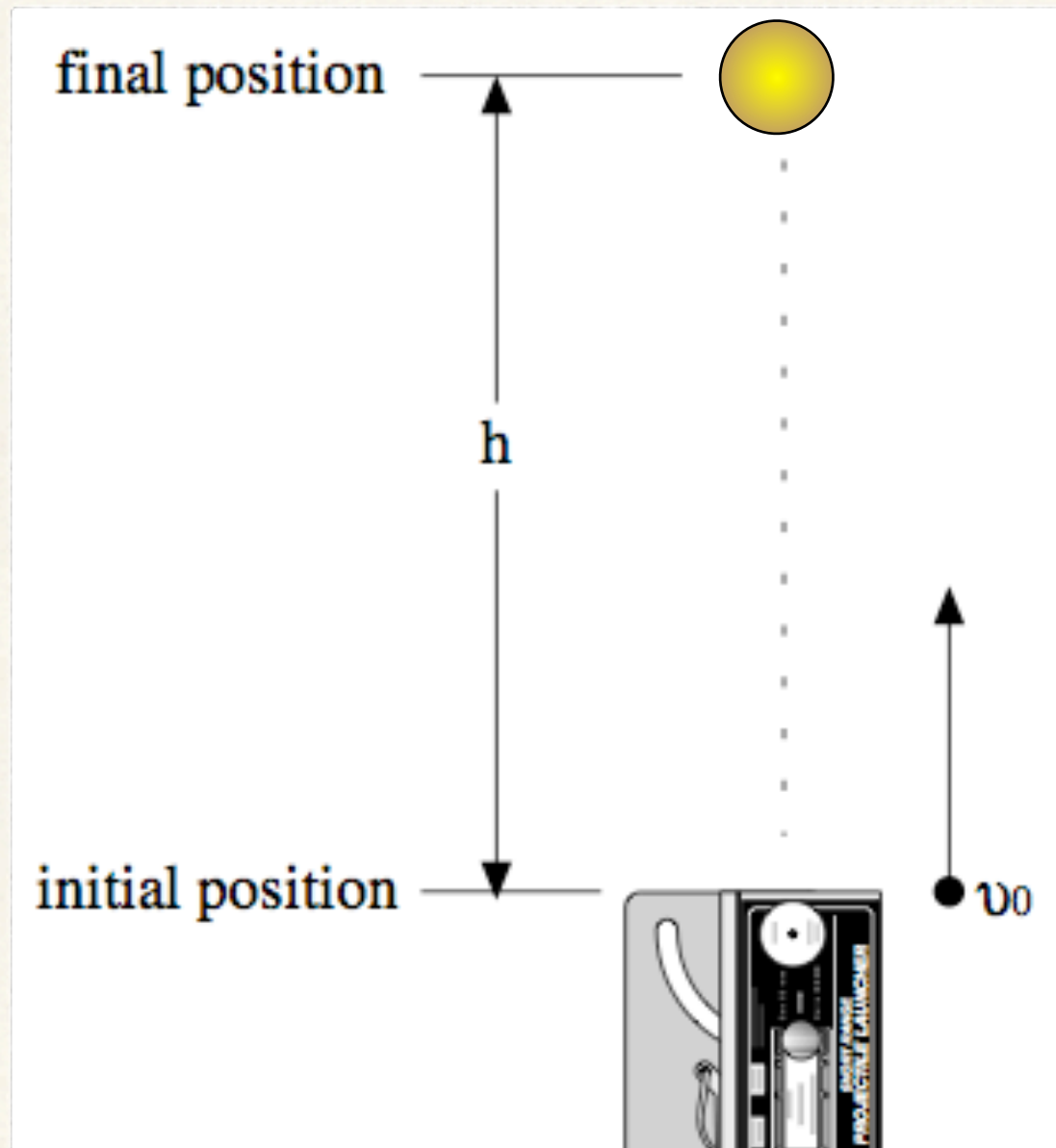
Elastic Potential

- ▶ In an earlier lab, you compressed a spring to “two clicks” or a distance of 6cm. The 10g ball went up 1.08m when launched at 90°.
- ▶ Find the PE at the top
- ▶ Find the Spring Constant k
- ▶ Find the KE at the top of the cannon, and the maximum velocity of the ball
- ▶ Find the maximum force used to push the spring



Elastic Potential

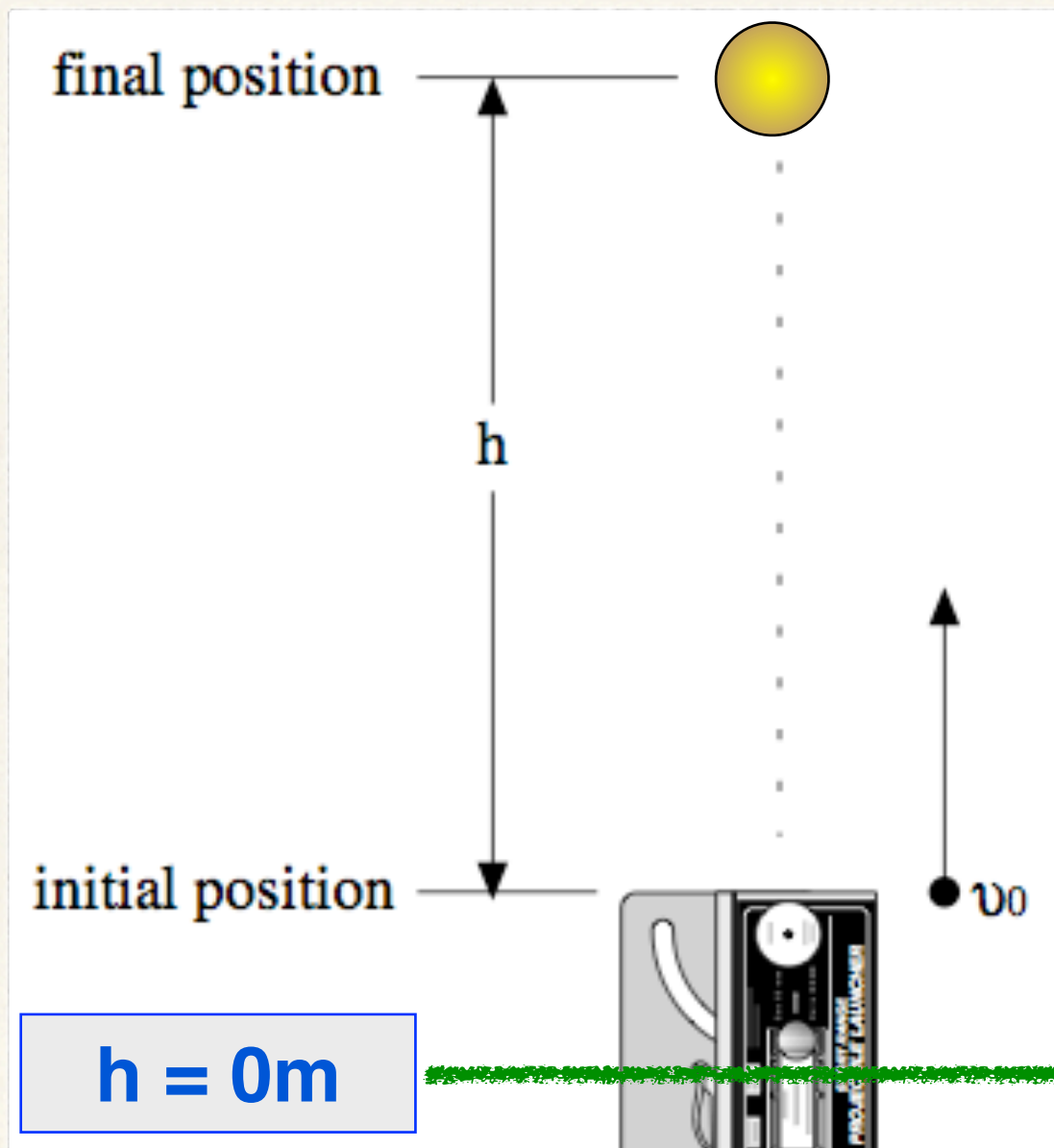
- ▶ In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- ▶ Find the PE at the top
- ▶ Find the Spring Constant k
- ▶ Find the KE at the top of the cannon, and the maximum velocity of the ball
- ▶ Find the maximum force used to push the spring

Elastic Potential

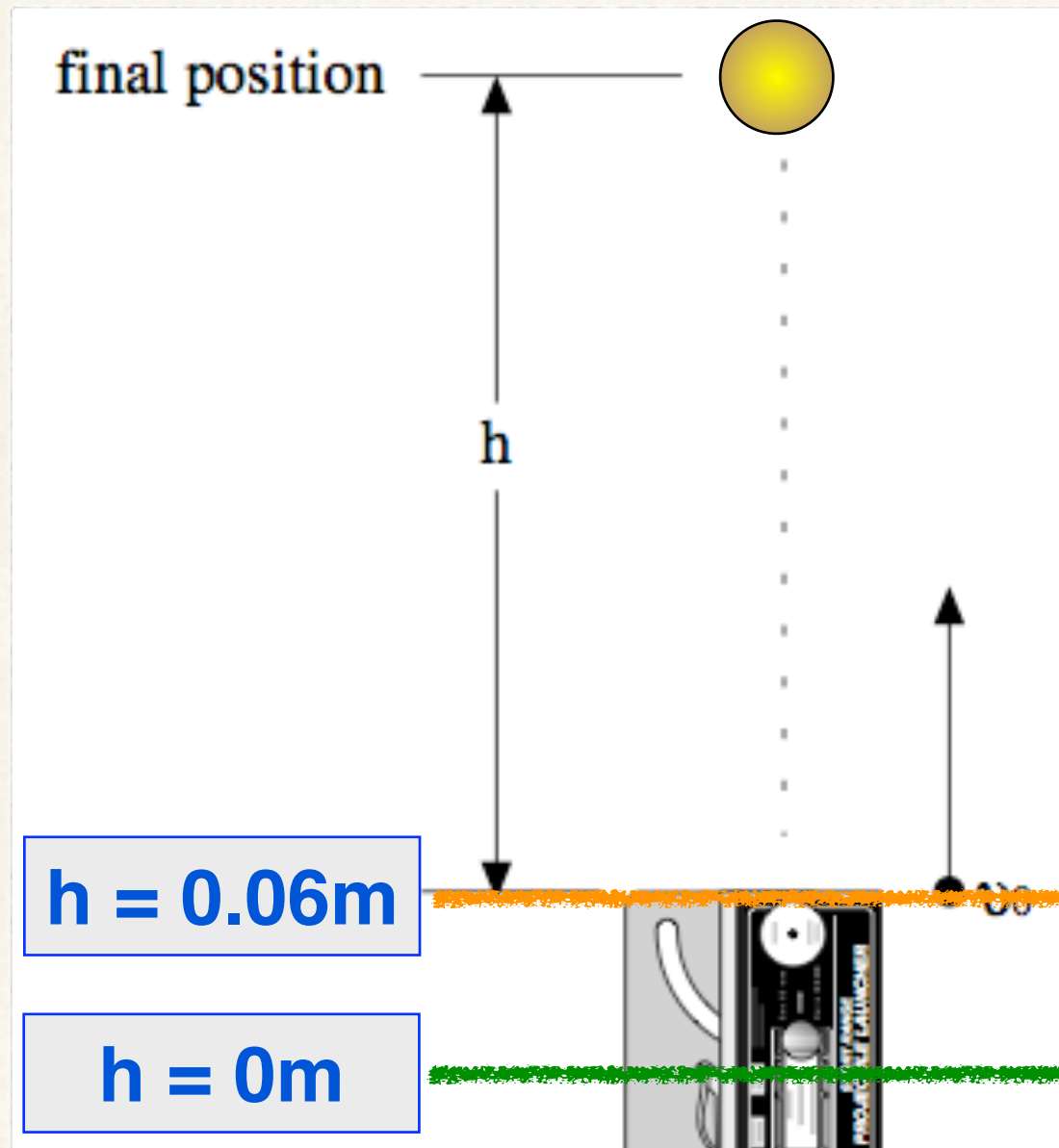
- ▶ In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- ▶ Find the PE at the top
- ▶ Find the Spring Constant k
- ▶ Find the KE at the top of the cannon, and the maximum velocity of the ball
- ▶ Find the maximum force used to push the spring

Elastic Potential

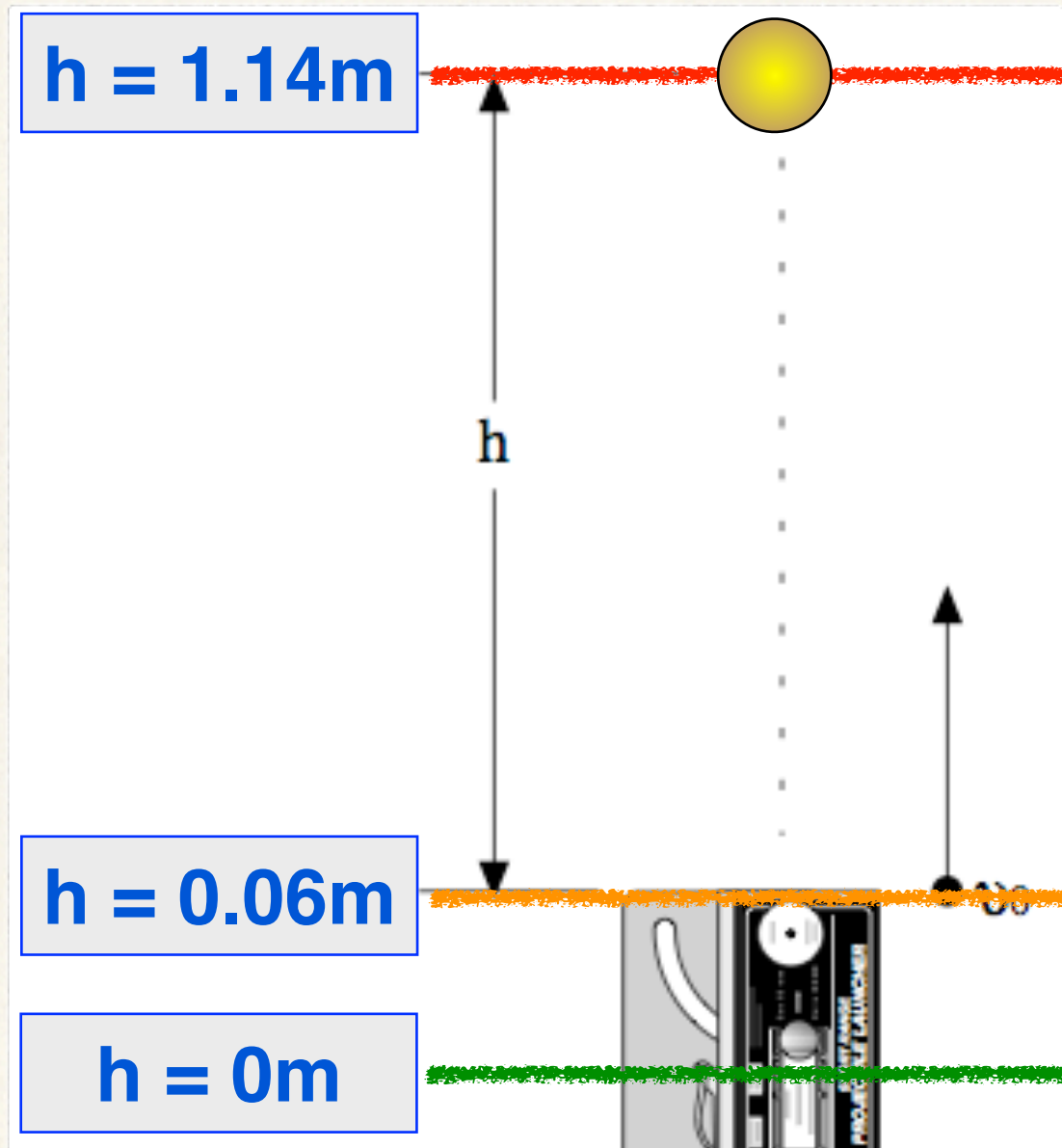
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- ▶ Find the PE at the top
- ▶ Find the Spring Constant k
- ▶ Find the KE at the top of the cannon, and the maximum velocity of the ball
- ▶ Find the maximum force used to push the spring

Elastic Potential

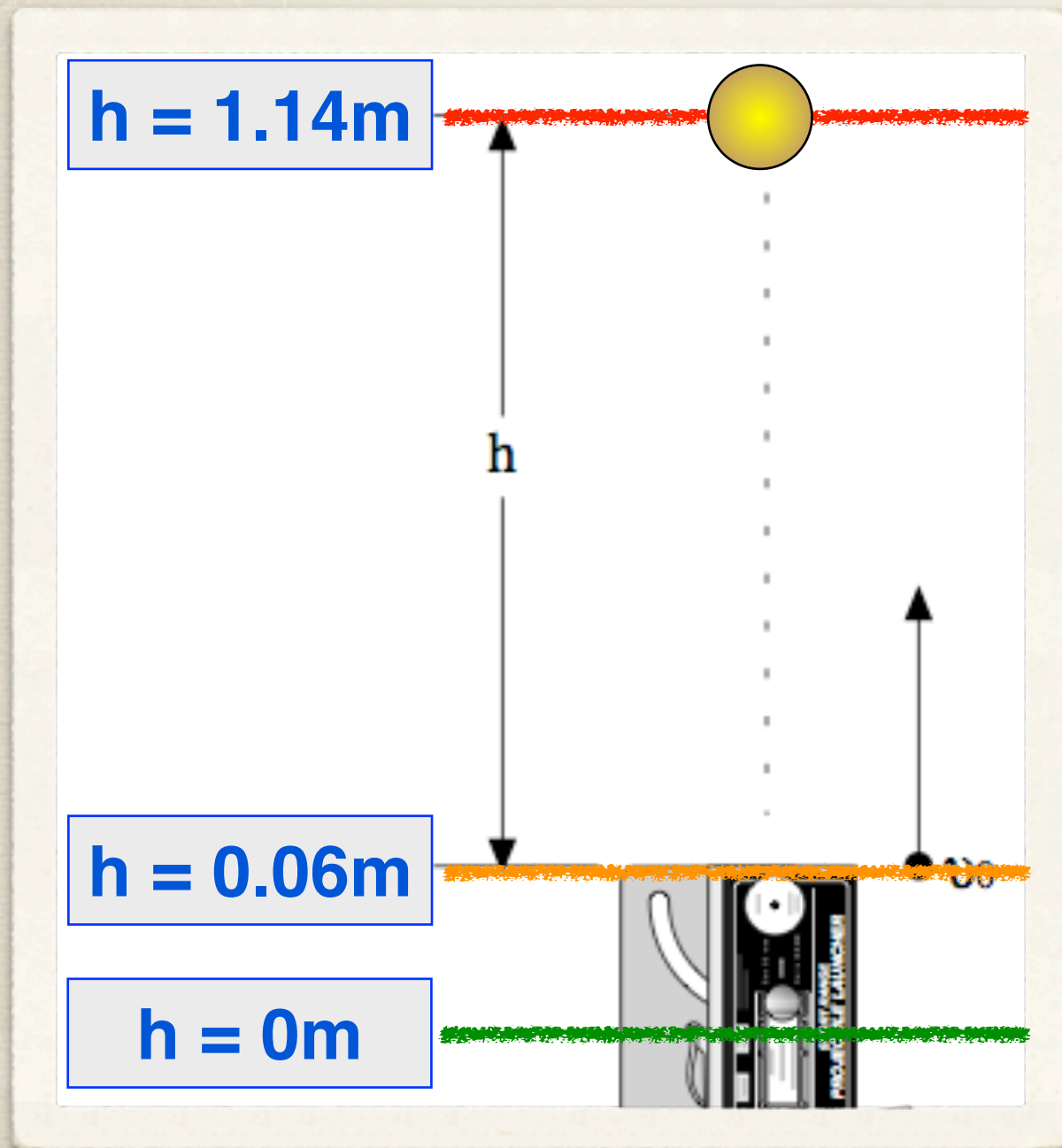
- ▶ In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- ▶ Find the PE at the top
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- ▶ Find the KE at the top of the cannon, and the maximum velocity of the ball
- ▶ Find the maximum force used to push the spring

