

# WHY would this work?

```
graph TD; Root[Root Node] --- L1[Leaf 1]; Root --- L2[Leaf 2]; Root --- L3[Leaf 3]; L1 --- L1_1[3]; L1 --- L1_2[2]; L1 --- L1_3[1]; L2 --- L2_1[4];
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### The Bottom Bar First

CCW 3x2 CW 2x1 CW 1x4

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# The Top Bar

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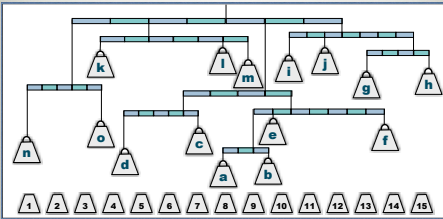
[illegible][illegible]

# Middle Example

The diagram illustrates a Huffman tree for the letters a-j. The root node has three children: 'i', an internal node, and 'j'. The internal node has three children: 'f', 'g', and 'h'. The 'f' node has two children: 'a' and 'b'. The 'g' node has two children: 'c' and 'd'. The 'h' node has one child: 'e'. Below the tree is a sequence of 10 leaf nodes labeled 1 through 10.

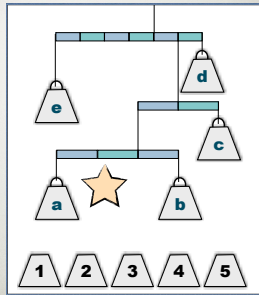
[illegible]

## The "IMPOSSIBLE" one



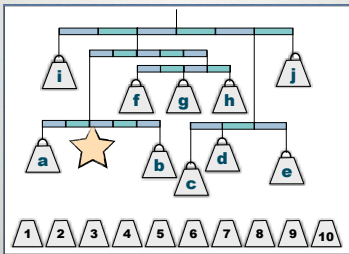
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## Easy Sample



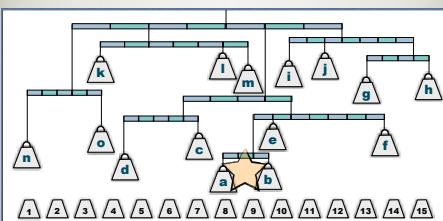
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## Middle Example



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## The "IMPOSSIBLE" one



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## Torque



What is the BEST way to open a door?

- The most force
- The right direction
- Far from the hinges

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$$T = F d \sin\theta$$

Torque (Nm)

Force (N)

distance (m)

or  $r$  for radius or  $l$  for lever arm

$\theta$  the angle between  $F$  and  $d$

so, push on a door at a right angle with a force of 25N,  
80cm from the hinges...

$$\text{Torque (Nm)} = 25\text{N} \cdot 0.8\text{m} \sin 90^\circ$$

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### Three States of Equilibrium

Vertical Forces -

"Ups" equal "Downs"

Horizontal Forces -

"Lefts" equal "Rights"

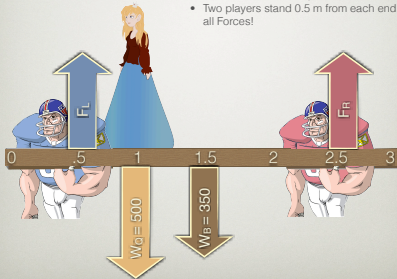
Torques -

"Clockwise" equals "Counter-clockwise"

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### Create a Free Body Diagram of the Board

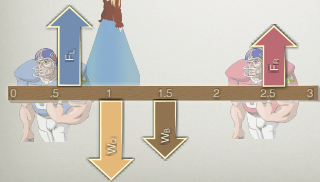
- The 500 N homecoming queen stands 1 m from the end of a 3 m, 350 N board as shown.
- Two players stand 0.5 m from each end. Find all Forces!



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### Vertical (y direction) Forces

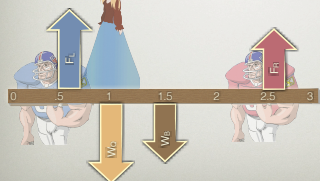
$$\begin{array}{c} \text{Up} = \text{Down} \\ F_L + F_R = 500 + 350 \end{array}$$



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### Horizontal (x direction) Forces

$$\begin{array}{c} \text{Left} = \text{Right} \\ 0 = 0 \\ \text{(but make sure you state this anyway)} \end{array}$$



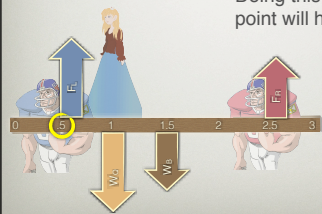
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## Torque- Turning Forces

pick a point where it is not turning

Pick any Axis

Doing this at a variable point will help



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Player L

$$\text{CCW} = \text{CW}$$

$$F_R(2)\sin 90 = 350(1)\sin 90 + 500(0.5)\sin 90$$

$$F_L(0)\sin 90 \text{ No Torque}$$

Torque  $T = F d \sin \theta$

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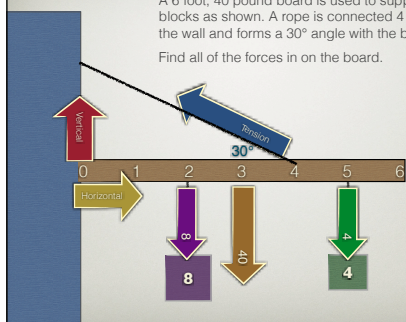
## Check

If you have picked a good place for your axis of rotation, you should have only simple algebra to handle.