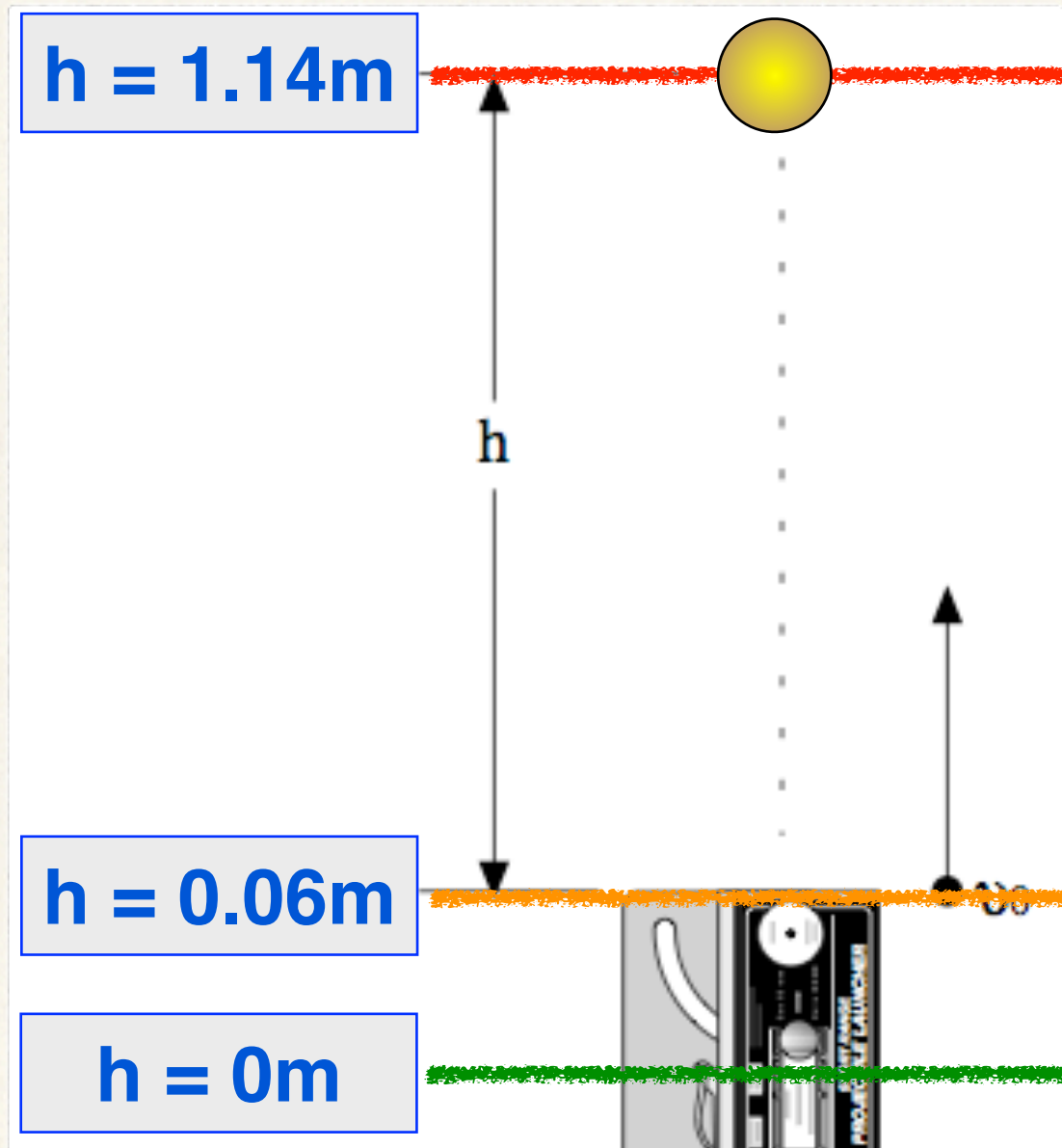
Elastic Potential

- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



Elastic Potential

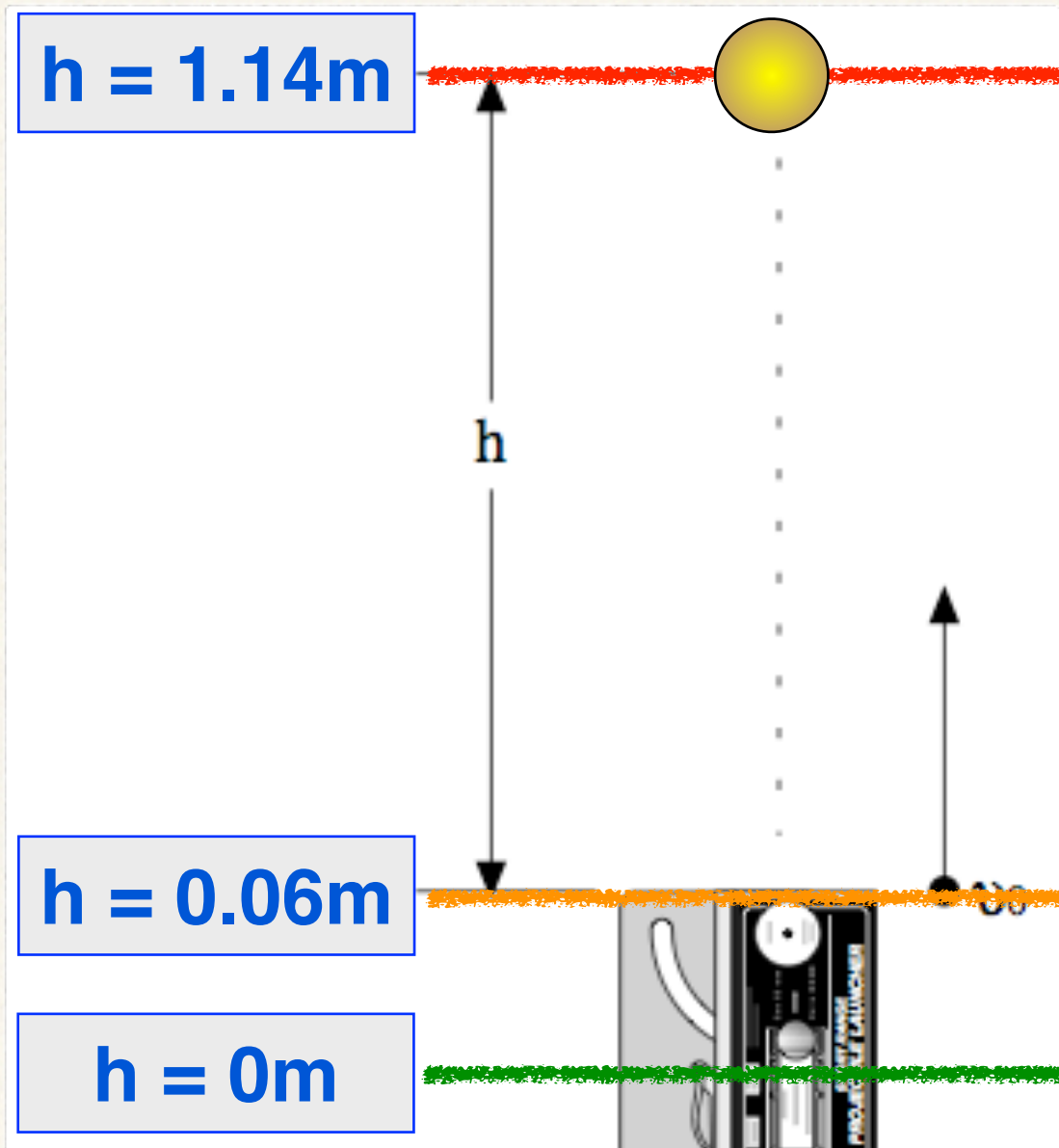
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- Find the PE at the top

Elastic Potential

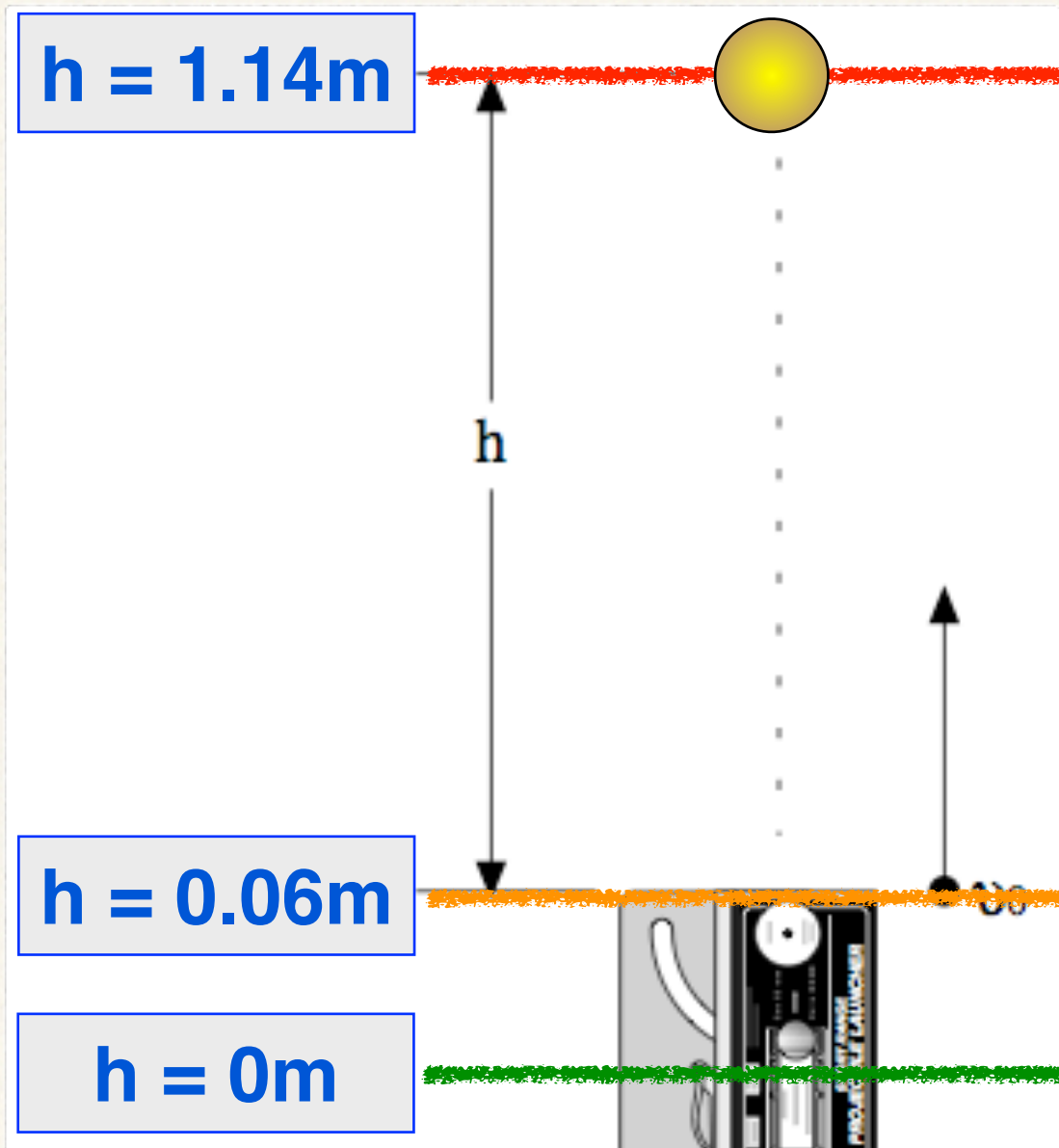
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- Find the PE at the top
- $PE = mgh$

Elastic Potential

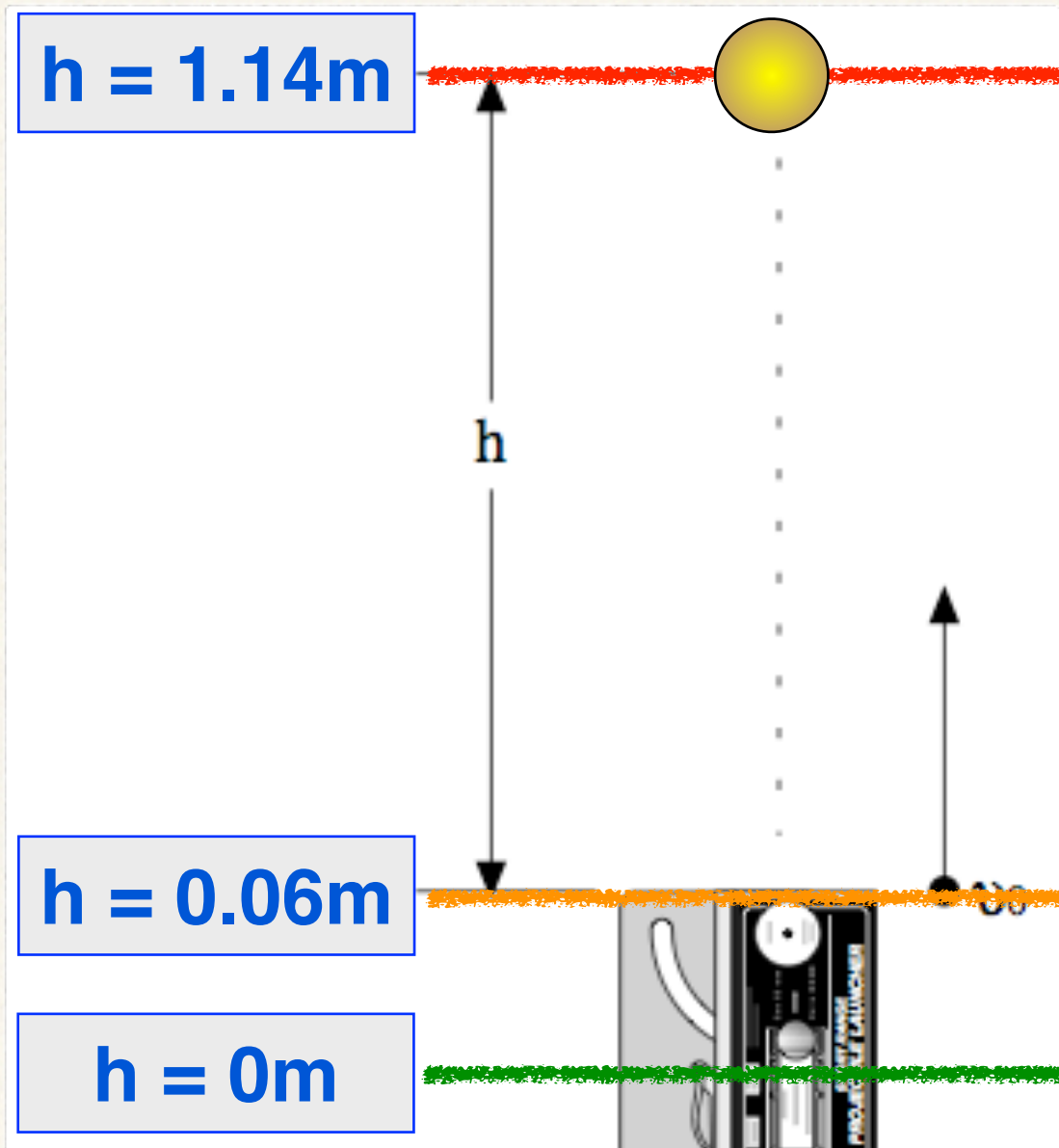
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- Find the PE at the top
- $PE = mgh$
- $PE = (0.010\text{kg})(9.8)(1.14)$

Elastic Potential

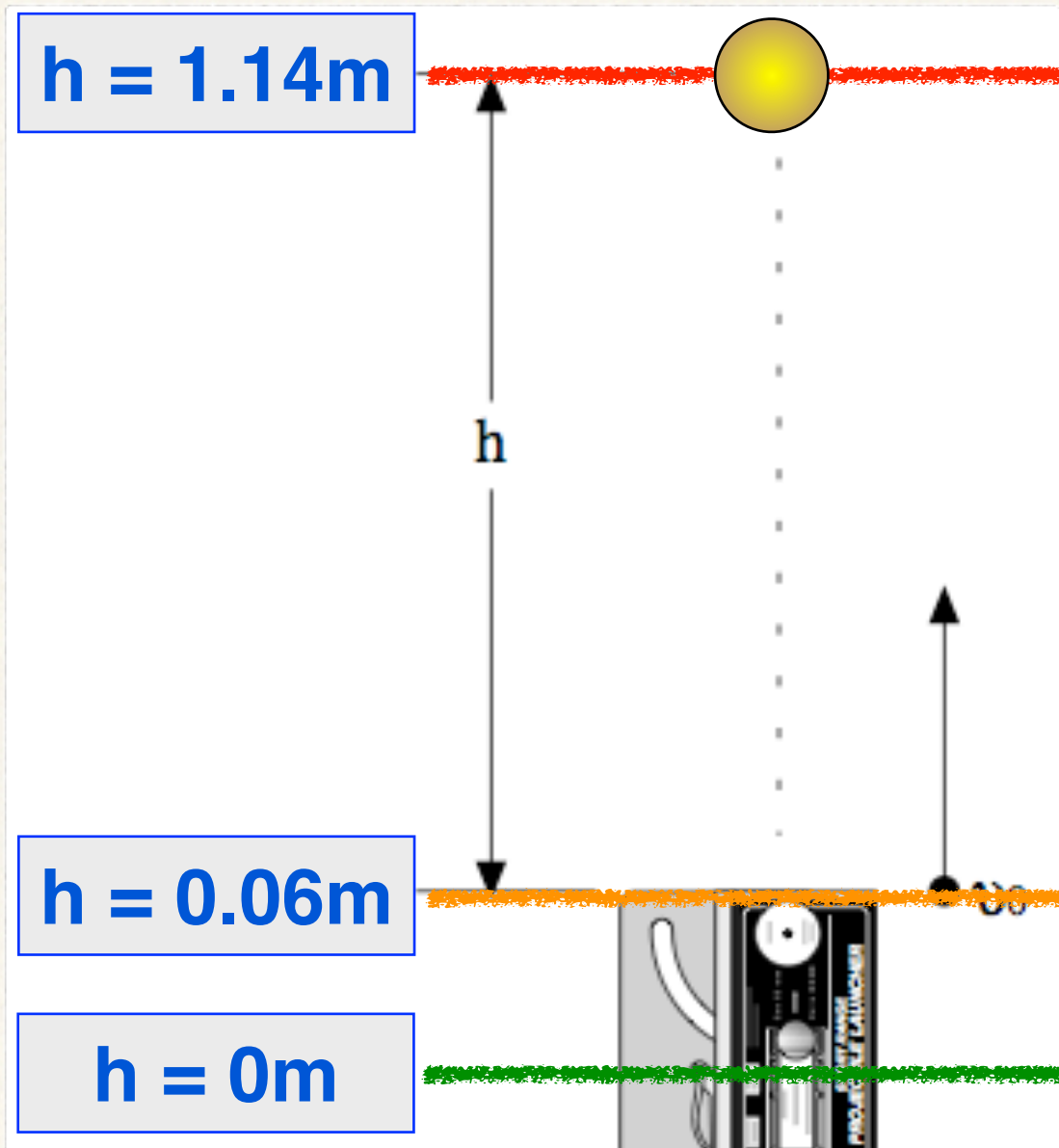
- ▶ In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- ▶ Find the PE at the top
- ▶ $PE = mgh$
- ▶ $PE = (0.010\text{kg})(9.8)(1.14)$
- ▶ $PE = 0.1117\text{J}$

Elastic Potential

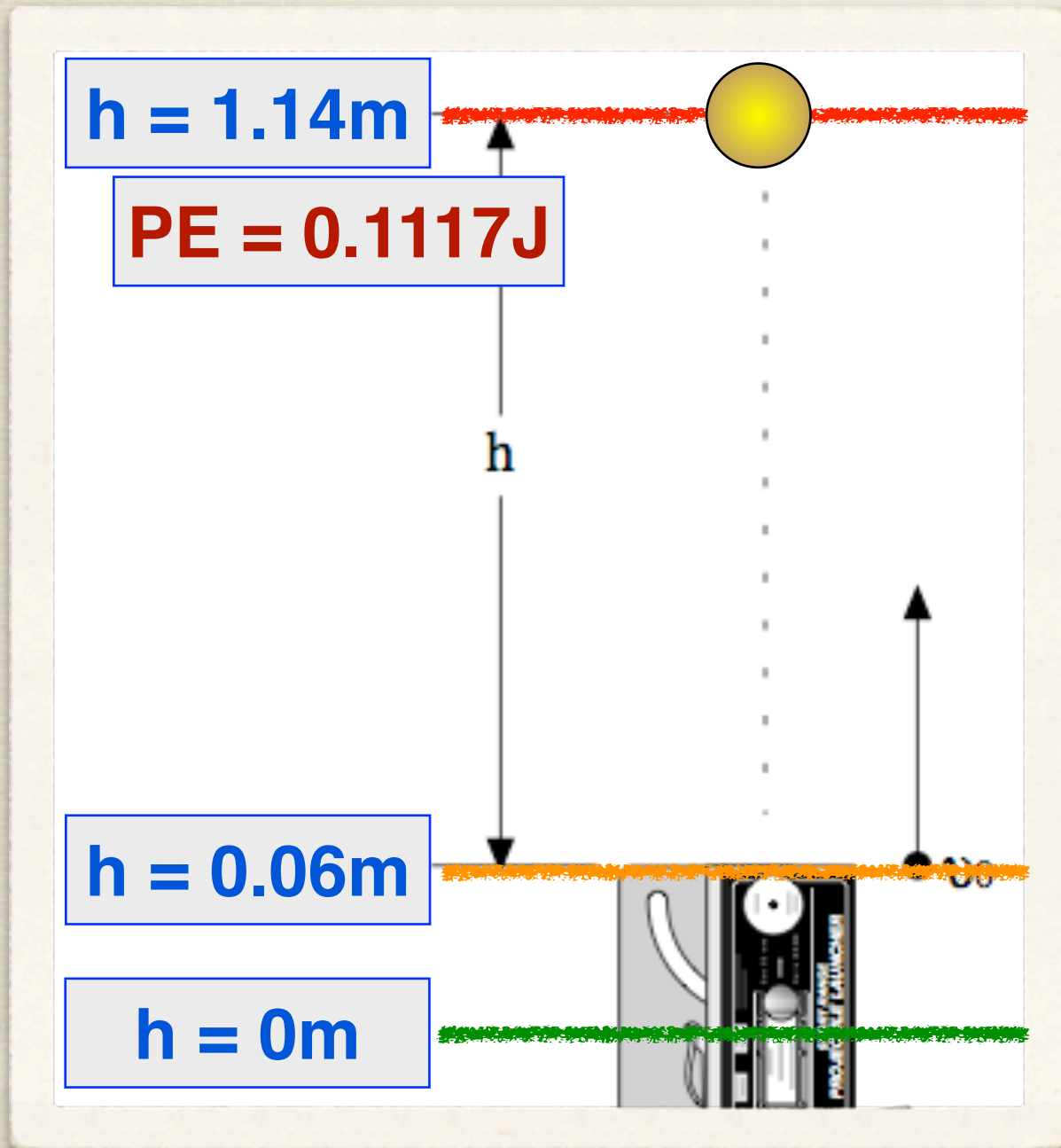
- ▶ In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- ▶ Find the PE at the top
- ▶ $PE = mgh$
- ▶ $PE = (0.010\text{kg})(9.8)(1.14)$
- ▶ $PE = 0.1117\text{J}$
- ▶ $TE = 0.1117\text{J}$

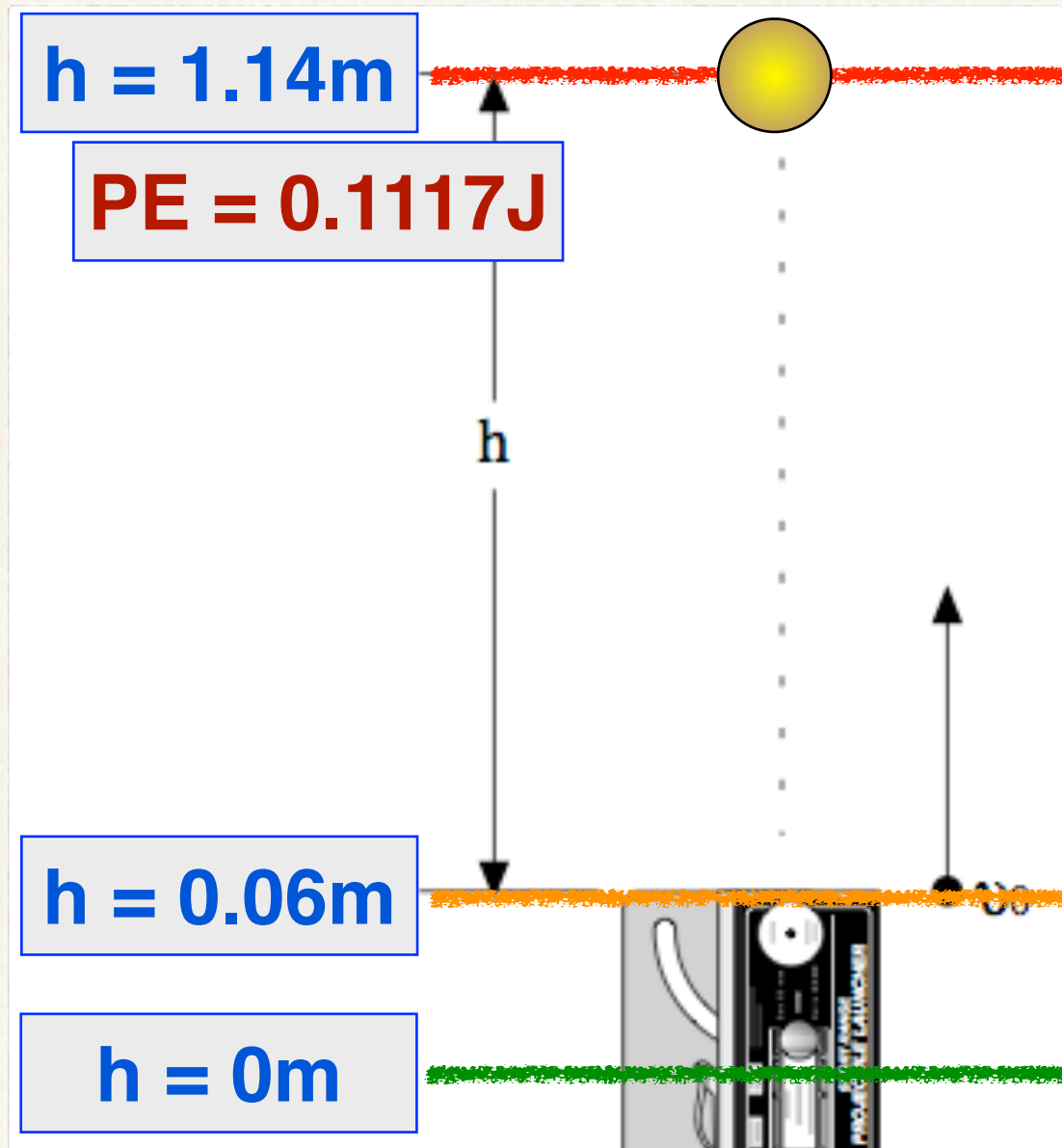
Elastic Potential

- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



Elastic Potential

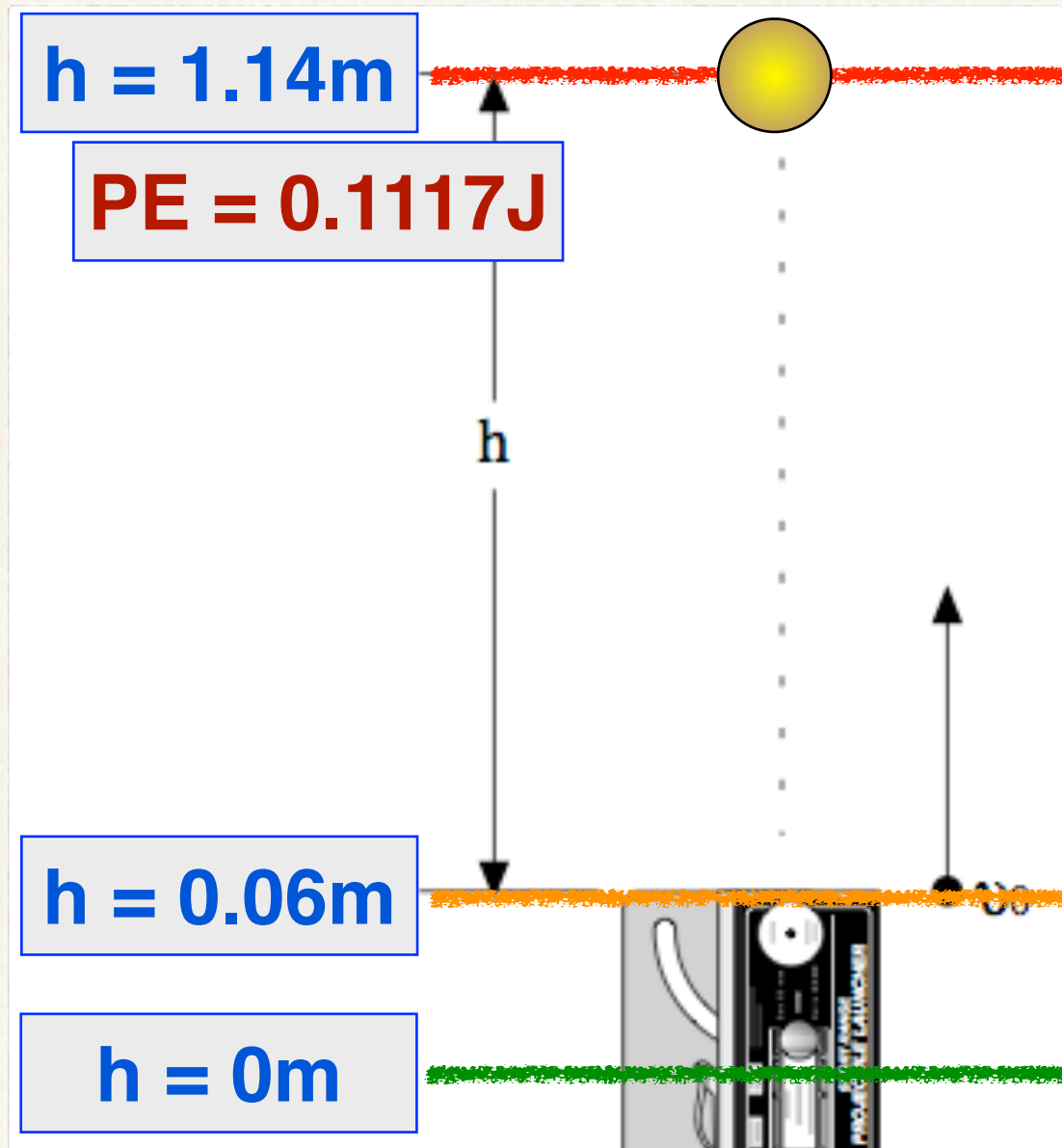
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- Find the Spring Constant k

Elastic Potential

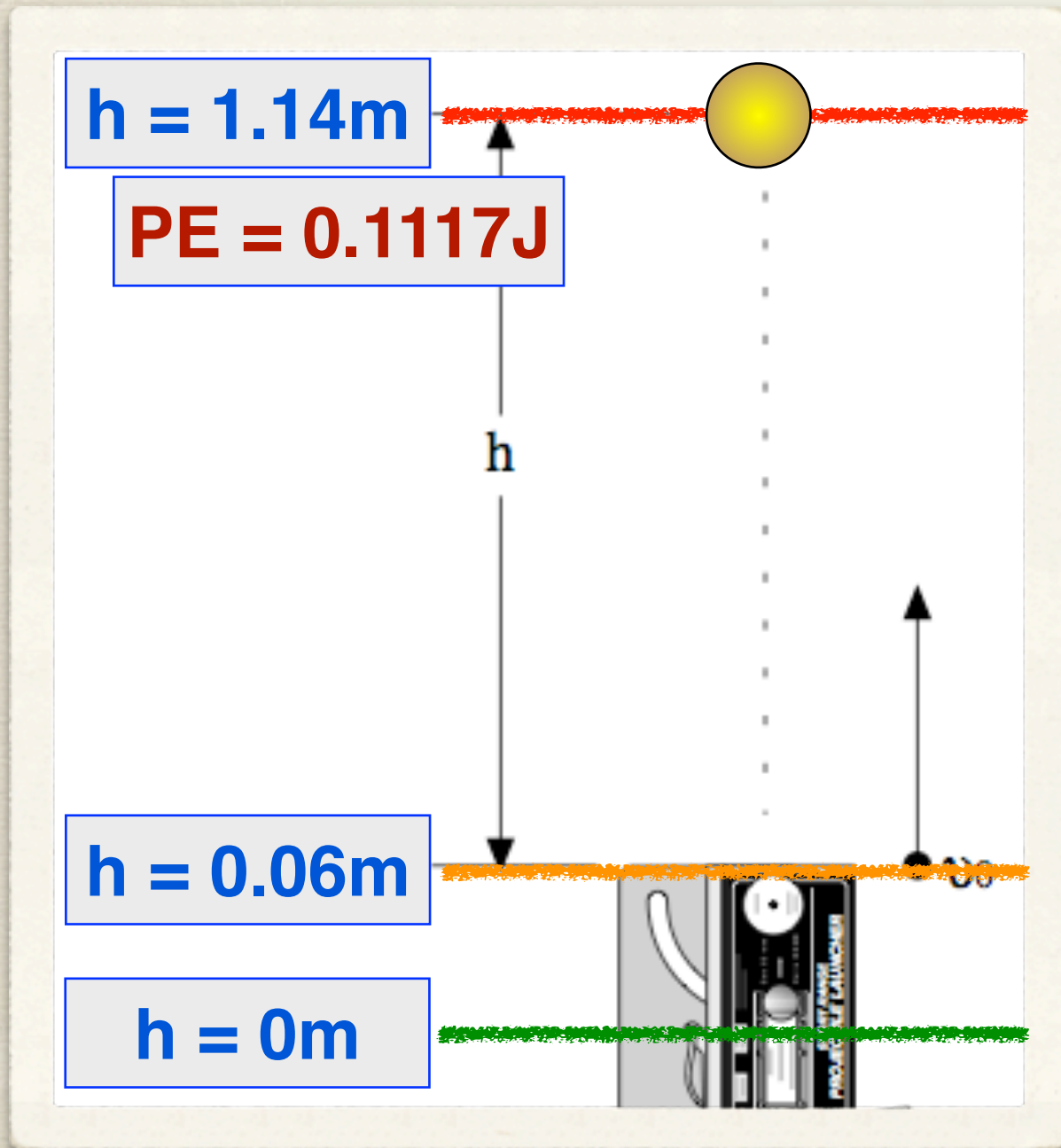
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- Find the Spring Constant k
- Elastic $PE = \frac{1}{2}kx^2$

Elastic Potential

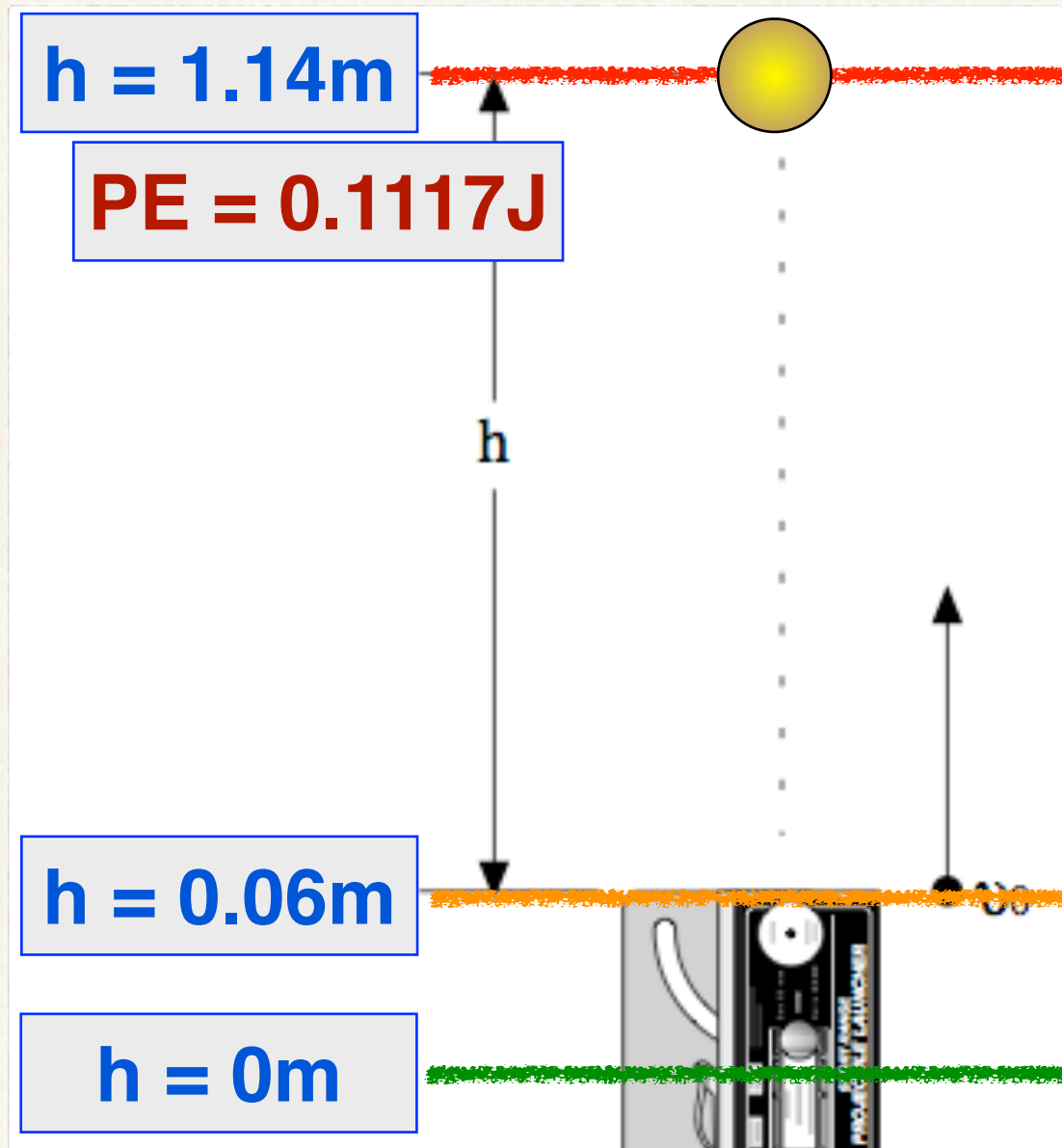
- ▶ In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- ▶ Find the Spring Constant k
- ▶ Elastic $PE = \frac{1}{2}kx^2$
- ▶ $0.1117\text{J} = \frac{1}{2} k (0.06)^2$

Elastic Potential

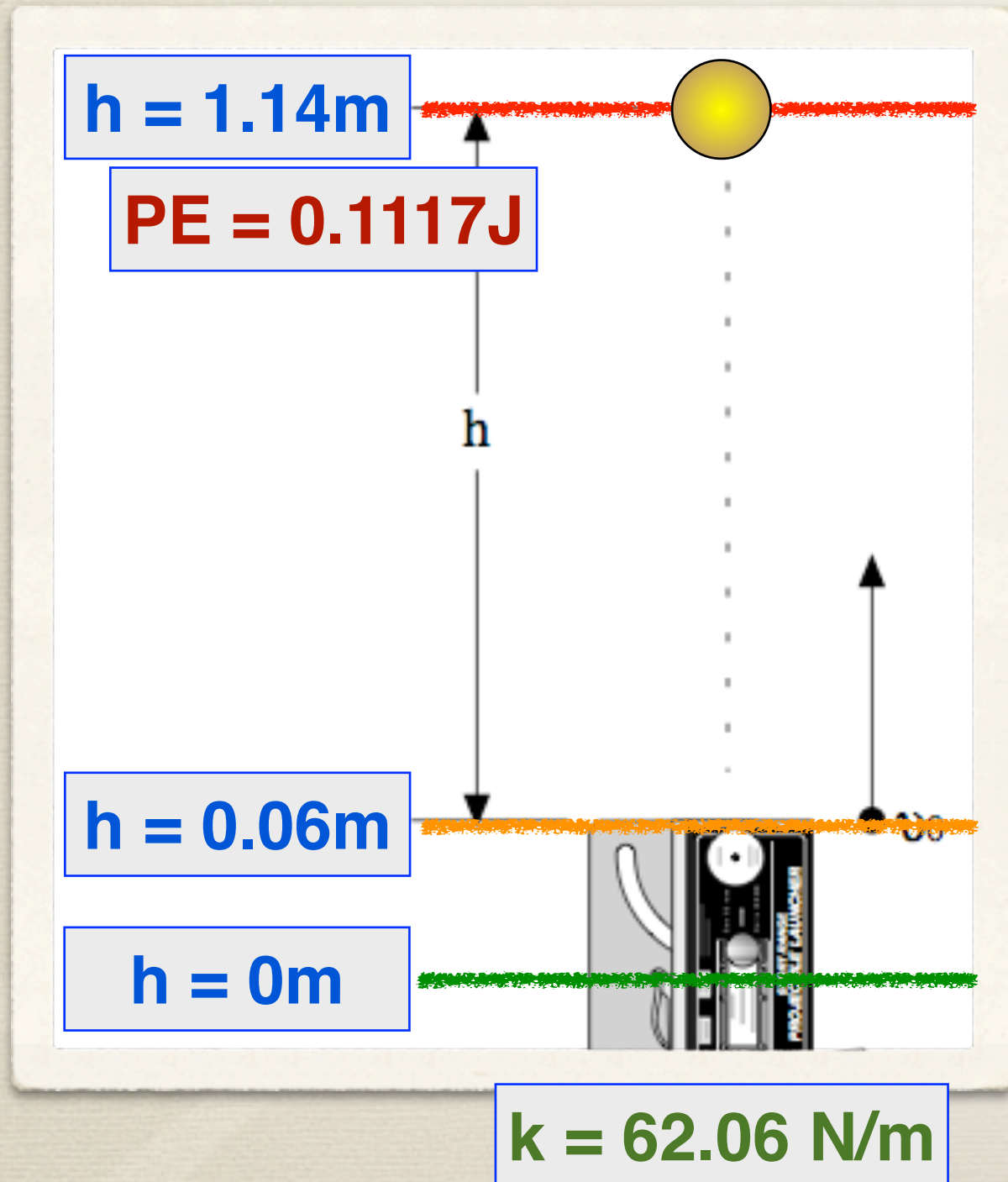
- ▶ In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- ▶ Find the Spring Constant k
- ▶ Elastic PE = $\frac{1}{2}kx^2$
- ▶ $0.1117\text{J} = \frac{1}{2} k (0.06)^2$
- ▶ $k = 62.06 \text{ N/m}$