If you have time, pick another axis of rotation and be sure that you get the same answer.

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A 6 foot, 40 pound board is used to support two blocks as shown. A rope is connected 4 feet from the wall and forms a  $30^\circ$  angle with the board. Find all of the forces in on the board.



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$$\text{Up} = \text{Down}$$

$$V + T \sin 30 = 8 + 40 + 4$$

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$T \cos 30^\circ = H$

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Finish Your Math

$CCW = CW$

$T(4)\sin 30 = 4(5)\sin 90 + 40(3)\sin 90 + 8(2)\sin 90$

$T(2) = 4(5) + 40(3) + 8(2)$

$T = 78 \text{ lb}$

$L = R$

$T \cos 30^\circ = H$

$H = 67.5 \text{ lb}$

$U = D$

$V + T \sin 30 = 8 + 40 + 4$

$V = 13 \text{ lb}$

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Climbing a Ladder  
Find all Forces

A 75 kg man has climbed 2 meters up a 7 meter ladder. The ladder has a mass of 55kg, and it forms a 60° angle with the ground. Find all forces.

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Climbing a Ladder  
Find all Forces

- Weight of Ladder
- 55 × 9.8
- Weight of Climber
- 75 × 9.8
- Normal
- "Wall"
- Horizontal

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Climbing a Ladder  
Find all Forces

$U = D$

$N = 735 + 539$

$N = 1274 \text{ N}$

$L = R$

$H = W$

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$CW = CCW$   
 $W(7)(\sin 60) = 539(3.5)(\sin 30)$   
 $735(2)(\sin 30)$   
 $W = 276.8 \text{ N}$

*Now finish your math*  
 $H = W$   
 $H = 276.8 \text{ N}$

*And Maybe...*  
 $F = \mu N$   
 $276.84 = \mu 1274$

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### Find all Forces

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### First, isolate the tire

$U = D$   
 $T_1 = 24(9.8)$   
 $T_1 = 235.2 \text{ N}$

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### Next, isolate the "knot"

$U = D$   
 $T_{gy} + T_{ry} = T_1$   
 $T_g \sin 48 + T_r \sin 16 = 235.2 \text{ N}$   
 $T_g = 316.49 - 0.371(T_r)$

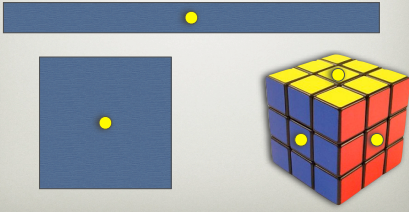
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$L = R$   
 $T_{gx} = T_{rx}$   
 $T_g \cos 48 = T_r \cos 16$   
 from u=d:  
 $T_g = 316.49 - 0.371(T_r)$   
 $211.77 - 0.248 T_r = 0.961 T_r$   
 $211.77 = 1.209 T_r$   
 $T_r = 175.1 \text{ N}$   
 $\therefore T_g = 251.5 \text{ N}$

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## Find the Center

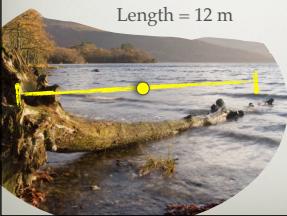
Easy sometimes



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## Find the Center

Length = 12 m



- Where is the center of mass for this tree?
- half the length?

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## Find the Center



$$x_{cm} = \frac{x_1 m_1 + x_2 m_2 + x_3 m_3}{m_{total}}$$

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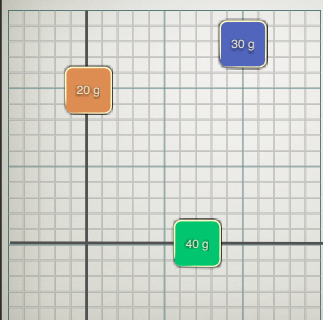
## Find the Center



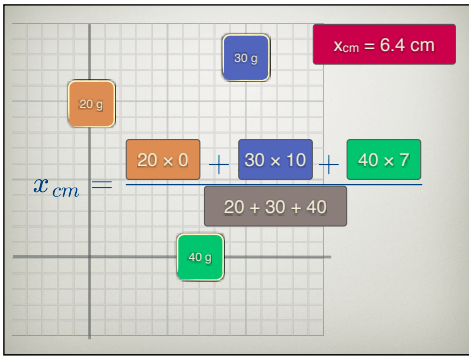
$$x_{cm} = \frac{15 \times 1 + 25 \times 6 + 50 \times 14}{15 + 25 + 50}$$

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## Find the Center



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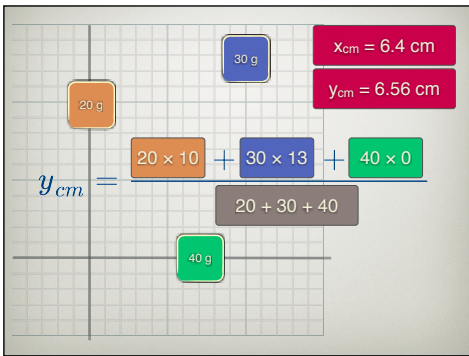
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