Elastic Potential

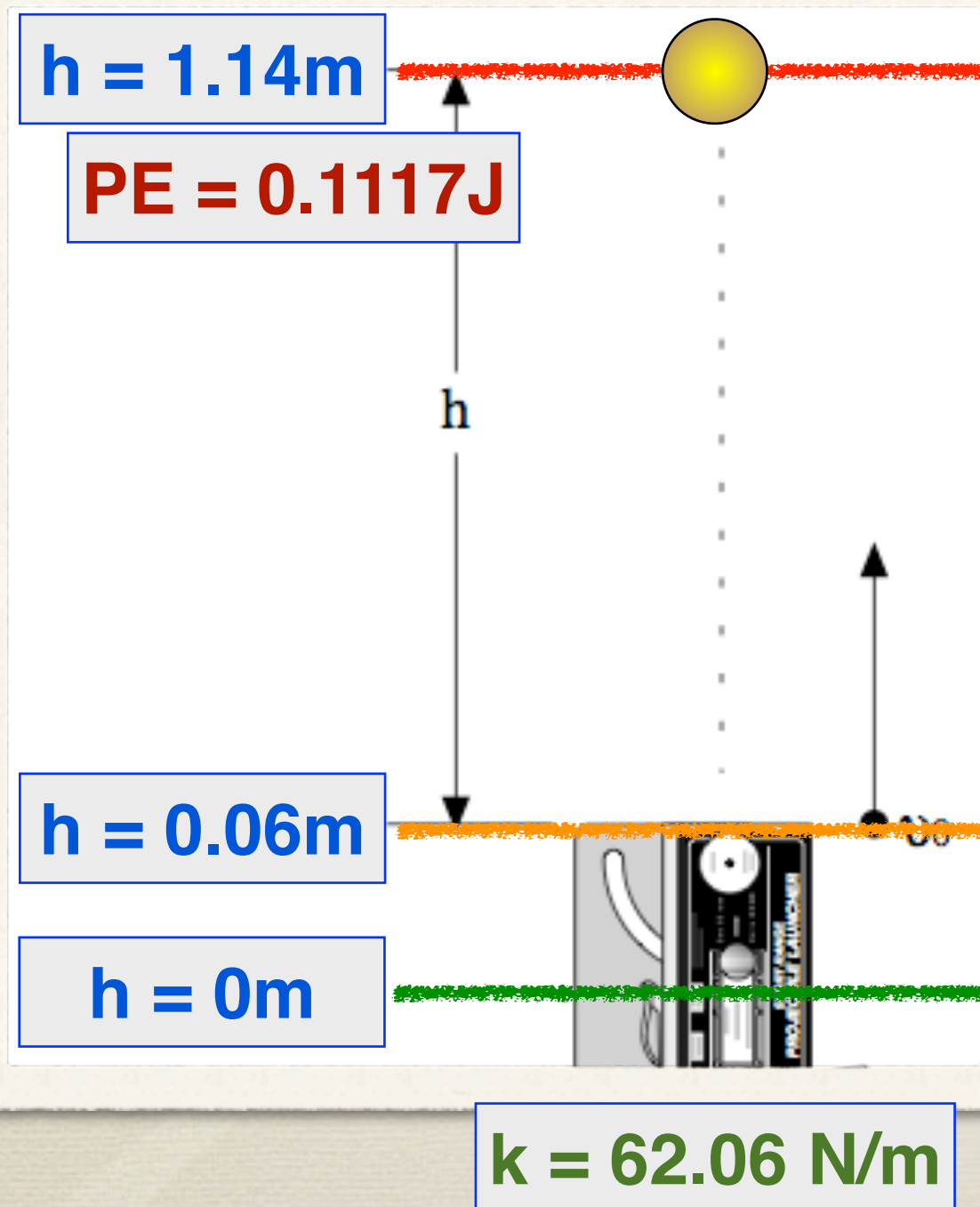
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



Elastic Potential

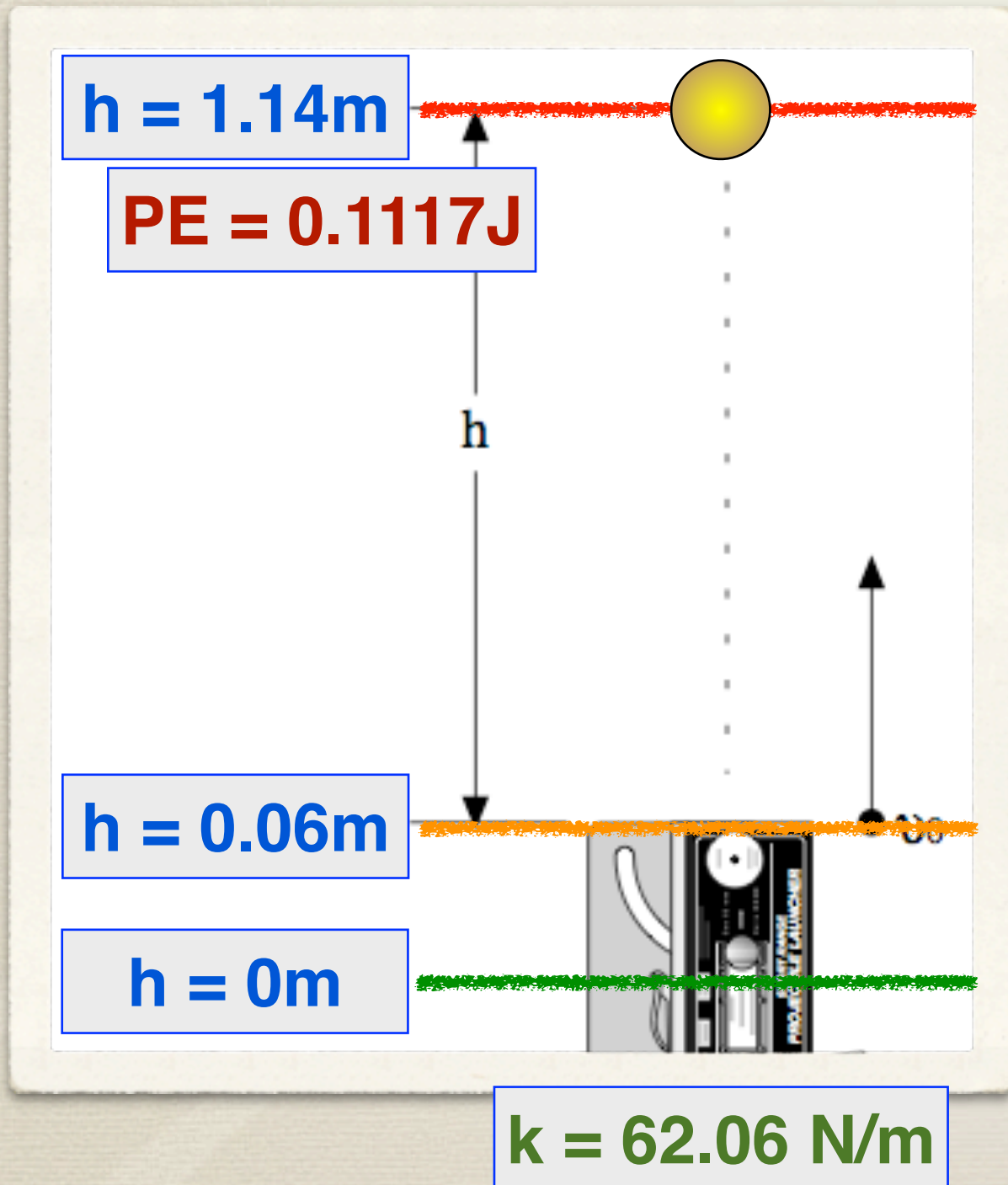
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.

- Find the KE and the velocity



Elastic Potential

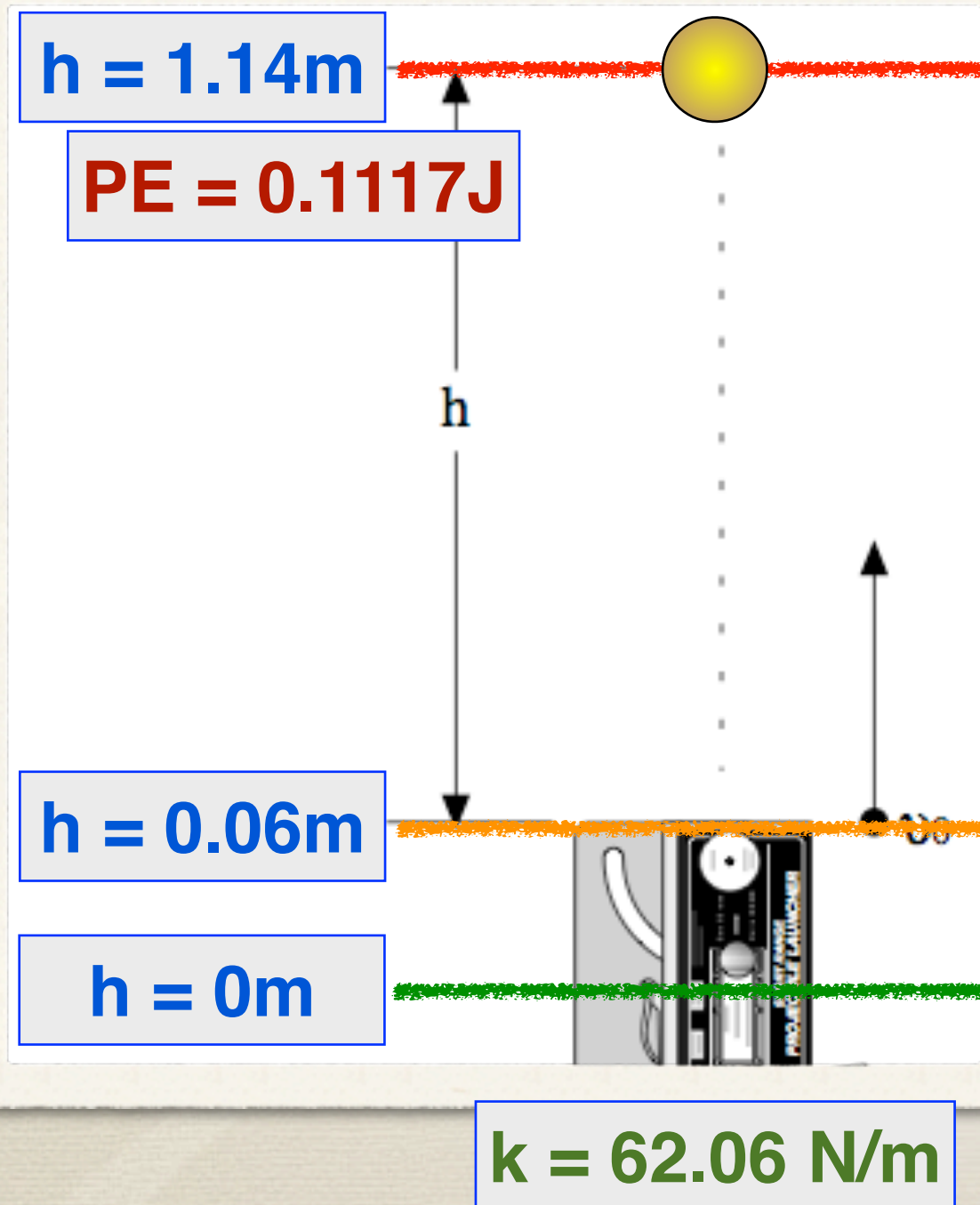
- ▶ In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- ▶ Find the KE and the velocity
- ▶ $PE = (0.010\text{kg})(9.8)(0.06)$

Elastic Potential

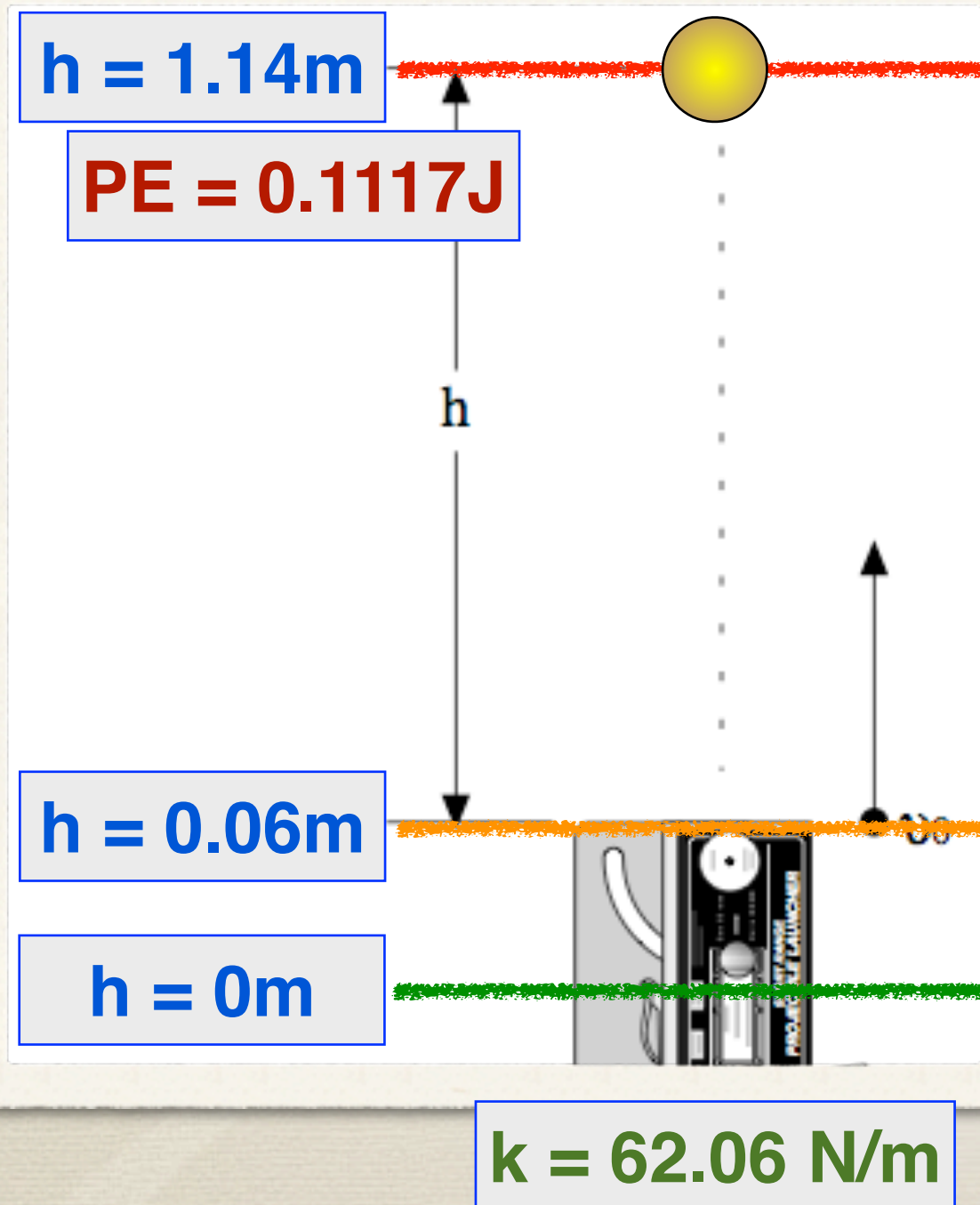
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- Find the KE and the velocity
- $PE = (0.010\text{kg})(9.8)(0.06)$
- $PE = 0.00588 \text{ J} = 5.88 \text{ mJ}$

Elastic Potential

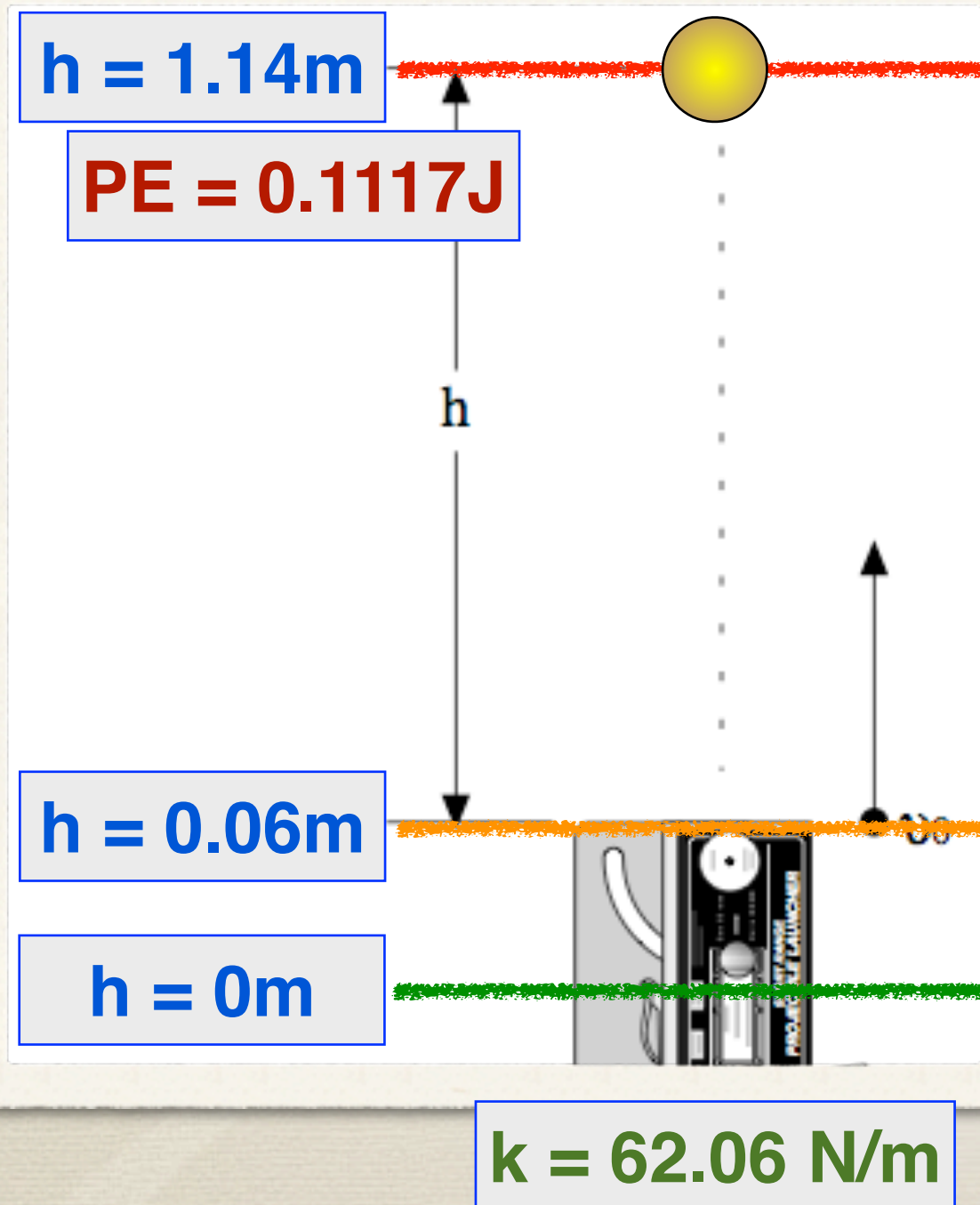
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Elastic Potential

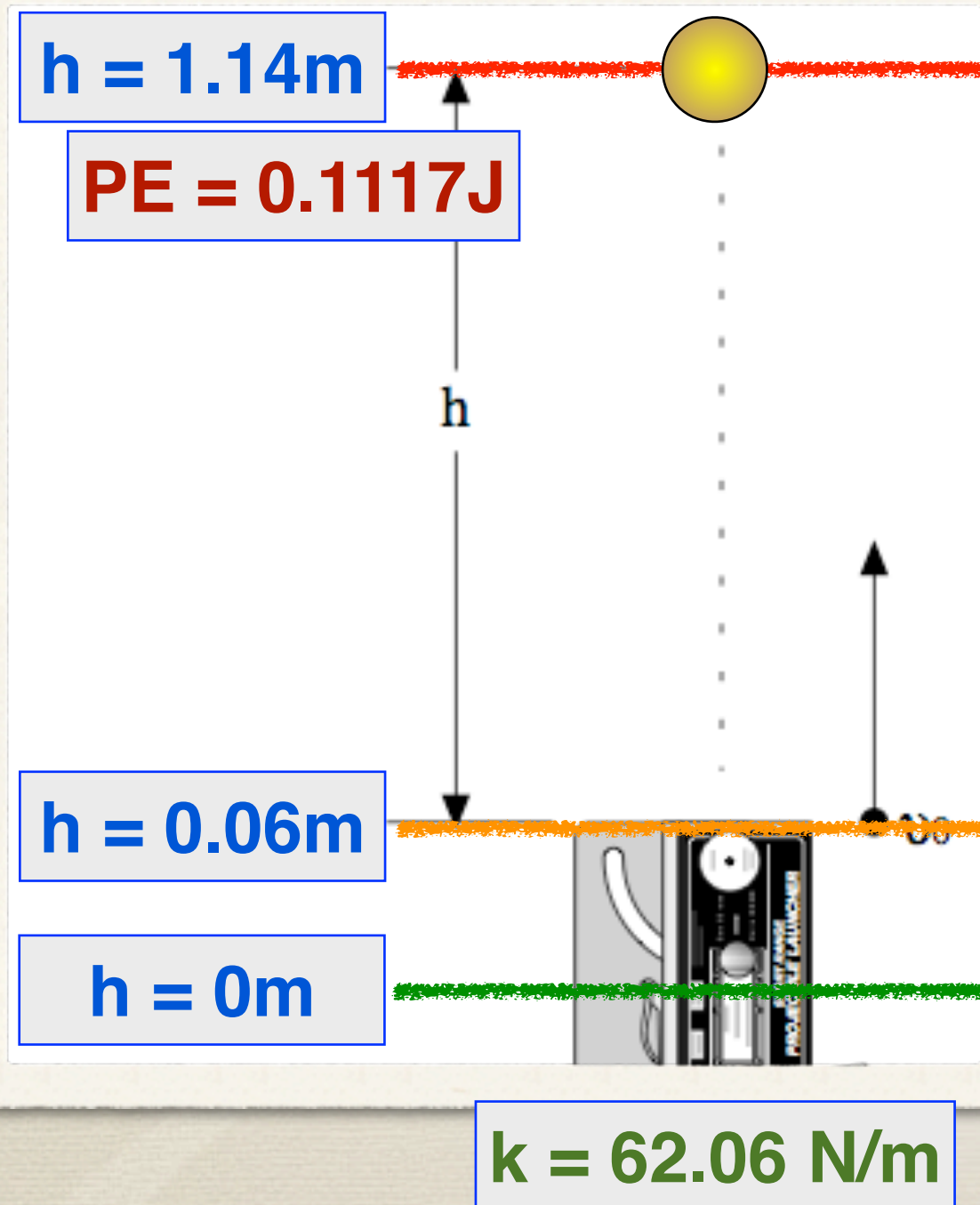
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- $0.1058\text{ J} = \frac{1}{2}(mv^2)$

Elastic Potential

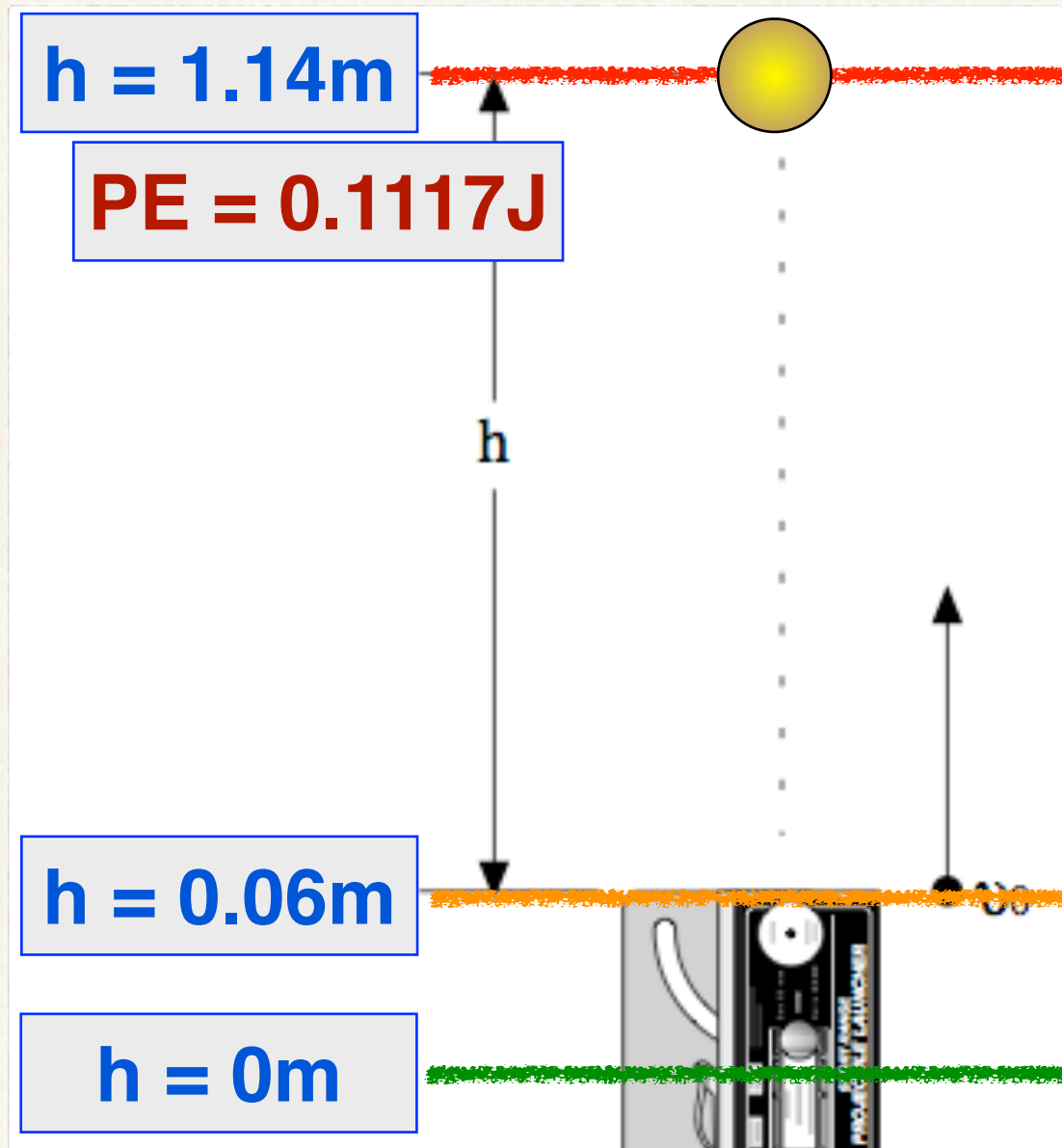
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- $0.1058\text{ J} = \frac{1}{2}(mv^2)$
- $0.1058\text{ J} = \frac{1}{2}(0.010)v^2$

Elastic Potential

- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.

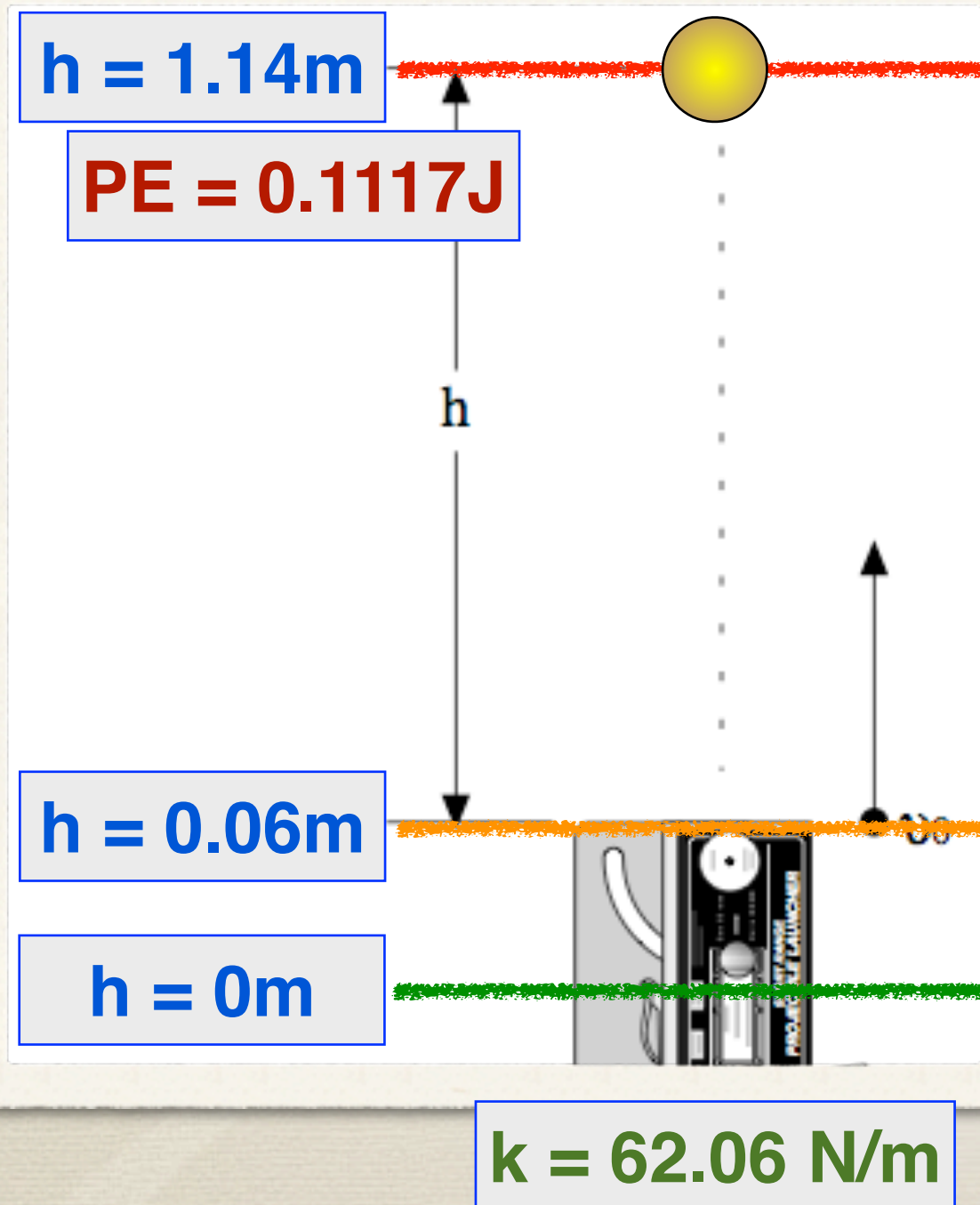


$$k = 62.06 \text{ N/m}$$

- Find the KE and the velocity
- $PE = (0.010\text{kg})(9.8)(0.06)$
- $PE = 0.00588 \text{ J} = 5.88 \text{ mJ}$
- $KE = 0.1117 - 0.00588 = 0.1058 \text{ J}$
- $0.1058 \text{ J} = \frac{1}{2}(mv^2)$
- $0.1058 \text{ J} = \frac{1}{2} (0.010) v^2$
- $v = 4.6 \text{ m/s}$

Elastic Potential

- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.

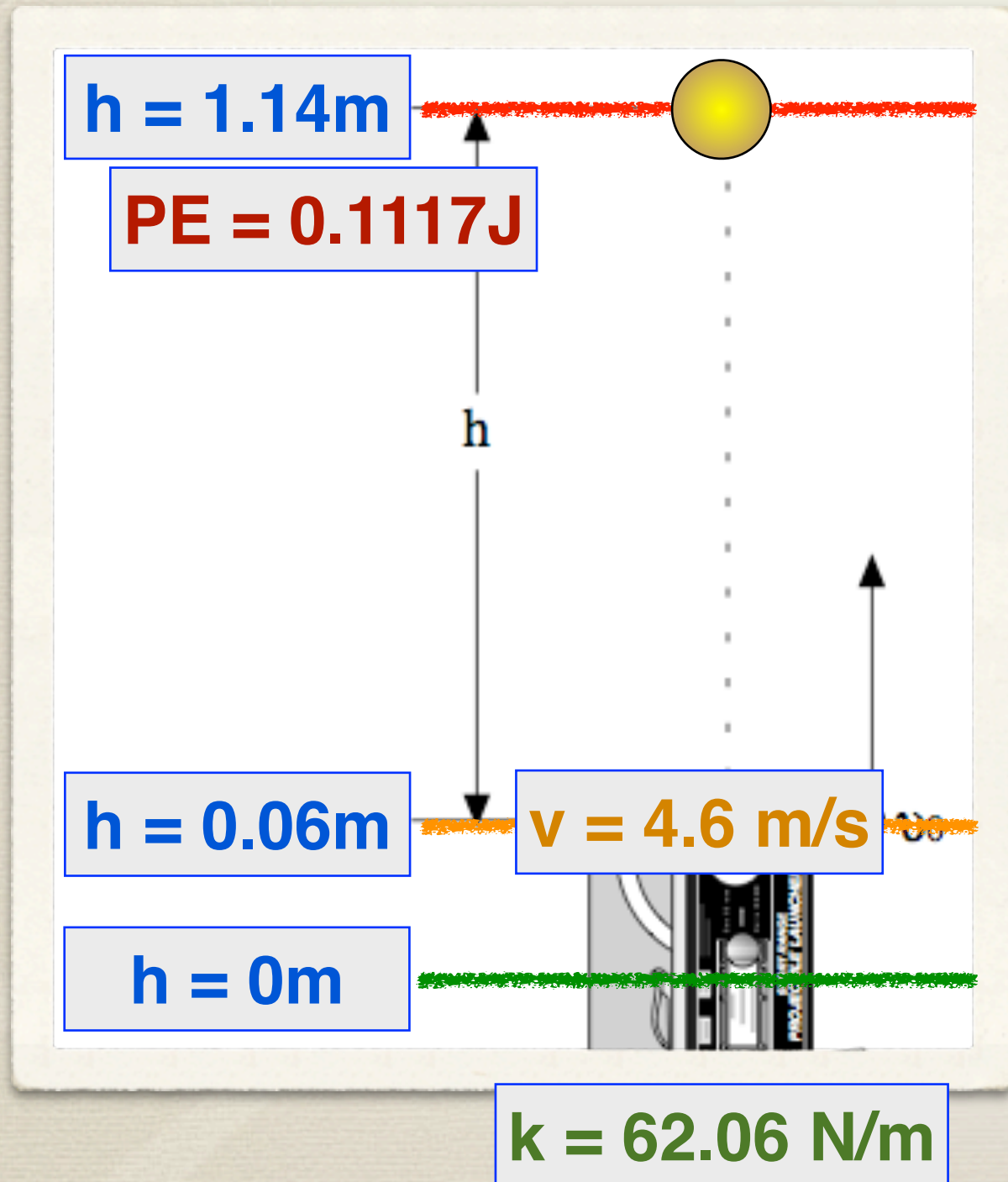


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- $0.1058 \text{ J} = \frac{1}{2} (0.010) v^2$
- $v = 4.6 \text{ m/s}$

and that is about what you calculated using old equations before

Elastic Potential

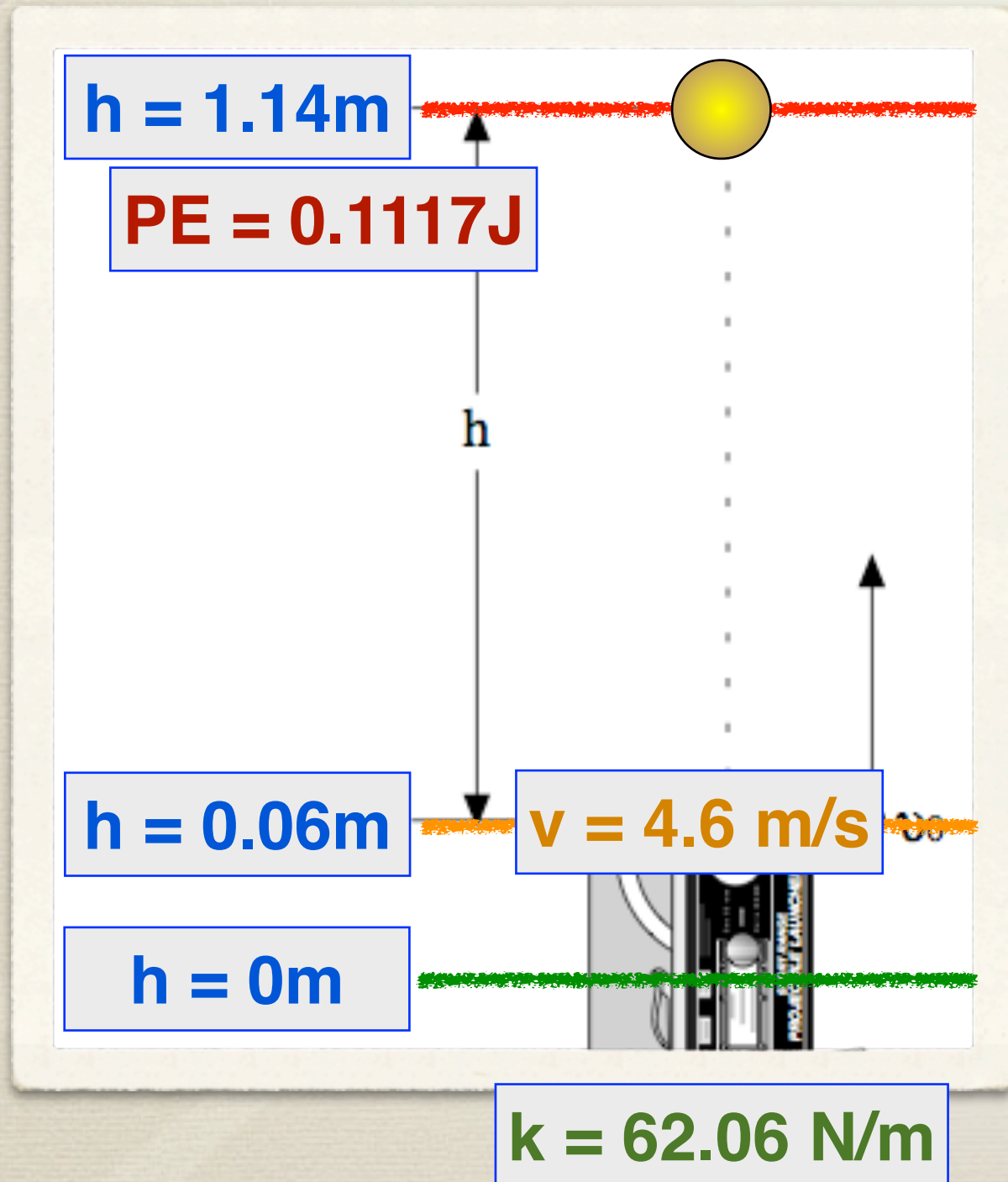
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Elastic Potential

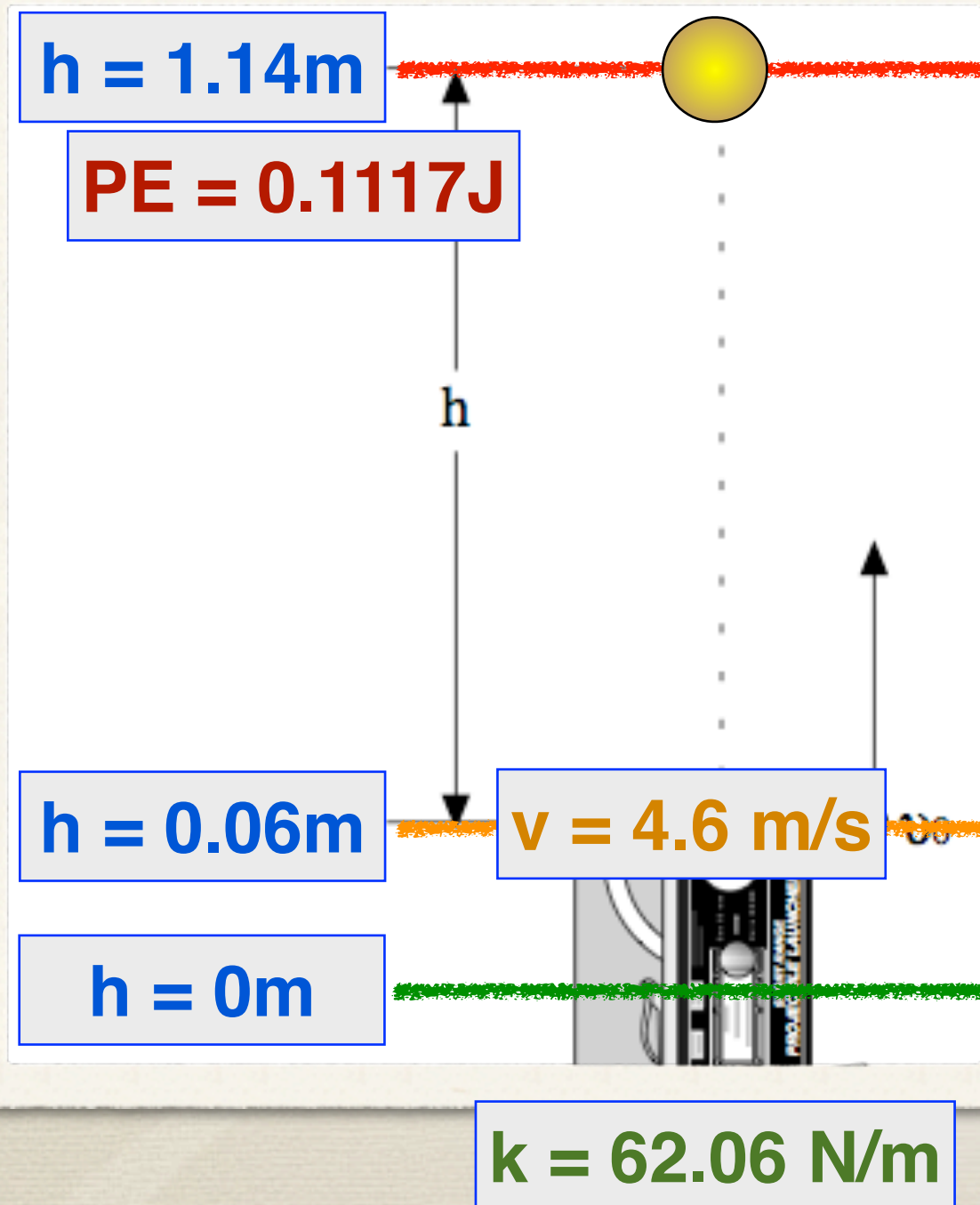
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.

- Find the maximum force used to push the spring



Elastic Potential

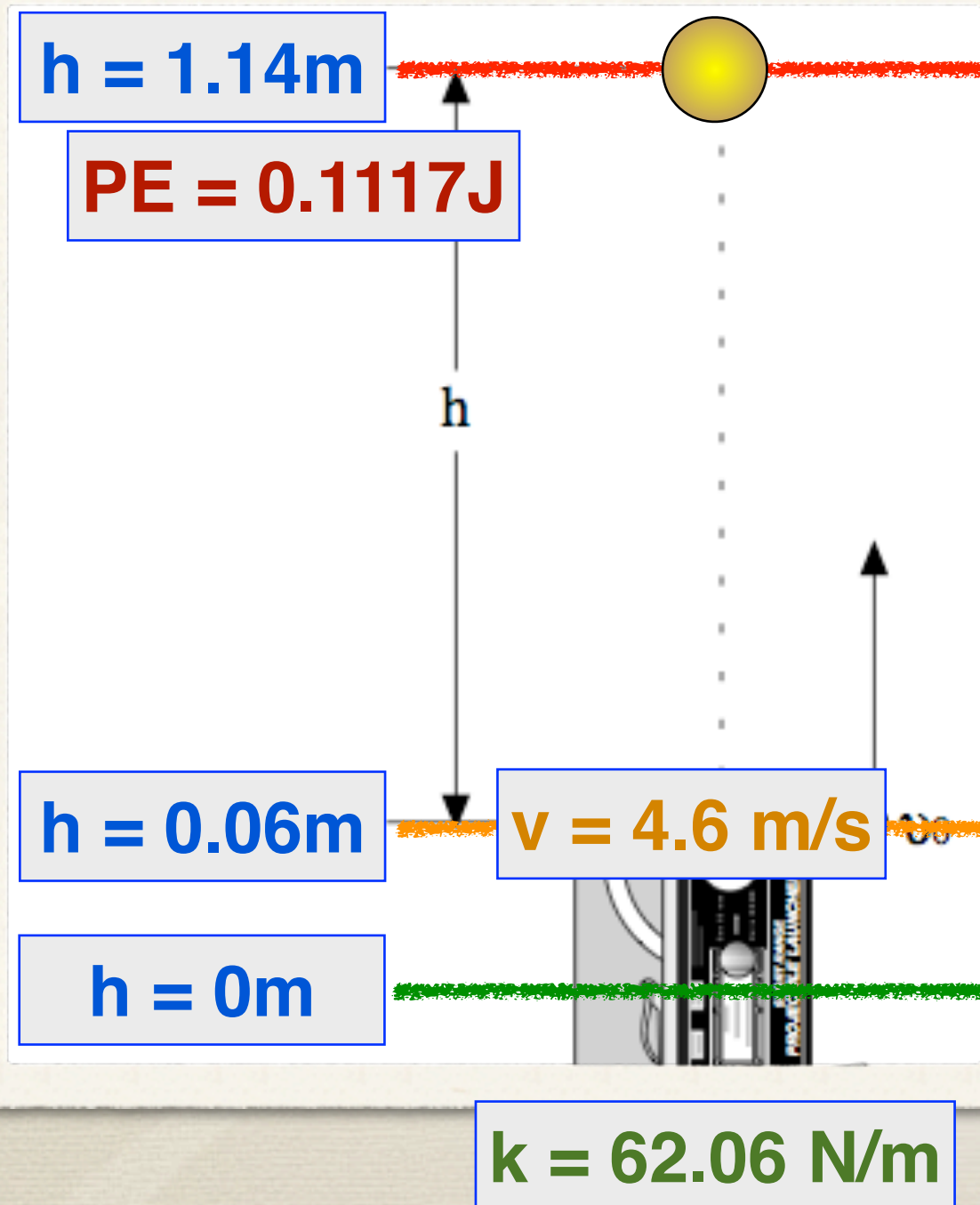
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- Find the maximum force used to push the spring
- $F = k x$

Elastic Potential

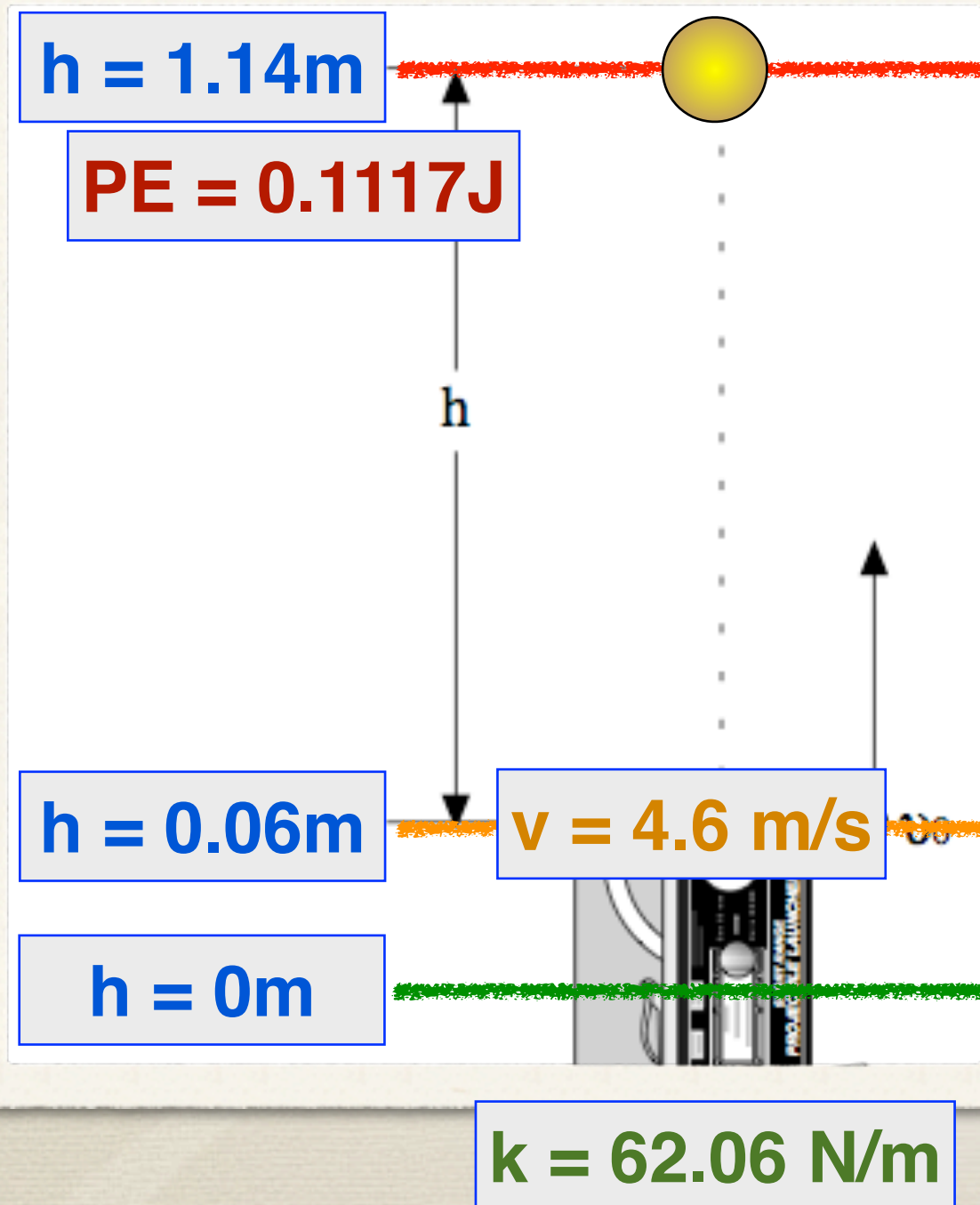
- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



- Find the maximum force used to push the spring
- $F = k x$
- $F = (62.06\text{ N/m}) (0.06\text{m})$

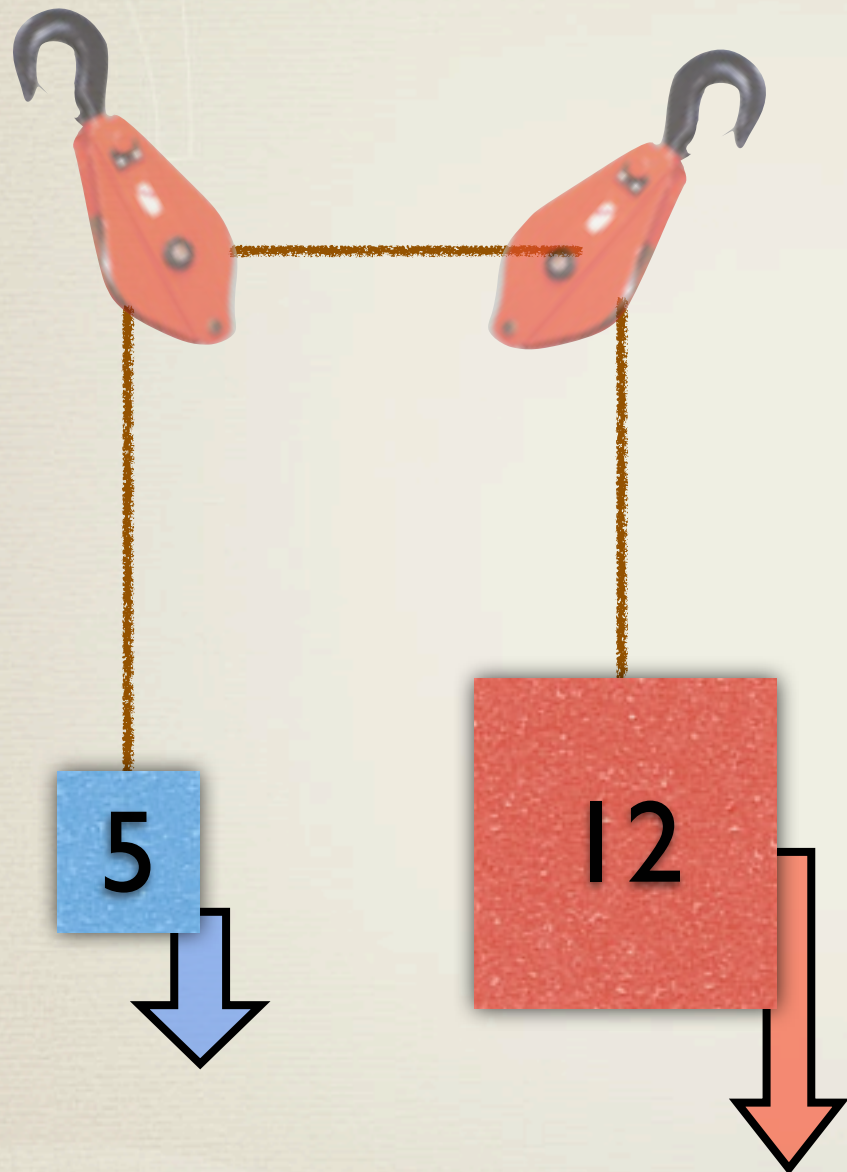
Elastic Potential

- In lab, you compressed a spring a distance of 6cm. The 10g ball went up 1.08m.



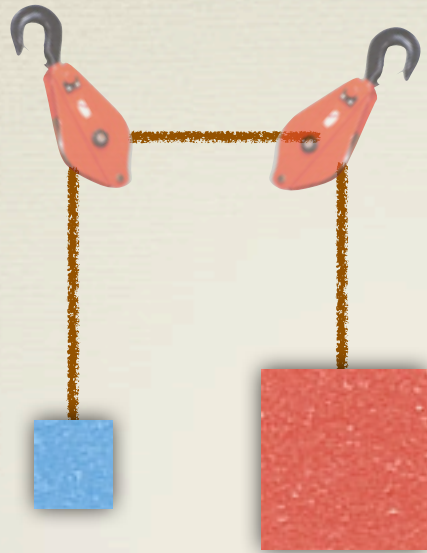
- Find the maximum force used to push the spring
- $F = k x$
- $F = (62.06 \text{ N/m}) (0.06\text{m})$
- $F = 3.7236 \text{ N}$

The Atwood Machine

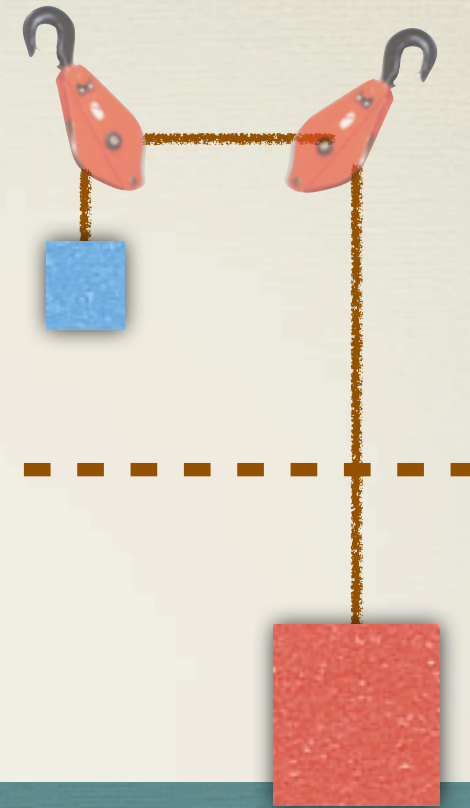


- Find the velocity of the red block as it hits the ground 3 m below.

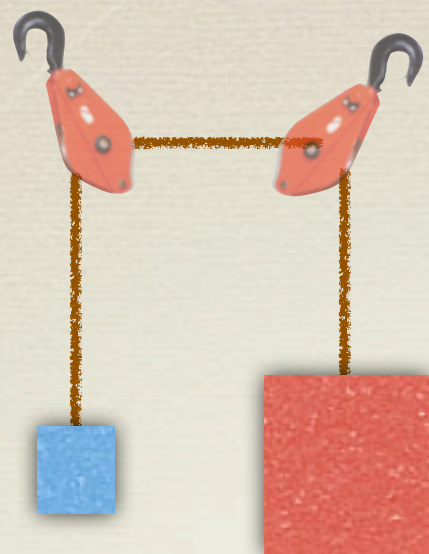
Conservation Of Energy



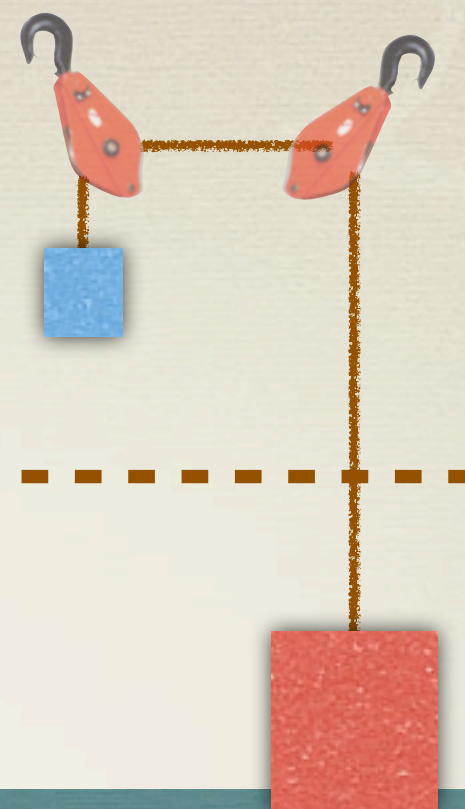
C.O.E.

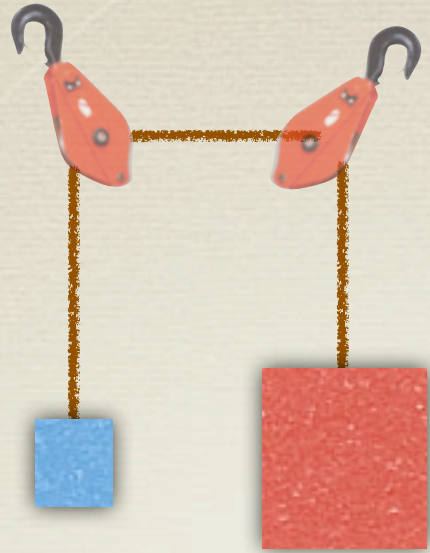


- Initial: Not moving, both have a height of 3m.
- Final: Both moving, Blue is at 6m, Red is at 0m.

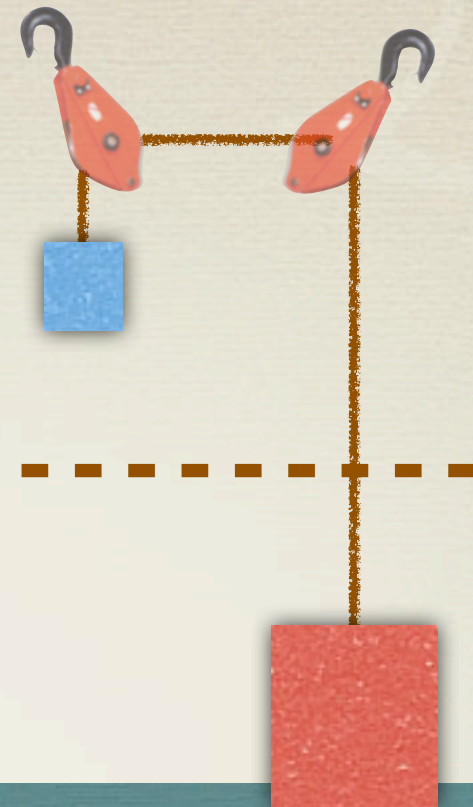


C.O.E.

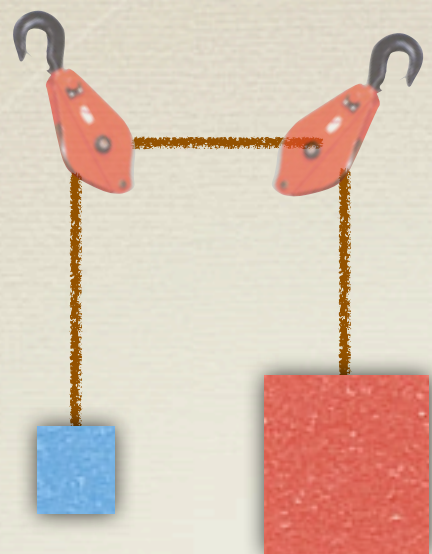




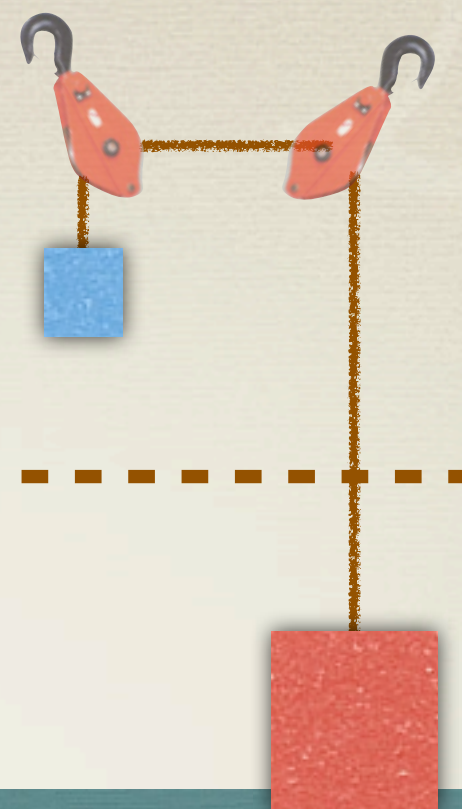
C.O.E.



$$\text{PE} + \text{PE} = \text{PE} + \text{KE} + \text{KE}$$

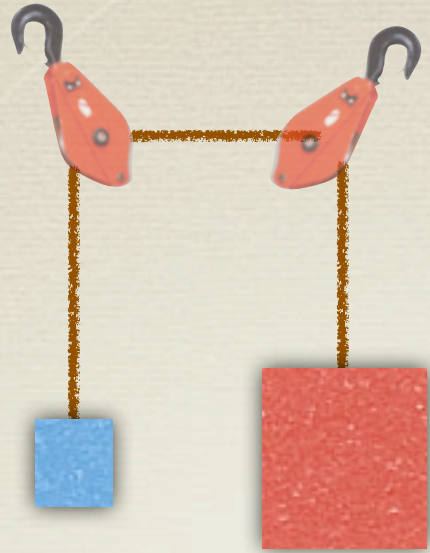


C.O.E.

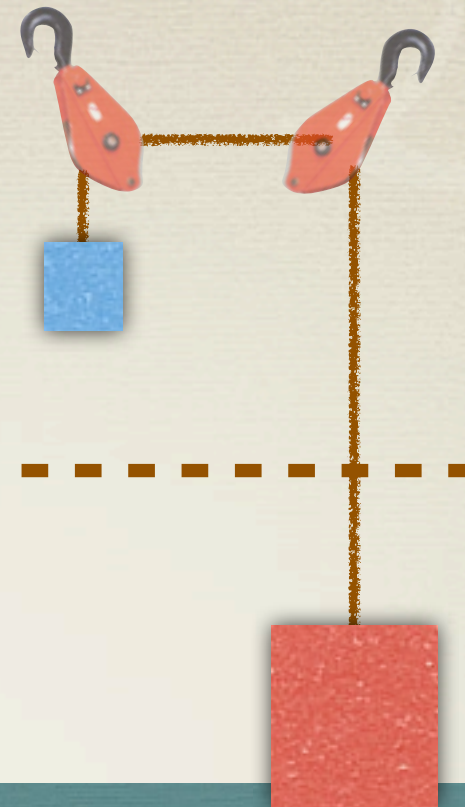


$$PE + PE = PE + KE + KE$$

$$mgh + mgh = mgh + \frac{1}{2}(mv^2) + \frac{1}{2}(mv^2)$$



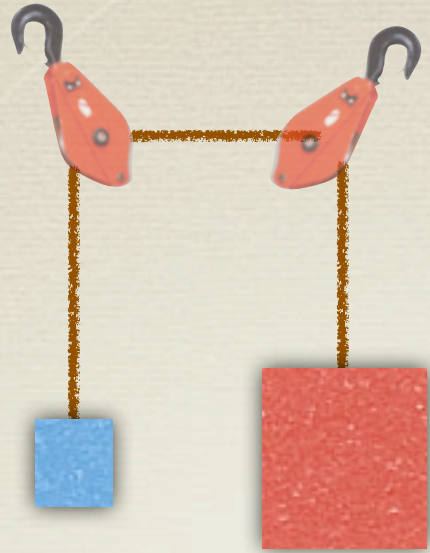
C.O.E.



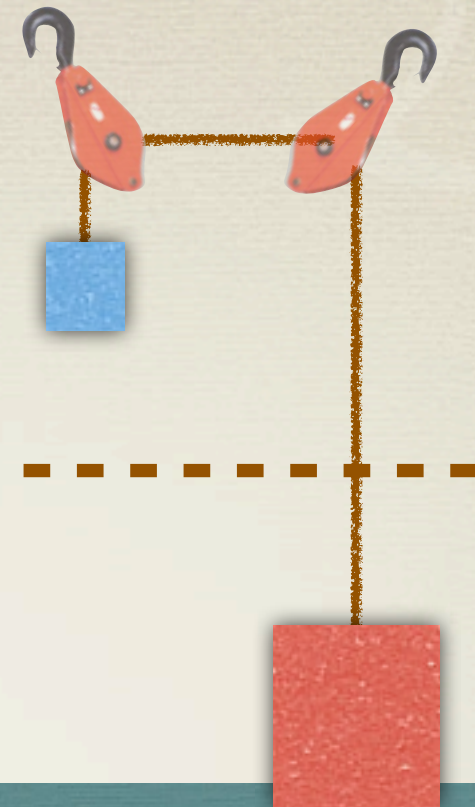
$$PE + PE = PE + KE + KE$$

$$mgh + mgh = mgh + \frac{1}{2}(mv^2) + \frac{1}{2}(mv^2)$$

$$5(9.8)(3) + 12(9.8)(3) = 5(9.8)(6) + \frac{1}{2}(5v^2) + \frac{1}{2}(12v^2)$$



C.O.E.

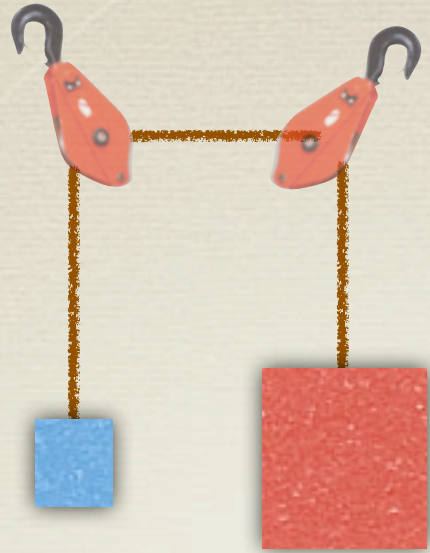


$$PE + PE = PE + KE + KE$$

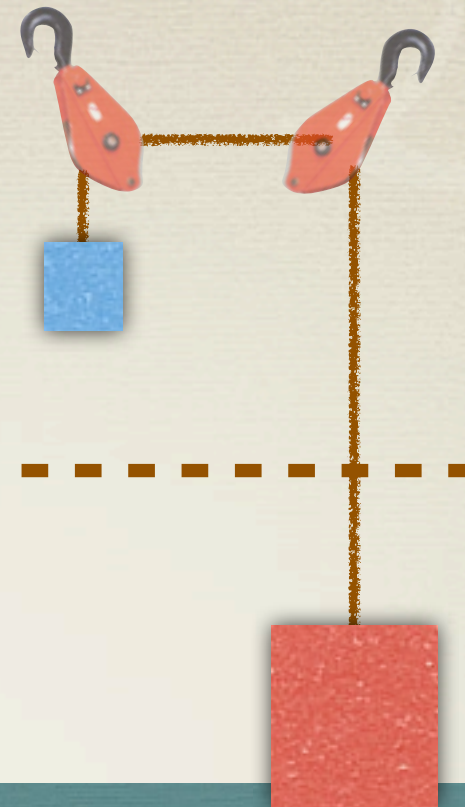
$$mgh + mgh = mgh + \frac{1}{2}(mv^2) + \frac{1}{2}(mv^2)$$

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$$147 + 352.8 = 294 + 2.5v^2 + 6v^2$$



C.O.E.



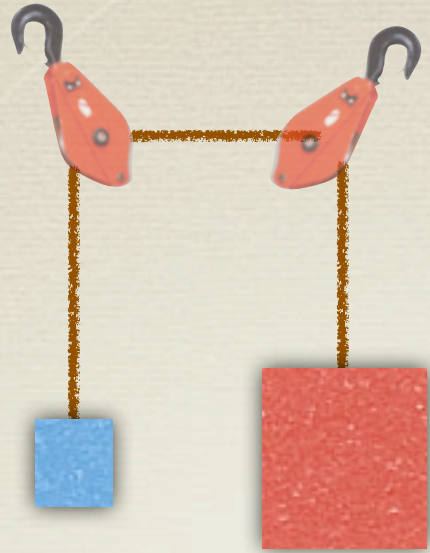
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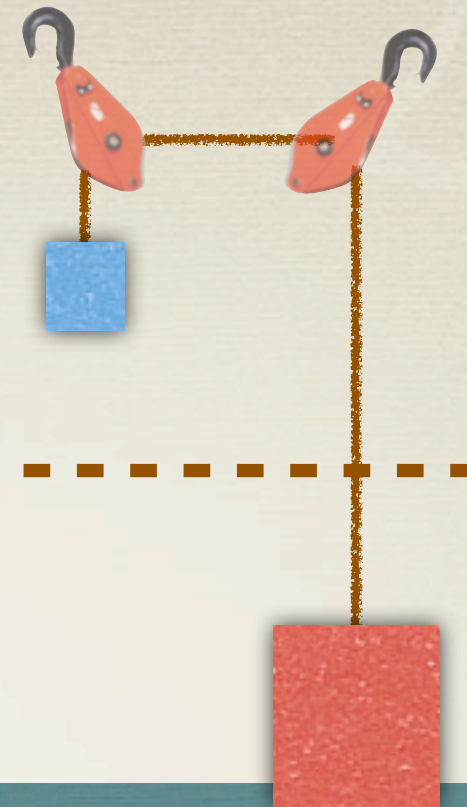
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$$205.8 = 8.5v^2$$



C.O.E.



$$PE + PE = PE + KE + KE$$

$$mgh + mgh = mgh + \frac{1}{2}(mv^2) + \frac{1}{2}(mv^2)$$

$$5(9.8)(3) + 12(9.8)(3) = 5(9.8)(6) + \frac{1}{2}(5v^2) + \frac{1}{2}(12v^2)$$

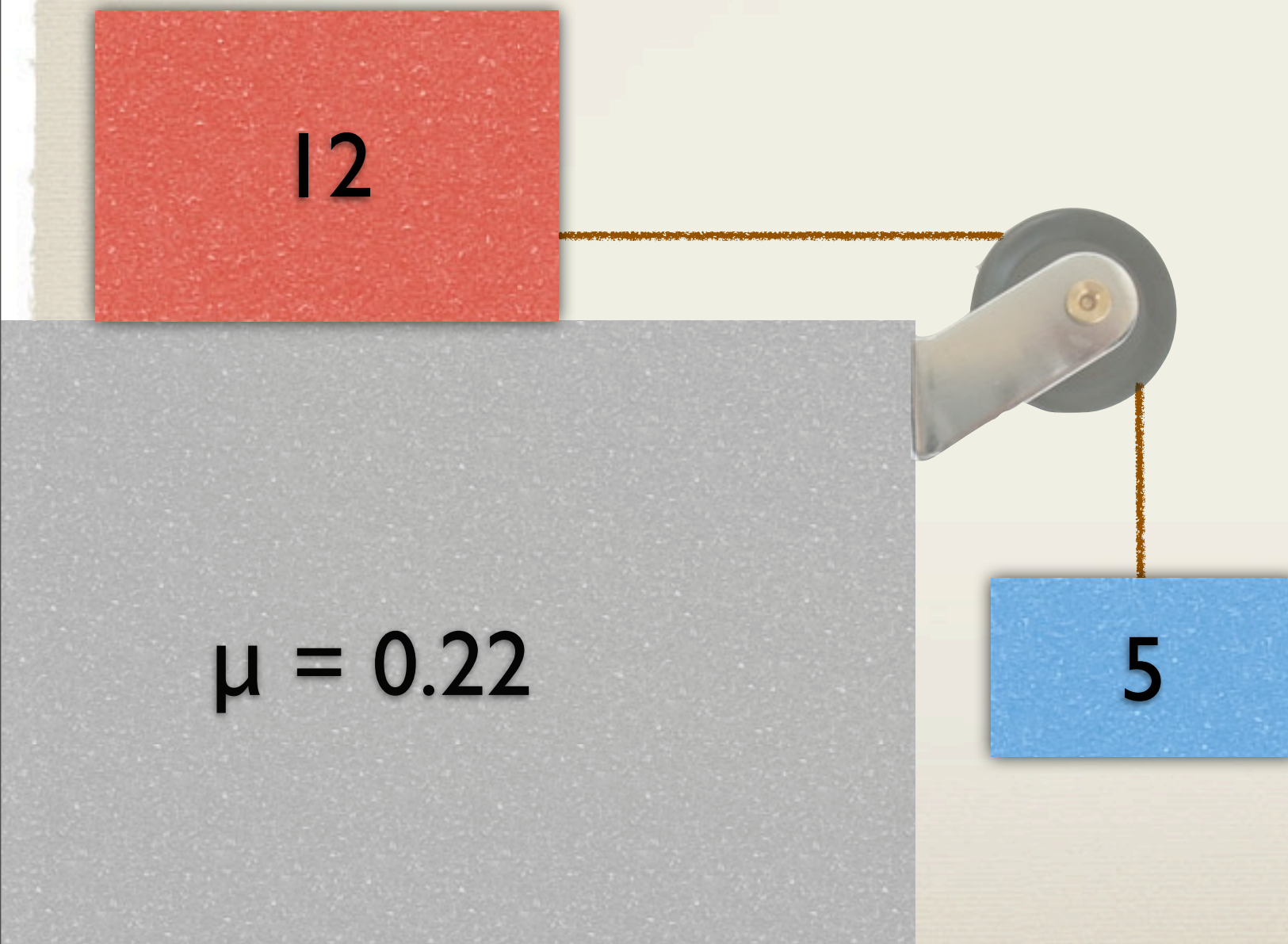
$$147 + 352.8 = 294 + 2.5v^2 + 6v^2$$

$$205.8 = 8.5v^2$$

$$4.92 = v$$

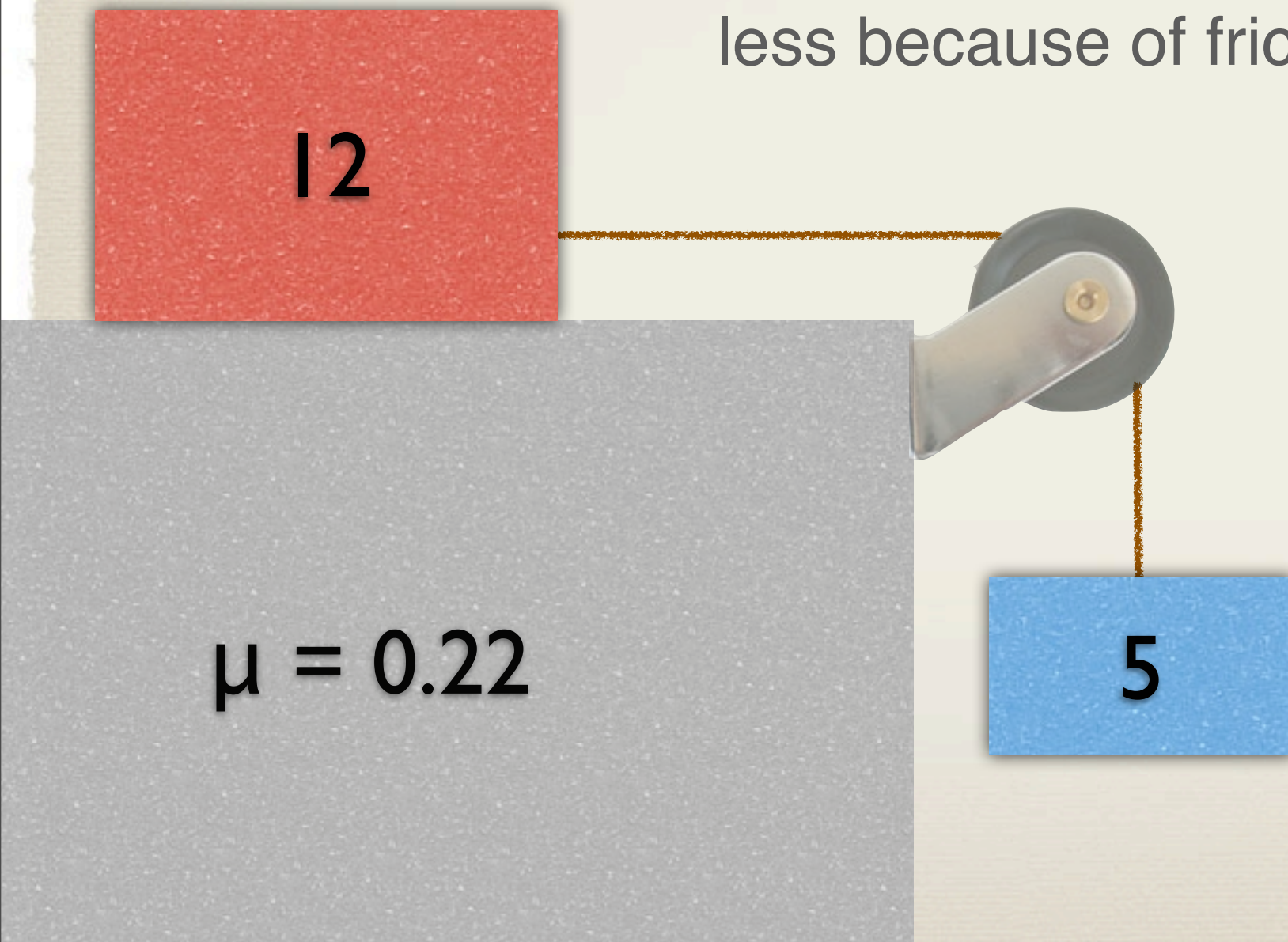
Energy Lost to Friction

- Find the velocity of the blue block as it hits the ground 8m below.

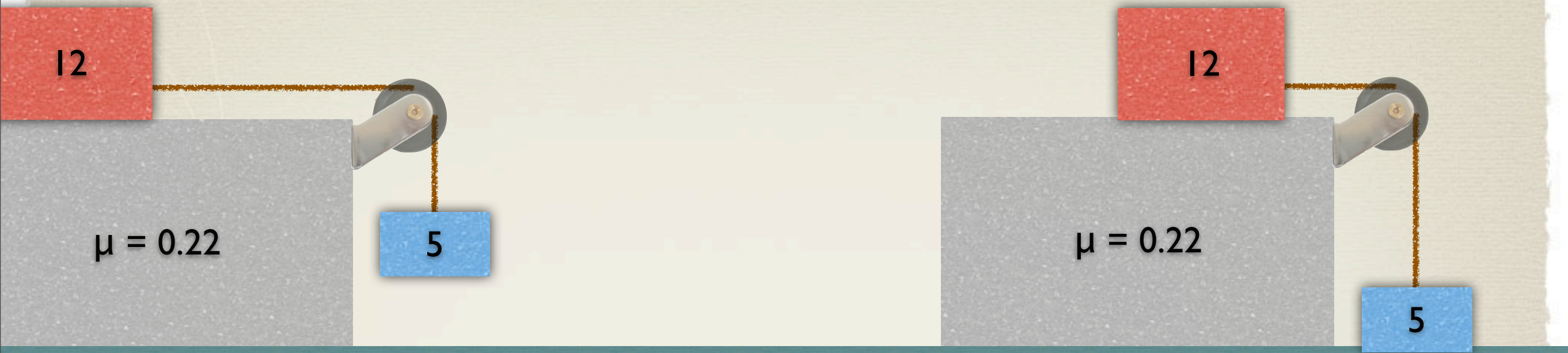


Energy Lost to Friction

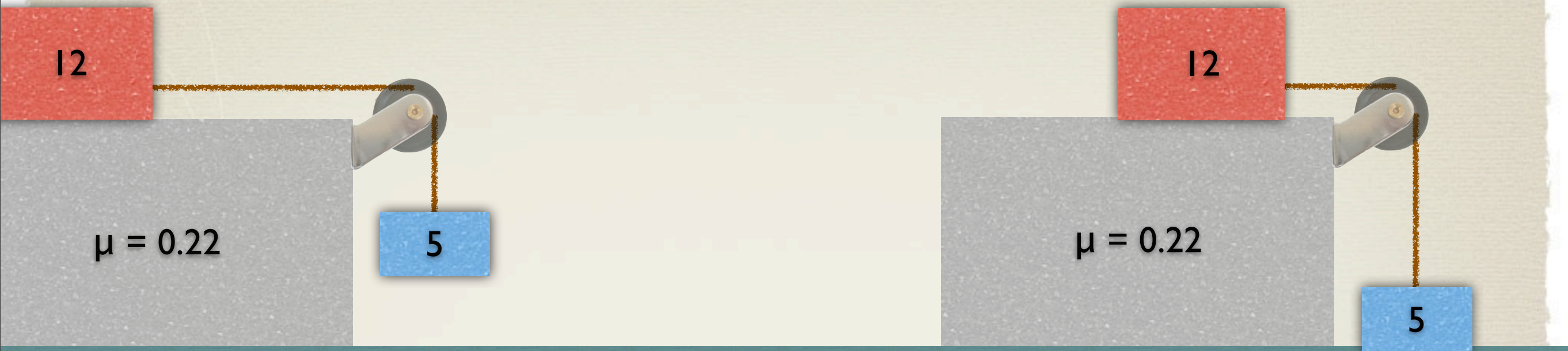
- ▶ Initial; the blue block has potential energy.
- ▶ Final; both blocks have kinetic, and TE is less because of friction.



Energy Lost to Friction

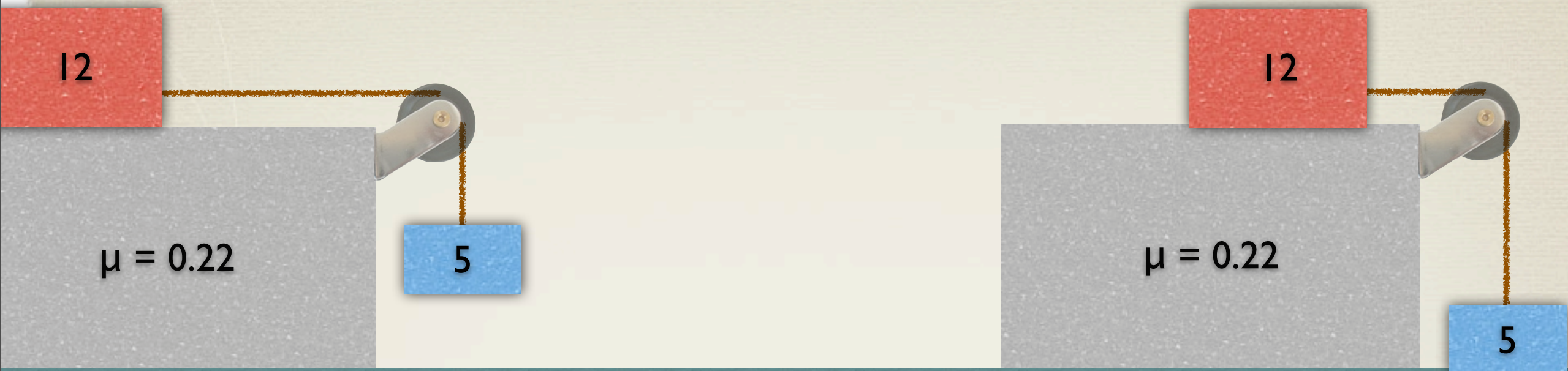


Energy Lost to Friction



$$PE = W_f + KE + KE$$

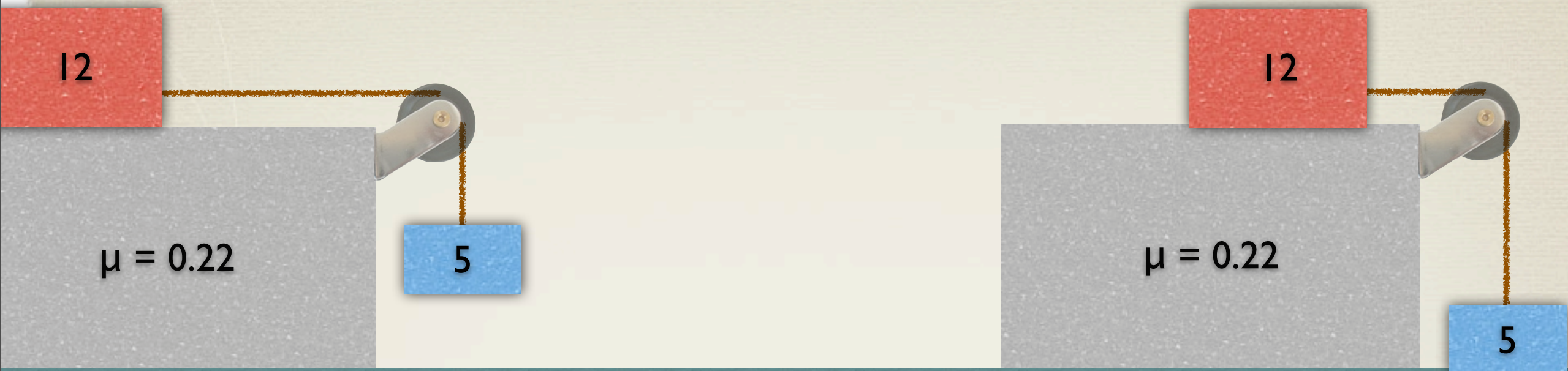
Energy Lost to Friction



$$PE = W_f + KE + KE$$

$$mgh = (\mu N)d + \frac{1}{2}(mv^2) + \frac{1}{2}(mv^2)$$

Energy Lost to Friction

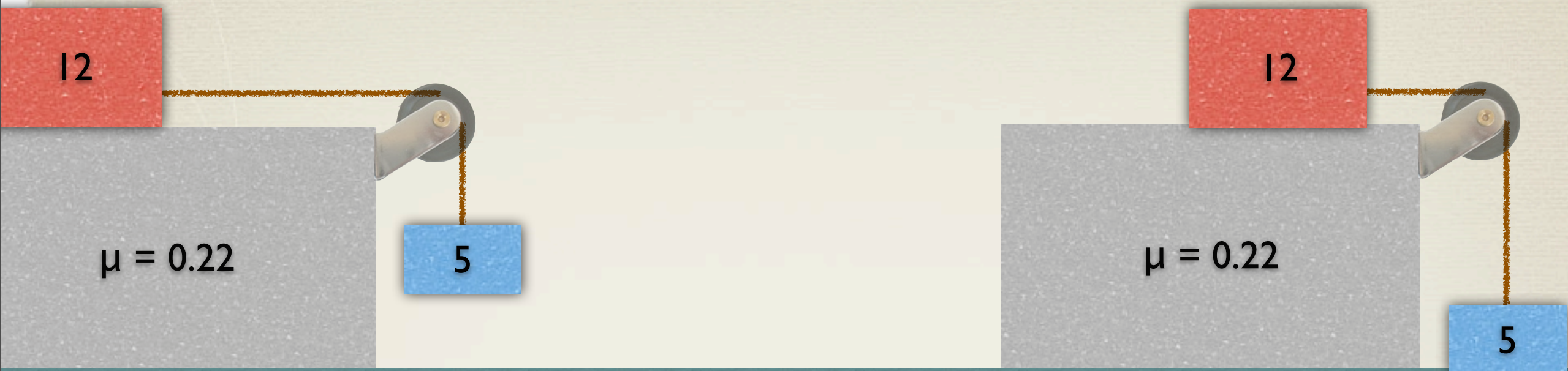


$$PE = W_f + KE + KE$$

$$mgh = (\mu N)d + \frac{1}{2}(mv^2) + \frac{1}{2}(mv^2)$$

$$5(9.8)(8) = (0.22)(12(9.8))(8) + \frac{1}{2}(5v^2) + \frac{1}{2}(12v^2)$$

Energy Lost to Friction



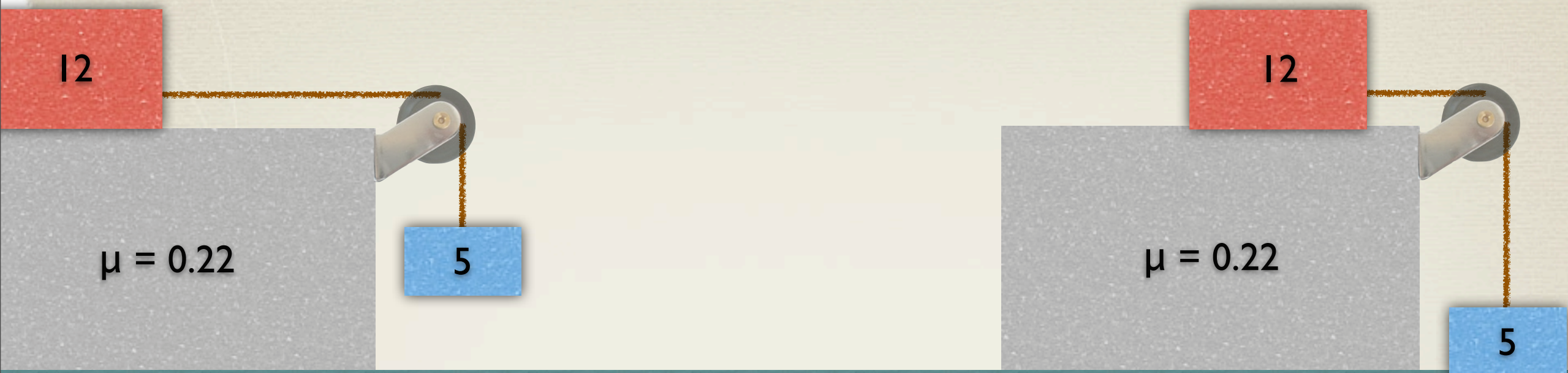
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$$392 = 206.98 + 2.5v^2 + 6v^2$$

Energy Lost to Friction



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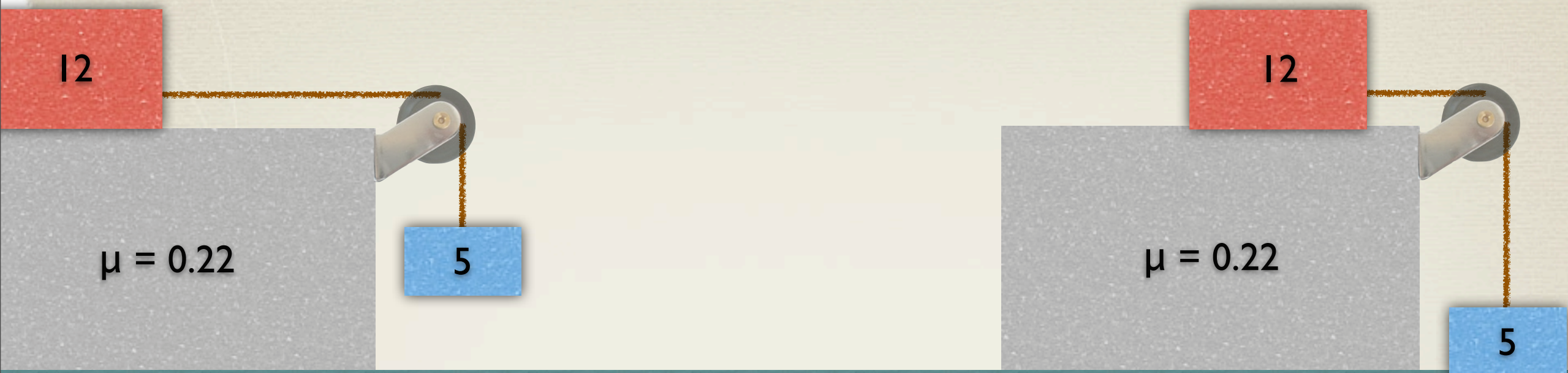
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$$392 = 206.98 + 2.5v^2 + 6v^2$$

$$185 = 8.5v^2$$

Energy Lost to Friction



$$PE = W_f + KE + KE$$

$$mgh = (\mu N)d + \frac{1}{2}(mv^2) + \frac{1}{2}(mv^2)$$

$$5(9.8)(8) = (0.22)(12(9.8))(8) + \frac{1}{2}(5v^2) + \frac{1}{2}(12v^2)$$

$$392 = 206.98 + 2.5v^2 + 6v^2$$

$$185 = 8.5v^2$$

$$4.67 \text{ m/s} = v$$

Academic Assignment

Academic Physics

Set 1 - Chapter 10

1, 2, 3, 5, 6, 7, 25, 26, 27, 28, 52, 53, 56, 57

Academic Physics

Set 2 - Chapter 10

60, 63, 67, 70, 71, 76, 79, 81, 83, 84, 85, 90, 93

Hooke's Law

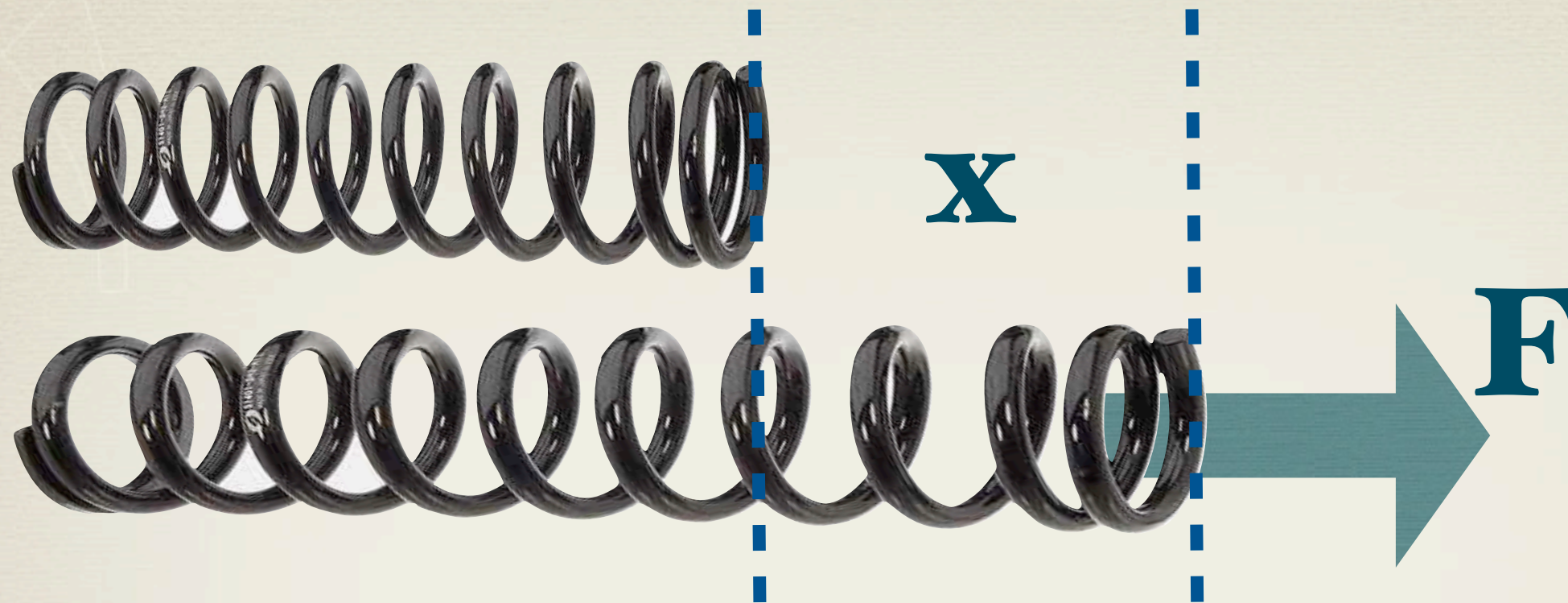


$$\mathbf{F} = (-) \mathbf{k} \mathbf{x}$$



- ▶ Force - required to stretch the spring, or restoring force. Often the weight (N)
- ▶ k - Spring Constant - How “tight” the spring is. (N/m)
- ▶ x - Stretch - a change in length (m)

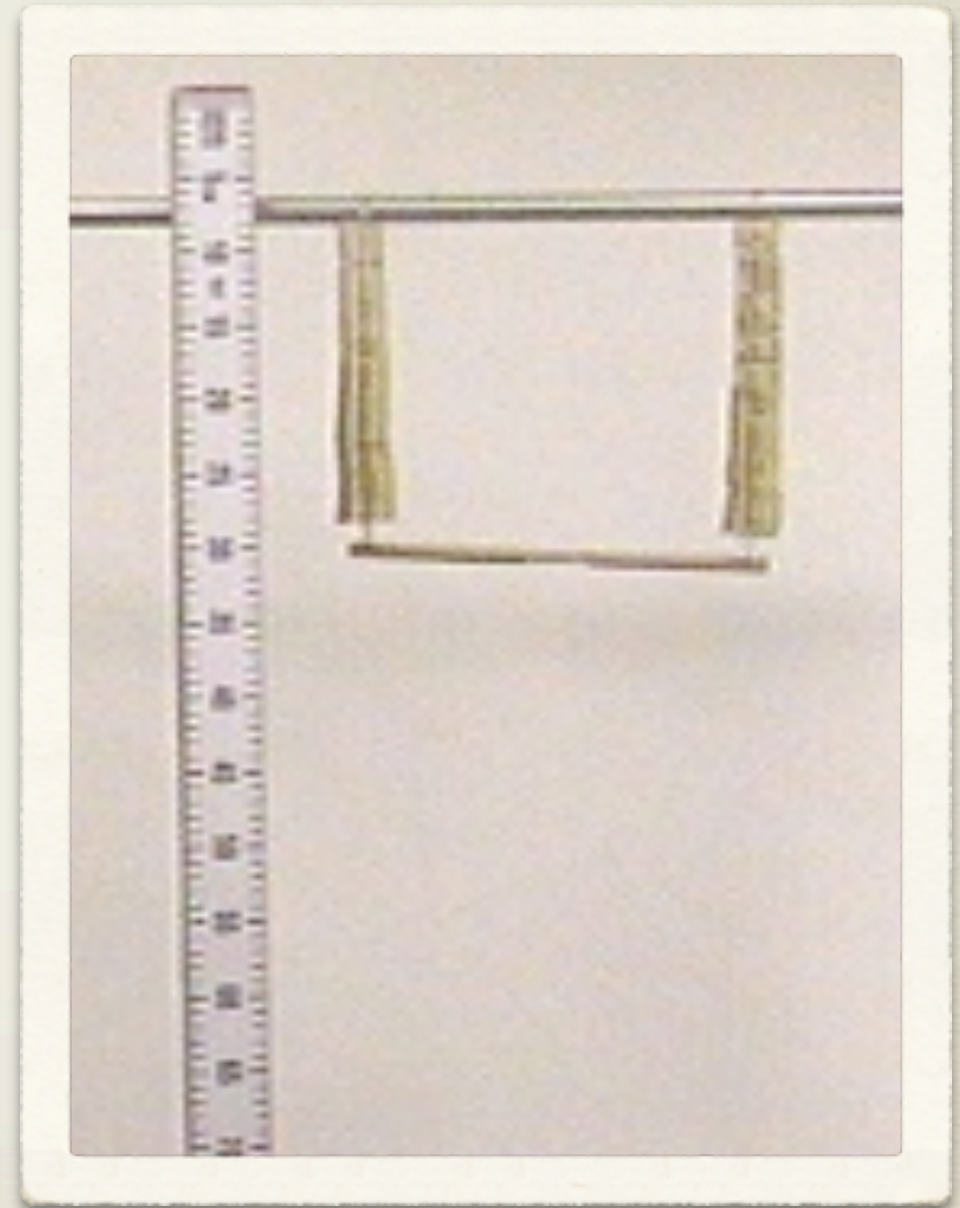
$$\mathbf{F} = (-) \mathbf{k} \mathbf{x}$$



- ▶ Force - required to stretch the spring, or restoring force. Often the weight (N)
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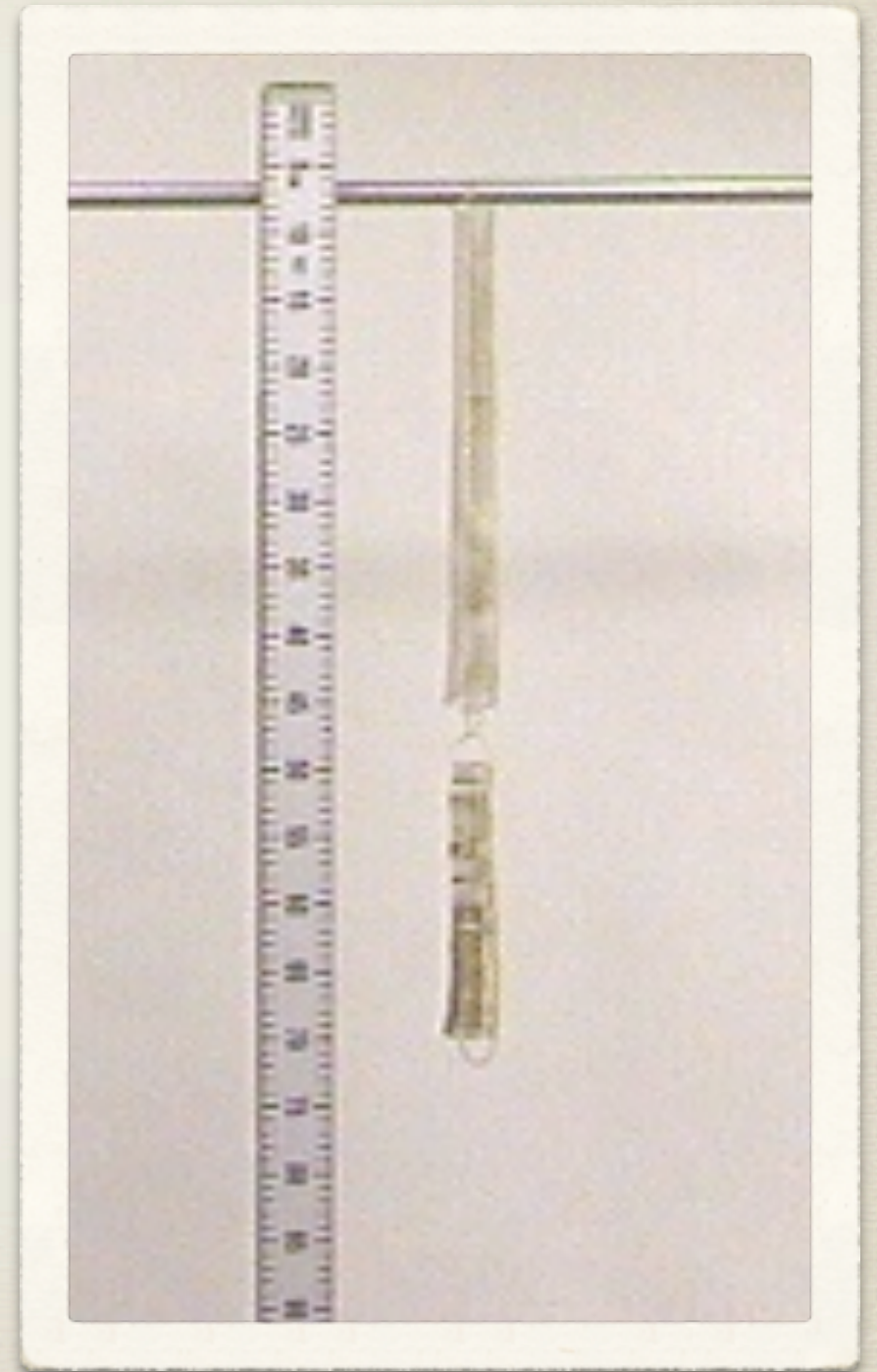
Springs in Parallel

- ▶ The same force is supported by two springs so neither has to stretch as far...
- ▶ ...or, it is harder to stretch two springs so the constant is increased
- ▶ $k = k_1 + k_2$



Springs in Series

- ▶ Both springs support the same amount of weight (not split in two like before)...
- ▶ or... it is easier to stretch
- ▶ $1/k = 1/k_1 + 1/k_2$



What is the spring constant?

► Up a track

